

Министерство образования и науки Российской Федерации
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«Уфимский государственный авиационный технический университет»

На правах рукописи



УСМАНОВА Регина Равилевна

**ПОВЫШЕНИЕ ЭФФЕКТИВНОСТИ ГАЗООЧИСТКИ
В ИНЕРЦИОННЫХ АППАРАТАХ С АКТИВНОЙ ГИДРОДИНАМИКОЙ**

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Научный консультант:
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УФА – 2017

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3.1		
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6.2		221
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3. $\frac{\partial}{\partial t} + \mathbf{U} \cdot \nabla$
4. $\frac{\partial}{\partial t} + \mathbf{U} \cdot \nabla$
5. $\frac{\partial}{\partial t} + \mathbf{U} \cdot \nabla$
6. $\frac{\partial}{\partial t} + \mathbf{U} \cdot \nabla$

Ansys CFX.

U', U'_r, U'_z

(r, z)

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 i=(0,5...7,5) % () i= (2,15...11,5) % (i<13%.
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CFX.

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$U', U'_r, U',$

(r, z)

Ansys

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CFX.

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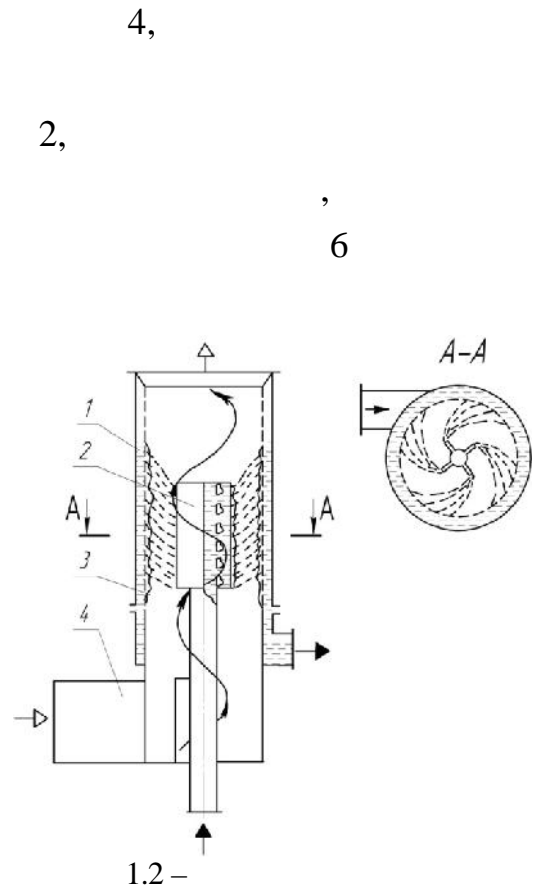
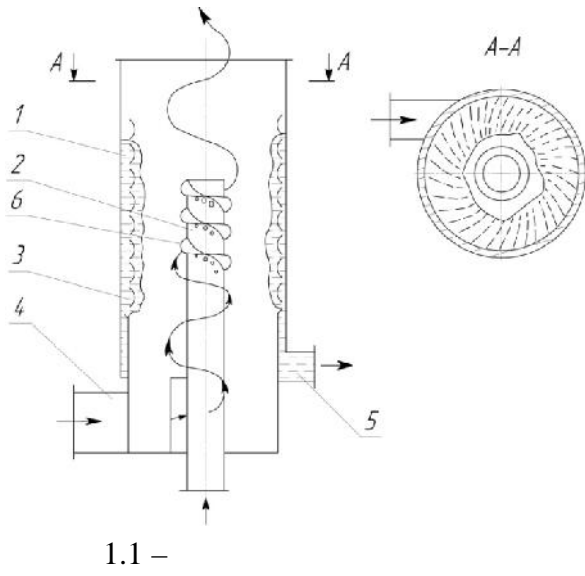
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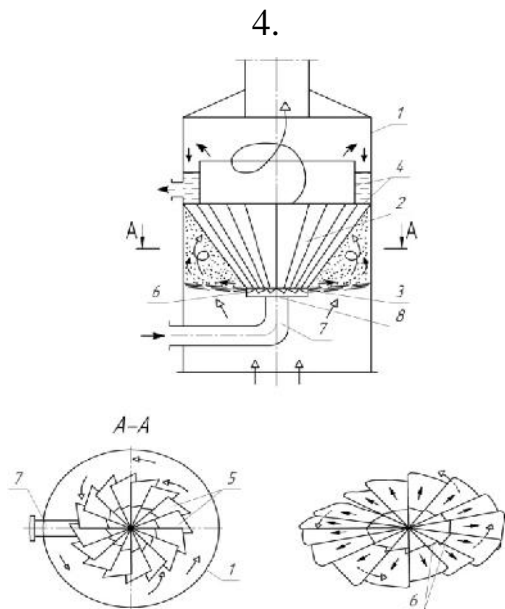
1.2,

[21],

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2, 4, 1, 2, () 3. 5 90% [100]. 1500 5

[22], 1.3, 2, 3

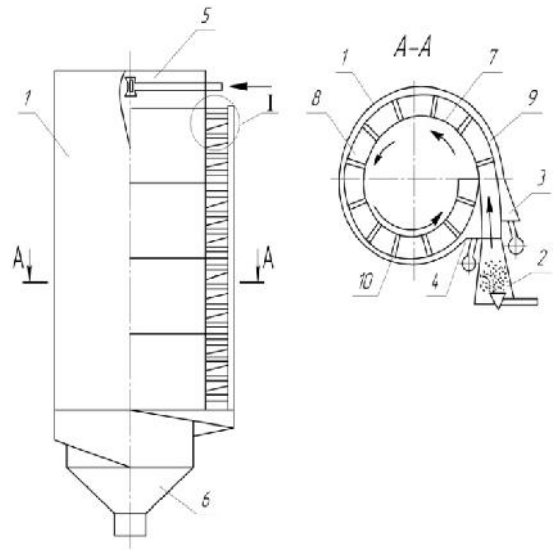


1.3 - ; 1 - ; 2 - ; 3, 4 - ; 5 - ; 6 - ; 7 - ; 8 - ; 2.

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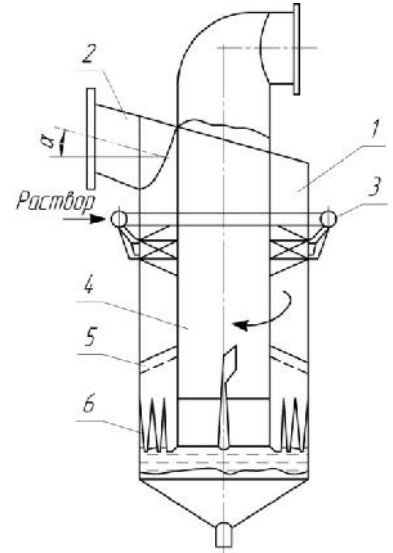
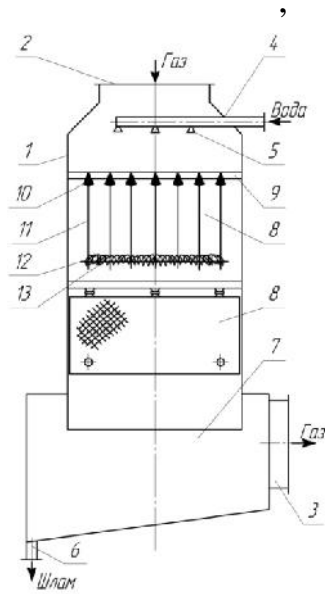
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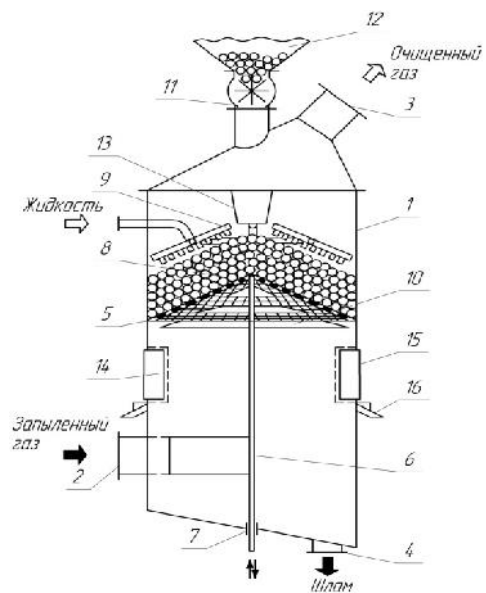
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- 11 - ; 12 - ;
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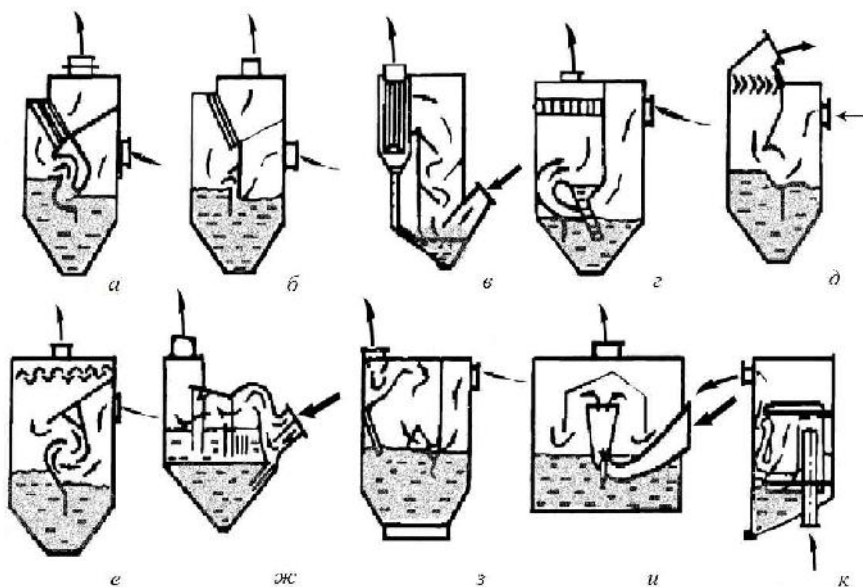
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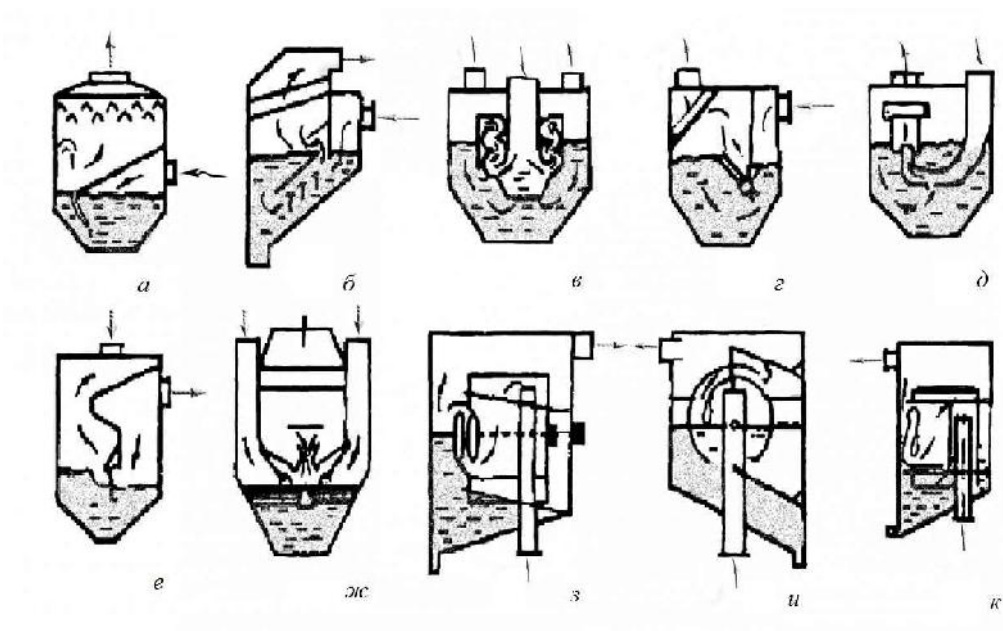
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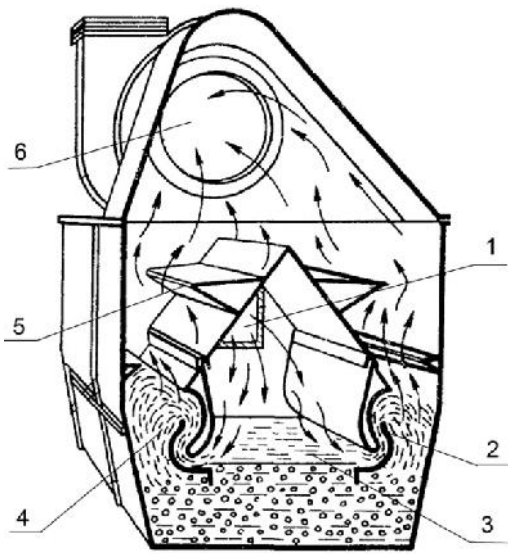
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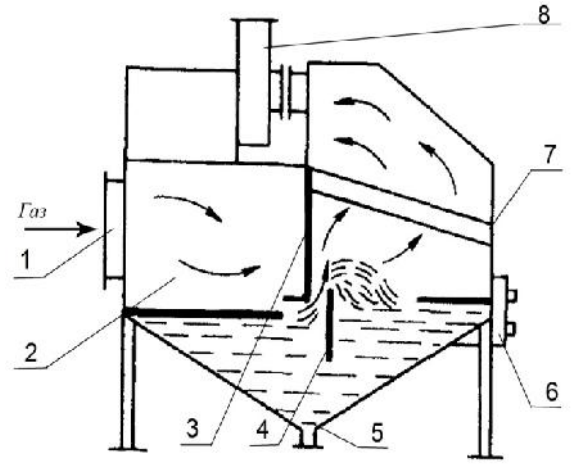
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[70,71]:
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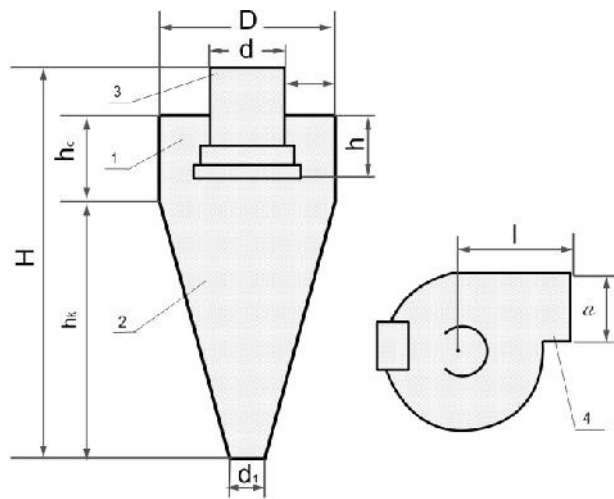
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[10, 12, 22].

[16, 19, 20]

[182].

[187]



1.13 – ; 2 – ; 3 – ;
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1.13 1.1

[60],

1.1 –

	b/D	0,05÷0,35
	d/D	0,15÷0,75
	h/b	1÷6
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	l/D	1,5÷5,5
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[47,51,102,114]

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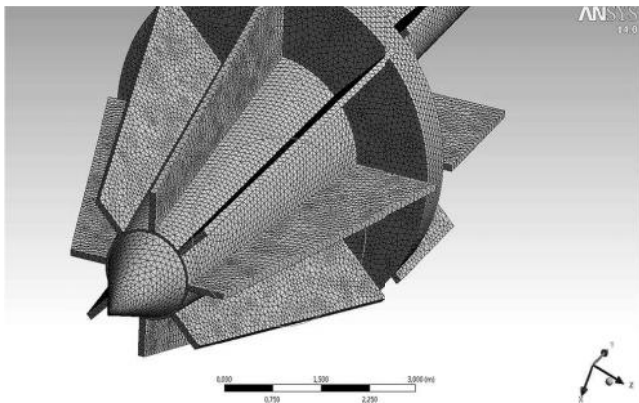
[127].

[106],

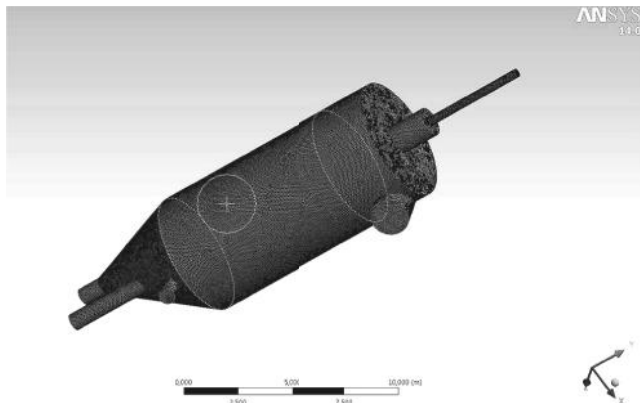
[145]

2.2

Ansys CFX



2.3 –



2.4 –

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Ansys CFX:

Ansys CFX

$$\mu = 1 \cdot 10^{-3}$$

$\rho = 72,5 \cdot 10^3 \text{ kg/m}^3$; $\mu = 0,0000189 \text{ Pa}\cdot\text{s}$; $\nu = 1,291 \cdot 10^{-6} \text{ m}^2/\text{s}$; $\gamma = 15,56 \cdot 10^6 \text{ J/m}^3$; $\beta = 2600 \text{ 1/K}$; $d = 1 \div 100 \text{ m}$; $V = 5,1 \div 35 \cdot 10^{-6} \text{ m}^3$.

$U_{wall} = 0$,

$$\begin{cases} \mathbf{U}_{inlet} = u_{axial} \bar{i} + u_{radial} \bar{j} + u_{swirl} \bar{k} \\ u_{axial} = u_1; u_{radial} = 0; u_{swirl} = 0 \end{cases} \quad \begin{cases} \mathbf{U}_{inlet} = u_{axial} \bar{i} + u_{radial} \bar{j} + u_{swirl} \bar{k} \\ u_{axial} = u_2; u_{radial} = 0; u_{swirl} = 0 \end{cases} \quad (2.1)$$

(2.2)

(2.3)

$$\frac{1}{r} \left[\frac{\partial}{\partial r} (r \rho v_r v_r) + \frac{\partial}{\partial z} (r \rho v_r v_z) \right] = \frac{1}{r} \left[\frac{\partial}{\partial r} \left(r \mu_T \frac{\partial v_r}{\partial r} \right) + \frac{\partial}{\partial z} \left(r \mu_T \frac{\partial v_r}{\partial z} \right) \right] - \frac{\partial P}{\partial r} - \mu_T \frac{v_r}{r^2} + \frac{\rho v_\phi^2}{r} \quad (2.2)$$

$$\frac{1}{r} \left[\frac{\partial}{\partial r} (r \rho v_r v_\phi) + \frac{\partial}{\partial z} (r \rho v_z v_\phi) \right] = \frac{1}{r} \left[\frac{\partial}{\partial r} \left(r \mu_T \frac{\partial v_\phi}{\partial r} \right) + \frac{\partial}{\partial z} \left(r \mu_T \frac{\partial v_\phi}{\partial z} \right) \right] - \mu_T \frac{v_\phi}{r^2} - \frac{\rho v_\phi v_r}{r} \quad (2.2)$$

$$\frac{1}{r} \left[\frac{\partial}{\partial r} (r \rho v_r v_z) + \frac{\partial}{\partial z} (r \rho v_z v_z) \right] = \frac{1}{r} \left[\frac{\partial}{\partial r} \left(r \mu_T \frac{\partial v_z}{\partial r} \right) + \frac{\partial}{\partial z} \left(r \mu_T \frac{\partial v_z}{\partial z} \right) \right] - \frac{\partial P}{\partial z} \quad (2.3)$$

$$div \rho \bar{v} = 0, \quad (2.3)$$

$\mu = \mu_0 \left(1 - \beta (T - T_0) \right)$;

$$\mu = C_{\mu} \cdot \rho \cdot \frac{k^2}{\varepsilon}, \tag{2.4}$$

k

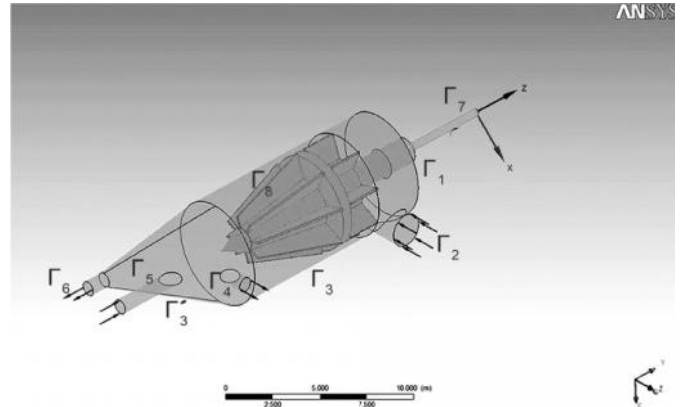
Ansys CFX

Ansys CFX,

(2.2) (2.3)

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2.5 –

1, 3, 4, 5 (2.5).

1 – 8, 3 – 4

0; $\frac{\partial \psi}{\partial r} = \max.$

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$$v_z = v_\phi = v_r = 0$$

4 6

$f(r)$

$$v_z = v_z(r), \quad \frac{\partial v_\phi}{\partial \lambda} = 0, \quad \int_0^{\psi_{\max}} d\psi = \int_0^D \rho r v_\phi(r) dr \quad (2.5)$$

3

$$\Psi_{i,\ell+1} = \Psi_{i,\ell} + \frac{\partial \Psi}{\partial r} \Big|_p \Delta r + \frac{1}{2} \frac{\partial^2 \Psi}{\partial r^2} \Big|_p \Delta r^2 + \frac{1}{6} \frac{\partial^3 \Psi}{\partial r^3} \Big|_p \Delta r^3 + O(\Delta r^4) \quad (2.6)$$

$$(\partial \Psi / \partial r^p) \Big|_p = 0, \quad \omega_{i,\ell} = -\frac{\partial v_z}{\partial r}, \quad v_z = v_r = 0$$

$$\frac{\partial^2 \Psi}{\partial r^2} \Big|_p = \rho r \left(\frac{\partial v_z}{\partial r} + v_z \right) \Big|_p = \rho r \frac{\partial v_z}{\partial r} \Big|_p$$

$$d/dr, d^2/dr^2 \quad (2.13)$$

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ij,

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$$ij = 0,$$

$$\omega = -\frac{2}{\rho r} \frac{\Psi_{i,\ell+1}}{\Delta r^2} + O(\Delta r)$$

(2.7)

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$$\omega = -\frac{2(\Psi_{+1} - \Psi)}{\rho r \Delta n^2} + O(\Delta n)$$

(2.8)

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$$\frac{\partial \omega}{\partial r} \Big|_p = \frac{\partial^2 v_r}{\partial z \partial r} - \frac{\partial^2 v_z}{\partial r^2} = \frac{\partial}{\partial z} \frac{\partial v_r}{\partial r} - \frac{1}{\rho} \left[\frac{1}{r} \frac{\partial^3 \Psi}{\partial r^3} - \frac{1}{r^2} \frac{\partial^2 \Psi}{\partial r^2} + \frac{1}{r^3} \frac{\partial \Psi}{\partial r} \right]$$

$$\frac{\partial v_r}{\partial r} = -\frac{\partial v_z}{\partial z} - \frac{v_r}{r}; v_r = 0 \Rightarrow \frac{\partial v_r}{\partial r} = -\frac{\partial v_z}{\partial z} \quad r, \quad ,$$

$$\frac{\partial \omega}{\partial r} \Big|_p = -\frac{\partial^2 v_z}{\partial z^2} \Big|_p - \frac{1}{\rho r} \frac{\partial^3 \Psi}{\partial r^3} \Big|_p, \quad \frac{\partial^2 v_z}{\partial z^2} = 0$$

.

,

$$\frac{\partial \omega}{\partial r} \Big|_p = -\frac{1}{\rho r} \frac{\partial^3 \Psi}{\partial r^3} \Big|_p = -\rho r \frac{\omega_{\ell+1} - \omega_\ell}{\Delta r}$$

$$\left. \frac{\partial \Psi}{\partial r} \right|_p, \left. \frac{\partial^2 \Psi}{\partial r^2} \right|_p, \left. \frac{\partial^3 \Psi}{\partial r^3} \right|_p \quad (2.13)$$

$$\Psi_{i,\ell+1} = \Psi_{i,\ell} + \frac{1}{2}(-\rho r \omega_{i,\ell}) \Delta r^2 + \frac{1}{6}(-\rho r \frac{\omega_{i,\ell+1} - \omega_{i,\ell}}{\Delta r}) \Delta r^3$$

, n = r, i, j

$$\omega = - \left[\frac{3(\Psi_{+1} - \Psi)}{r \rho \Delta r^2} + \frac{\omega_{+1}}{2} \right] \quad (2.9)$$

, r , d/dr = 0

$$\frac{\Psi_{i,\ell+1} - \Psi_{i,\ell}}{\Delta r^2 \rho} = \frac{1}{2}(-r \omega_{i,\ell}) + \frac{1}{6} \left(-r \frac{\omega_{i,\ell+1} - \omega_{i,\ell}}{\Delta r} \right) \Delta r +$$

$$+ \frac{1}{6}(-2\omega_{i,\ell}) \Delta r + \frac{\Delta r^2}{24} \left(-r \frac{\partial^2 \omega}{\partial r^2} \right) + \frac{\Delta r^2}{24} \left(-3 \frac{\omega_{i,\ell+1} - \omega_{i,\ell}}{\Delta r} \right)$$

$$\omega = \frac{\Psi - \Psi_{+1}}{\Delta r^2 \rho \left(\frac{r}{3} + \frac{5\Delta r}{24} \right)} - \frac{\frac{r}{6} + \frac{\Delta r}{8}}{\frac{r}{3} + \frac{5\Delta r}{24}} \omega_{r+1} \quad (2.10)$$

[101] (2.17)

$$\omega = q_1 + q_2 \omega_{+1} \quad (2.11)$$

7 . 7 r, = 0 ,

(d/dr) = 0.

(d/dr) = 0, = 0.

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$$Q = 2\pi r l \left| v_r \right| \quad (2.12)$$

$$\left| v_r \right| = \left| v_r \right|;$$

$$\psi = \psi_{\max} \cdot z/l, \quad (2.13)$$

$z -$

$; l -$

[101]

$=const,$

[78]

$d \nu_r / dz$

$$\omega = \frac{\partial v_r}{\partial z} = -\frac{I}{\rho r} \frac{\partial^2 \psi}{\partial z^2} = \frac{I}{\rho r} \frac{\psi_{-2} - 2\psi_{-1} + \psi}{\Delta z^2} \quad (2.14)$$

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$=0.$

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$$\frac{\partial \omega}{\partial z} = 0, \quad \frac{\partial \psi}{\partial z} = 0 \Rightarrow \psi = \psi_{-1}, \quad \omega = \omega_{-1} \quad (2.15)$$

$$\frac{\partial \omega}{\partial z} = \frac{\partial v_r}{\partial z} = 0, \quad \frac{\partial^2 \psi}{\partial z^2} = 0.$$

, z_r , ν_r , $\omega = 0.$

(2.15):

$$\omega = -\frac{2}{\rho r} \frac{\psi_a - \psi}{\Delta n^2},$$

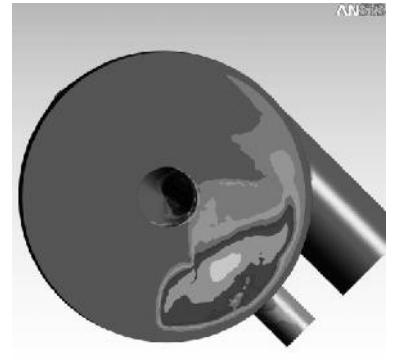
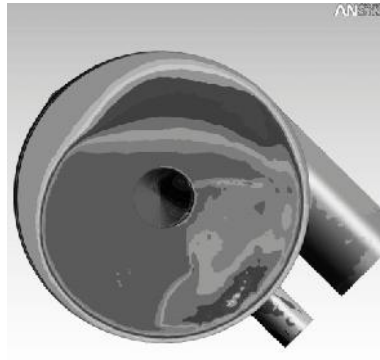
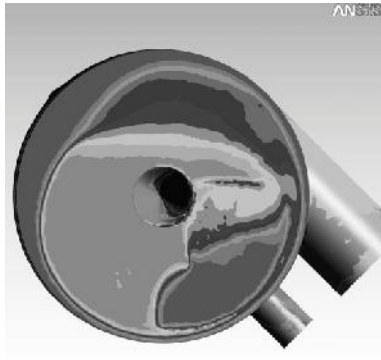
$$\Delta n^2 = (\Delta r \cos \beta)^2 = \frac{\Delta z^2}{1 + \gamma^2}; \quad \gamma = \frac{\Delta z}{\Delta r} \quad (2.16)$$

[81]

2.3

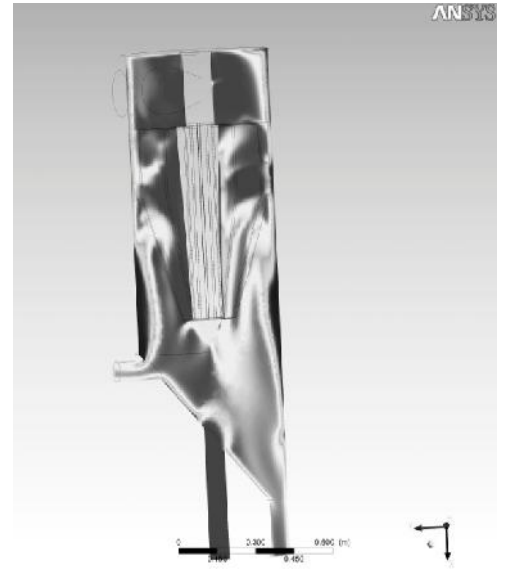
nsys FX

2.6-2.8.



3%,

(2.9).



2.9 -

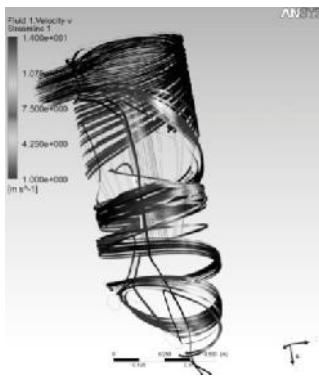
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8÷10%

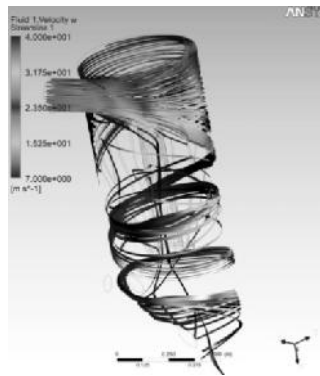
[74, 76].

[183].

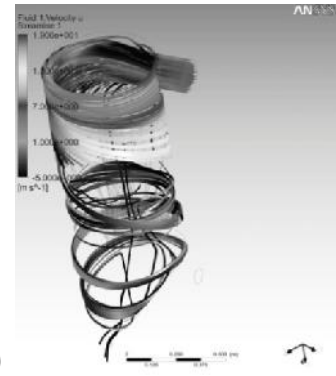
2.10,



2.10 –



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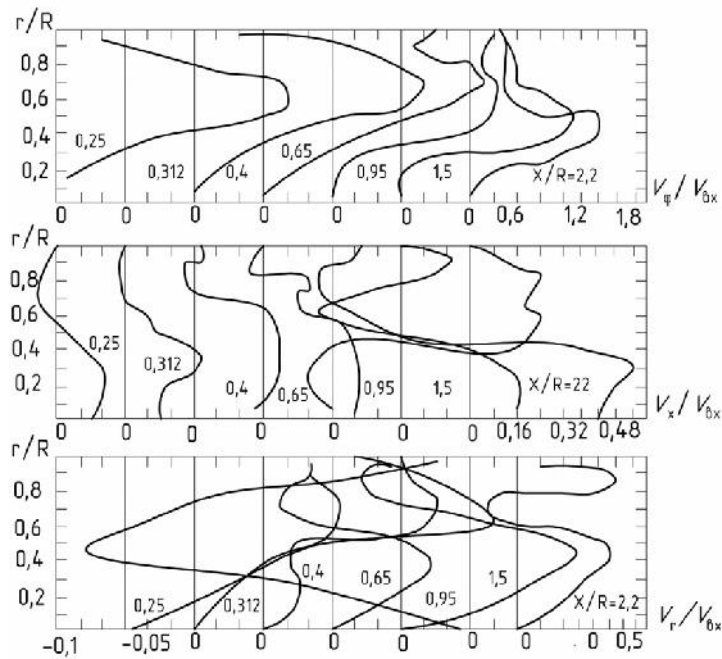


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2.10 , (2.10,)

, (2.10,)
 , , (2.10,).



2.11 –

$r/R = 0,25; 0,312; 0,4; 0,65; 0,95; 1,5; 2,2$

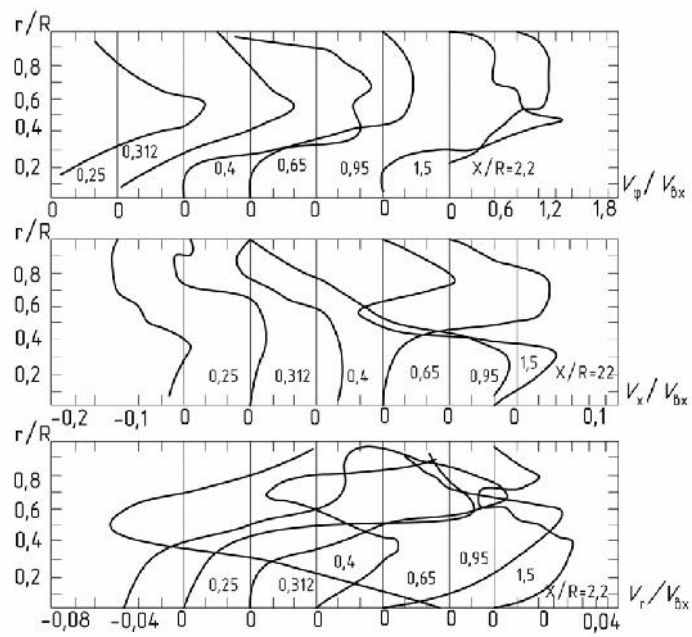
$V_r/V_{0x} = 0,05; V_\phi/V_{0x} = 1,8; Re = 3 \cdot 10^4$

[75, 134.

135, 189]

($r/R = 0,25; 0,312; 0,4; 0,65; 0,95$)
 (2.9).

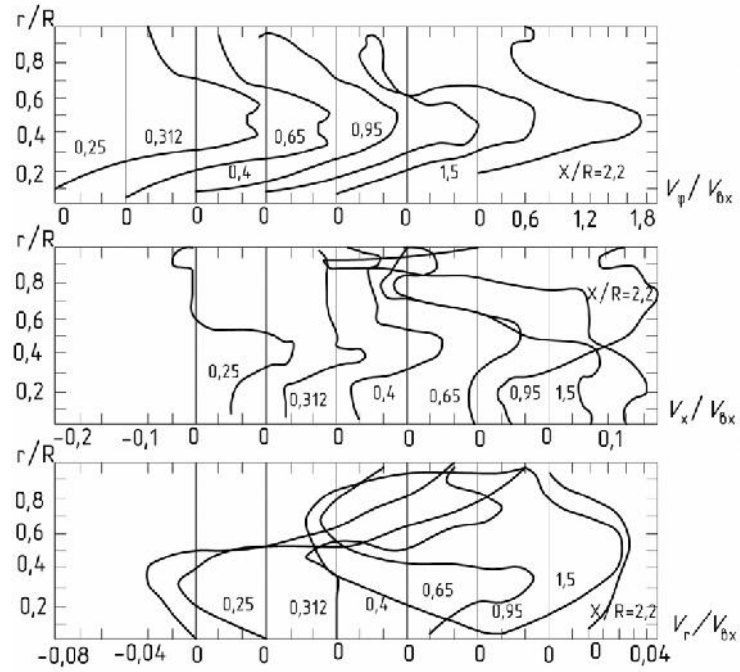
[48,75].



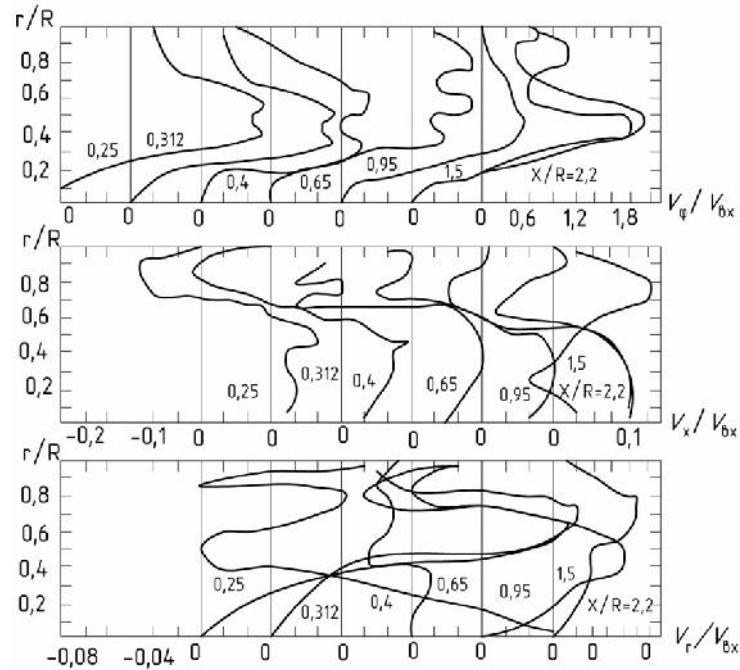
2.12 –

 $x/R = 0,25; 0,312; 0,4; 0,65; 0,95; 1,5; 2,2$
 $V_y/V_{bx} = 0,05; V_x/V_{bx} = 1,8; Re = 6 \cdot 10^4$

() ()

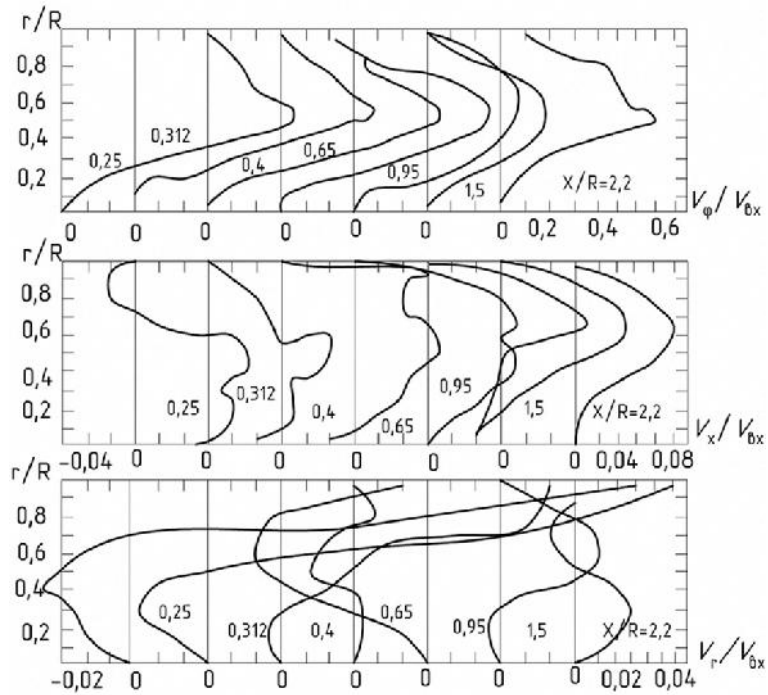


2.13 –

 $r/R = 0,25; 0,312; 0,4; 0,65; 0,95; 1,5; 2,2$
 $V/V = 0,05; V/V = 1,8; Re = 1 \cdot 10^4$


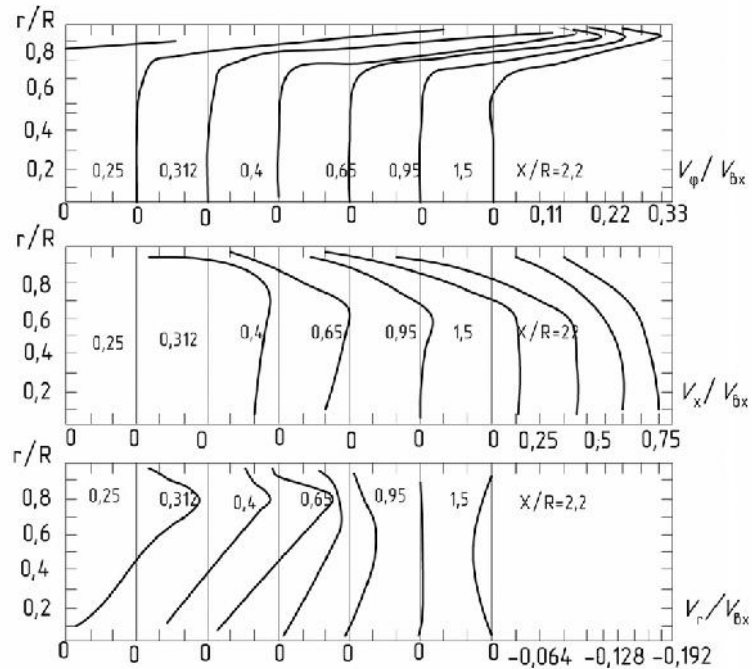
2.14 –

 $r/R = 0,25; 0,312; 0,4; 0,65; 0,95; 1,5; 2,2$
 $V/V = 0,01; V/V = 1,8; Re = 5 \cdot 10^4$



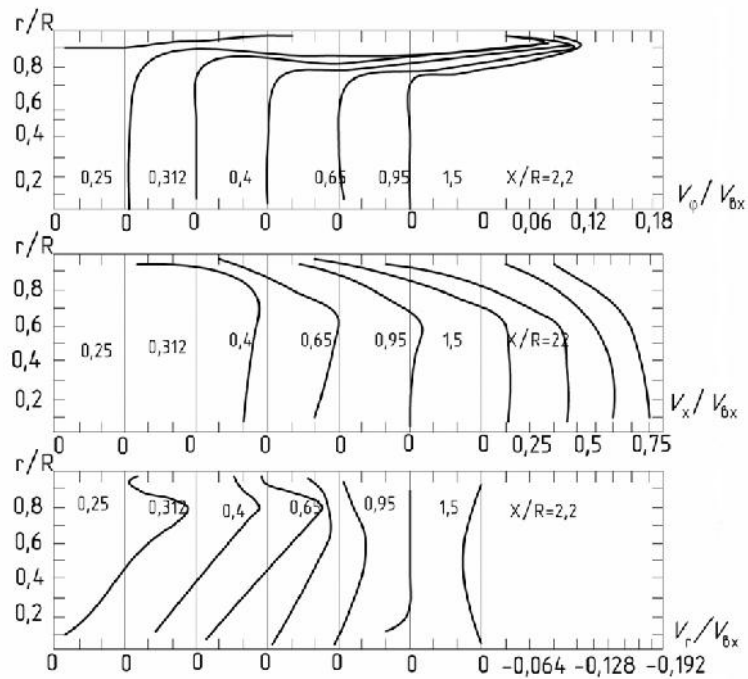
2.15 –

$r/R = 0,25; 0,312; 0,4; 0,65; 0,95; 1,5; 2,2$:
 $V^I / V^I = 0,04; V^I / V^I = 0,1; Re = 5 \cdot 10^3$



2.16 –

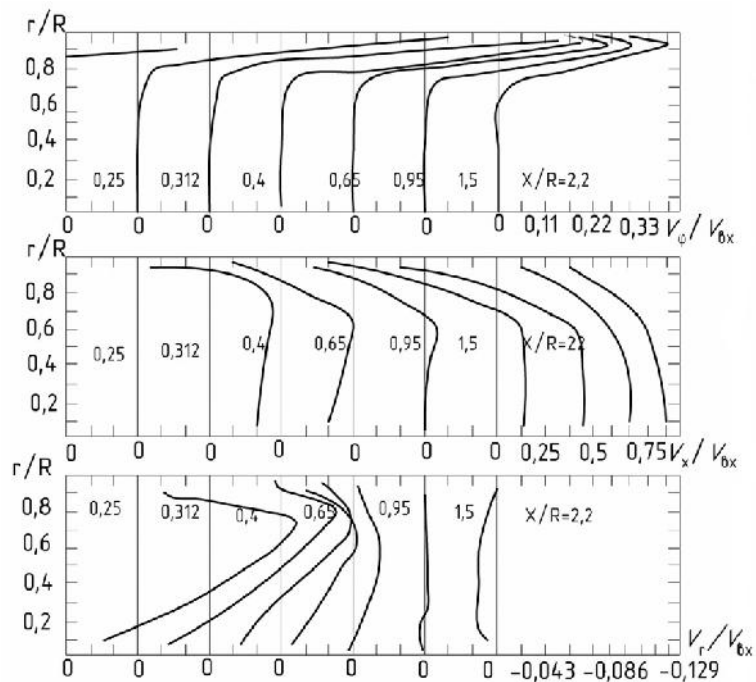
$r/R = 0,25; 0,312; 0,4; 0,65; 0,95; 1,5; 2,2$:
 $V^I / V^I = 0,05; V^I / V^I = 1,8; Re = 1 \cdot 10^4$



2.17 –

$r/R = 0,25; 0,312; 0,4; 0,65; 0,95; 1,5; 2,2$

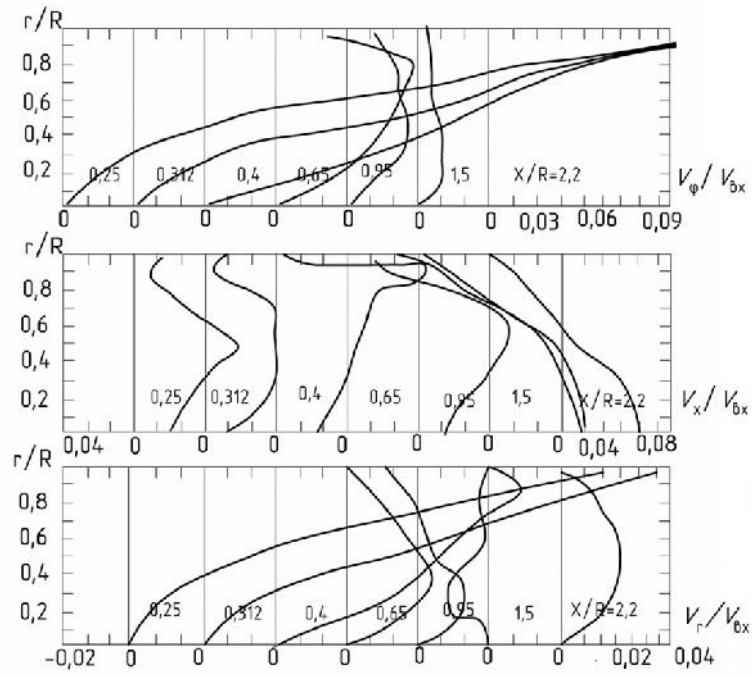
$V_{\theta} / V_{b\theta} = 0,05; V_x / V_{bx} = 1,8; Re = 2 \cdot 10^4$



2.18 –

$r/R = 0,25; 0,312; 0,4; 0,65; 0,95; 1,5; 2,2$

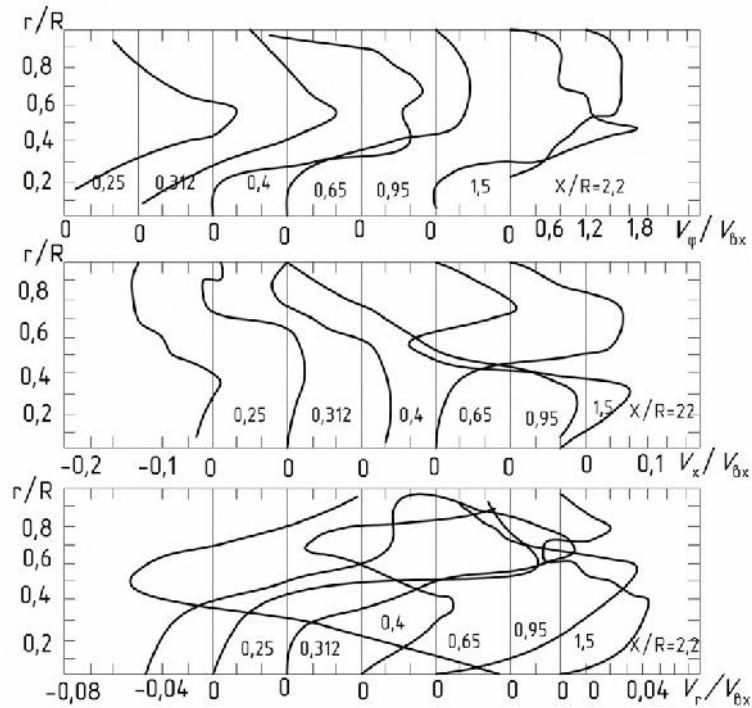
$V_{\theta} / V_{b\theta} = 0,05; V_x / V_{bx} = 1,8; Re = 3 \cdot 10^4$



2.19 –

$r/R = 0,25; 0,312; 0,4; 0,65; 0,95; 1,5; 2,2$

$V_\phi / V_{b\phi} = 0,05; V_x / V_{bx} = 1,8; Re = 1 \cdot 10^2$



2.20 –

$r/R = 0,25; 0,312; 0,4; 0,65; 0,95; 1,5; 2,2$

$V_\phi / V_{b\phi} = 0,04; V_x / V_{bx} = 0,6; Re = 5 \cdot 10^3$

$$Re=(1,5\div 6,0)\cdot 10^4.$$

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V

(2.2.15, 2.19),

(2.16-2.18).

V

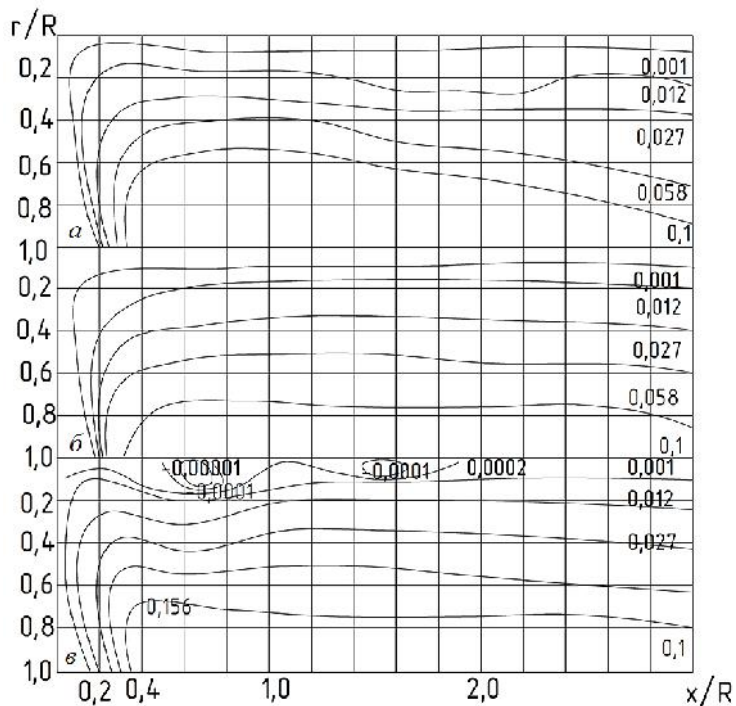
V

2.15-2.20)

(/R = 0,4-0,65

),

V

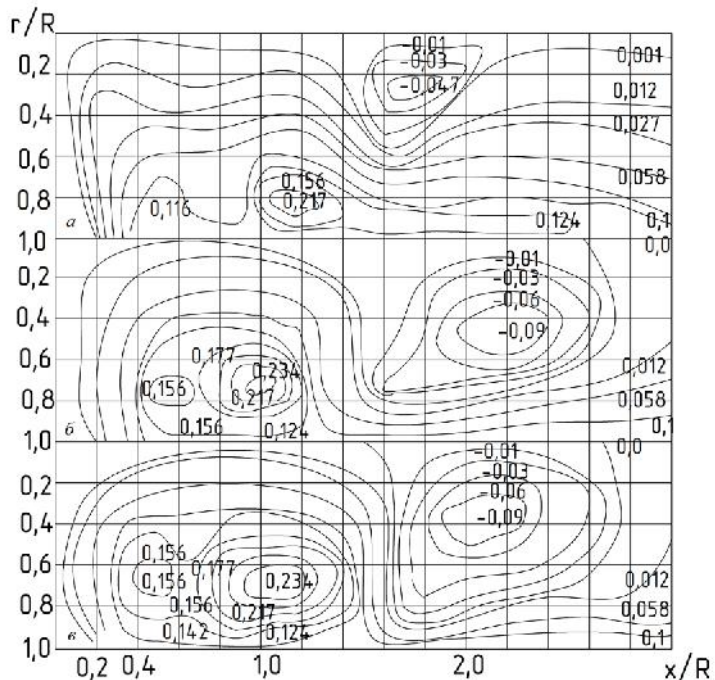


2.21 –

$$V / V = 0,01; V / V = 1,8.$$

:

$$-Re = 1 \cdot 10^1; \quad -Re = 1 \cdot 10^2; \quad -Re = 1 \cdot 10^3$$

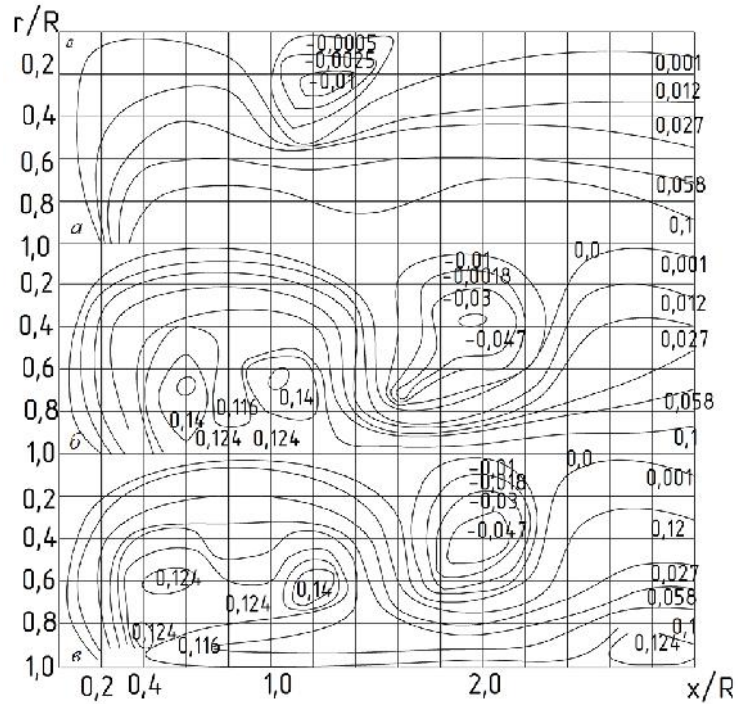


2.22 –

$$V / V = 0,01; V / V = 1,8.$$

:

$$-Re = 3 \cdot 10^3; \quad -Re = 4 \cdot 10^3; \quad -Re = 1 \cdot 10^4$$



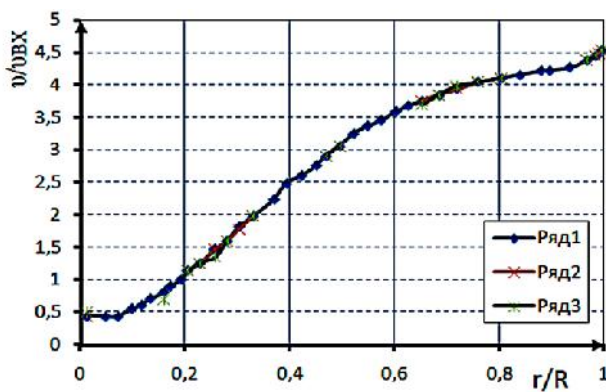
2.23 –

$V / V = 0,01; V / V = 1,8.$

:

$-Re = 5 \cdot 10^4; -Re = 6 \cdot 10^4; -Re = 7 \cdot 10^4$

Ansys CFX



2.24 –

$Re = 1000,$

2.24

[139],

[140],

[137].

1 – ; 2 – ; 3 –

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2.4

Zh u (1993) [149],
 . (1994) [25], G rbis & Sp k yny (1995) [109], Cr w . (1998) [200],
 (2003) [40] t n & F ssler (1994), lgh b shi (1994) [23–25],
 McL ughlin (1994) [37–40], Cr w . (1996) [21], Sim nin (1996) [41, 42],
 (1996), L th (2000), S mm rfeld (2000) [43–46], M sh y k
 & P ndy (2003) [34–36].

DNS L S

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[47, 48].

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[11].

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[44]

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3.

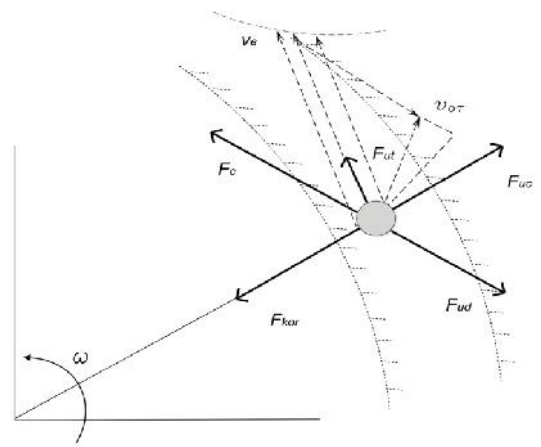
4.

5.

[54].

$$Nu = 2.$$

(2.26).



2.26 -

(2.27). $OXYZ, OZ,$

$OXYZ$

$$m \frac{d\vec{v}}{dt} = \vec{F}_{st} \quad (2.17)$$

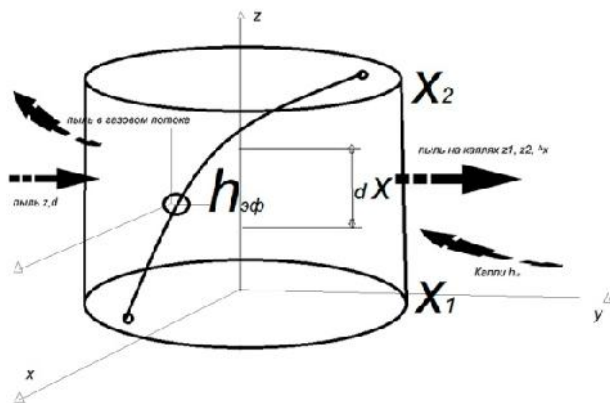
m – ;
 d – ;
 F_{st} –

()

(2.17)

(r ; ; z).

U – , V – W –



2.27 –

$O'X'Y'Z',$
 $O'Z'$

OZ

W

$$\omega(t) = \frac{U}{r} \quad (2.18)$$

$O'X'Y'Z'$

$$m = \frac{1}{6} \pi \rho d^3$$

$$m \frac{d\vec{v}}{dt} = \vec{F}_{Cm} - m\vec{a}_0 + m[\vec{r}' \times \vec{\omega}] + m[\vec{\omega} \times [\vec{r}' \times \vec{\omega}]] + 2m[\vec{v}' \times \vec{\omega}]$$

$$\frac{d\vec{v}}{dt} = \frac{1}{m} \vec{F}_{Cm} - \vec{a}_0 + [\vec{r}' \times \vec{\omega}] + [\vec{\omega} \times [\vec{r}' \times \vec{\omega}]] + 2[\vec{v}' \times \vec{\omega}] \quad (2.19)$$

$$\vec{\alpha}_0 -$$

$$d\vec{v} -$$

$$[\vec{r}' \times \vec{\omega}] -$$

$$[\vec{\omega} \times [\vec{r}' \times \vec{\omega}]] -$$

$$2[\vec{v}' \times \vec{\omega}] -$$

$$F = 3\pi\mu d [\vec{v}' - \vec{v}] \quad (2.20)$$

$$\vec{\mu} -$$

$$(2.19)$$

$$\frac{dW}{dt} e_z = \frac{dW}{dt} e_z,$$

$$[\vec{r}' \times \vec{\omega}] = [\vec{r}' \times \frac{d\vec{\omega}}{dt}] = [\vec{r}' \times \frac{d}{dt} (\frac{U}{r} e_z)] = -r \left(\frac{1}{r} \frac{dU}{dt} - \frac{U}{r^2} V_x \right) e_y = \left(-\frac{dU}{dt} + \frac{UV}{r} \right) e_y$$

$$[\vec{\omega} \times [\vec{r}' \times \vec{\omega}]] = \frac{U^2}{r_x} [e_z \times [e_x \times e_z]] = -\frac{U^2}{r} [e_z \times e_y] = \frac{U^2}{r} e_x$$

$$2[\vec{v}' \times \vec{\omega}] = 2v_x [e_x \times \vec{\omega}] = 2v_x \frac{U_x}{r} [e_x \times e_z] = \left(-2 \frac{UV}{r} \right) e_y$$

$$\vec{e}_x, \vec{e}_y, \vec{e}_z -$$

$$, \quad \vec{r} = \vec{e}_x \cdot r, v_x = v$$

:

$$m \frac{d\vec{v}}{dt} = \vec{F}_{Cm} - m\vec{a}_0 + m[\vec{r} \times \vec{\omega}] + m[\vec{\omega} \times [\vec{r} \times \vec{\omega}]] + 2m[\vec{v} \times \vec{\omega}]$$

$$\frac{d\vec{v}}{dt} = \frac{1}{m} \vec{F}_{Cm} - \vec{a}_0 - \frac{dU}{dt} \vec{e}_y - \frac{U}{r} V \vec{e}_y + \frac{U^2}{r} \vec{e}_x$$

 $O'X'Y'Z'$,

:

$$\begin{cases} \frac{dV_{x'}}{dt} = \frac{1}{m} F_{Cm\ x'} + \frac{U^2}{r} \\ 0 = \frac{1}{m} F_{Cm\ y} - \frac{dU}{dt} - \frac{U}{r} V \\ 0 = \frac{1}{m} F_{Cm\ z} - \frac{dW}{dt} \end{cases}$$

$$\begin{cases} \frac{dV}{dt} = \frac{1}{m} F_{Cm\ x} + \frac{U^2}{r} \\ \frac{dU}{dt} = \frac{1}{m} F_{Cm\ y} - \frac{U}{r} V \\ \frac{dW}{dt} = \frac{1}{m} F_{Cm\ z} \end{cases} \quad (2.21)$$

(2.18)

(2.20)

(2.21),

:

$$\begin{cases} \frac{dU_z}{d\tau} = \frac{3}{4} \cdot \frac{\rho}{\rho} \cdot \frac{\xi}{d} \cdot U \cdot (V_z - U_z) + g; U_z = \frac{dx}{d\tau} \\ \frac{dU_\phi}{d\tau} = \frac{3}{4} \cdot \frac{\rho}{\rho} \cdot \frac{\xi}{d} \cdot U \cdot (V_\phi - U_\phi) + \frac{\omega \cdot r}{\tau}; U_\phi = \omega \cdot r = r \frac{d\phi}{d\tau} \\ \frac{dU_r}{d\tau} = \frac{3}{4} \cdot \frac{\rho}{\rho} \cdot \frac{\xi}{d} \cdot U \cdot (V_r - U_r) - \frac{\omega \cdot r}{\tau} + \omega^2 r; U_r = \frac{dr}{d\tau} \end{cases} \quad (2.22)$$

:

$$\left\{ \begin{array}{l} \frac{d W_z}{d \tau} = \frac{3}{4} \cdot \frac{\rho}{\rho} \cdot \frac{\xi}{d} \cdot W \cdot (V_z - W_z) + g; W_z = \frac{dx}{d \tau} \\ \frac{d W_\varphi}{d \tau} = \frac{3}{4} \cdot \frac{\rho}{\rho} \cdot \frac{\xi}{d} \cdot W \cdot (V_\varphi - W_\varphi) + \frac{\omega \cdot r}{\tau}; W_\varphi = \omega \cdot r = r \frac{d\varphi}{d \tau} \\ \frac{d W_r}{d \tau} = \frac{3}{4} \cdot \frac{\rho}{\rho} \cdot \frac{\xi}{d} \cdot W \cdot (V_r - W_r) - \frac{\omega \cdot r}{\tau} + \omega^2 r; W_r = \frac{dr}{d \tau} \end{array} \right. \quad (2.23)$$

() ; $r -$ () ; $\mu -$ () ; $U -$

[192].

$$\begin{cases} \frac{dU}{dt} = \frac{18\mu}{\rho d^2} \left(\frac{R_0}{r} U_{\tau 0} - U \right) - \frac{U V}{r} + g \\ \frac{dV}{dt} = \frac{18\mu}{\rho d^2} \left(\frac{Q_0}{R_0^2} \cdot V, \left(\frac{\alpha}{R_z}; \frac{z}{R_z}; \frac{r}{R_z}; \frac{D}{R_z}; \dots \right) - V \right) + \frac{U^2}{r} + \frac{\omega r}{t} \\ \frac{dW}{dt} = \frac{18\mu}{\rho d^2} \left(\frac{Q_0}{R_0^2} \cdot W, \left(\frac{\alpha}{R_z}; \frac{z}{R_z}; \frac{r}{R_z}; \frac{D}{R_z}; \dots \right) - W \right) - \frac{\omega r}{t} + \omega^2 r; \end{cases} \quad (2.25)$$

:

$$\begin{aligned} \frac{R_z^2 \cdot U_z}{G_0} = \frac{R_z^2}{S}; U_z' = \frac{R_z^2}{G_0} \cdot U_z, U_\phi' = \frac{R_z^2}{G_0} \cdot U_\phi, U_r' = \frac{R_z^2}{G_0} \cdot U_r, t' = \frac{G_0}{R_z^3} \cdot t, z' = \frac{z}{R_z}, \phi' = \phi \\ U_z' = \frac{dr'}{dt'}, U_\phi' = \frac{dz'}{dt'}, U_r' = \frac{d\phi'}{dt'} \cdot r'. \end{aligned} \quad (2.26)$$

(2.25)

$$\begin{aligned} & , \quad = \frac{\mu R_z^3}{\rho G_0 d^2}, \\ & , \quad = \frac{R_z^2}{S} \end{aligned}$$

(2.25)

,

:

$$\begin{cases} \frac{dU}{dt} = 18 \left(\frac{U}{r} - U \right) - \frac{U V}{r} \\ \frac{dV}{dt} = 18 \left(U (\alpha; z; r; D \dots) - V \right) + \frac{U^2}{r} \\ \frac{dW}{dt} = 18 \left(U (\alpha; z; r; D \dots) - W \right) \end{cases} \quad (2.27)$$

:

$$r' \Big|_{t=0} = r'_0, z' \Big|_{t=0} = z'_0, \phi' \Big|_{t=0} = 0 -$$

$$U' \Big|_{t=0} = U'_0, U'_\phi \Big|_{t=0} = U'_0, U'_r \Big|_{t=0} = U'_0 -$$

(2.27)

$$U' (; z'; r'; D'; \dots)$$

$$W' (; z'; r'; D'; \dots), \dots$$

, . . .

$U' (; z'; r'; D'; \dots) = W' (; z'; r'; D'; \dots).$

, . . .

[86].

(2.28),

10⁵:

$$\begin{pmatrix} -18C - \frac{V}{r} & -\frac{U}{r} & 0 & -18\frac{C_p C}{r^2} - \frac{UV}{r^2} & 0 \\ \frac{2U}{r} & -18C_r & 0 & 18C_p \frac{dV}{dr} - \frac{U^2}{r^2} & 18C_p \frac{dV}{dz} \\ 0 & 0 & -18C & 18C_p \frac{dW}{dr} & 18C_p \frac{dW}{dz} \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \end{pmatrix} \quad (2.28)$$

(2.27)

n

x^{n+1} ,

x^n , $(n+1)$

(2.27),

((2.26)), :

$$\left\{ \begin{array}{l} \frac{U^{n+1} - U^n}{\Delta t} = 18C_p \left(\frac{C}{r^n} - U^{n+1} \right) - \frac{U^{n+1} V^n}{r^n} \\ \frac{V^{n+1} - V^n}{\Delta t} = 18C_p \left(V(r^n, z^n) - V^{n+1} \right) + \frac{(U^n)^2}{r^n} \\ \frac{W^{n+1} - W^n}{\Delta t} = 18C_p \left(W(r^n, z^n) - W^{n+1} \right) \\ \frac{r^{n+1} - r^n}{\Delta t} = V^{n+1} \\ \frac{z^{n+1} - z^n}{\Delta t} = W^{n+1} \\ \frac{\varphi^{n+1} - \varphi^n}{\Delta t} = \frac{U^{n+1}}{r^n} \end{array} \right. \quad (2.29)$$

(2.27)

:

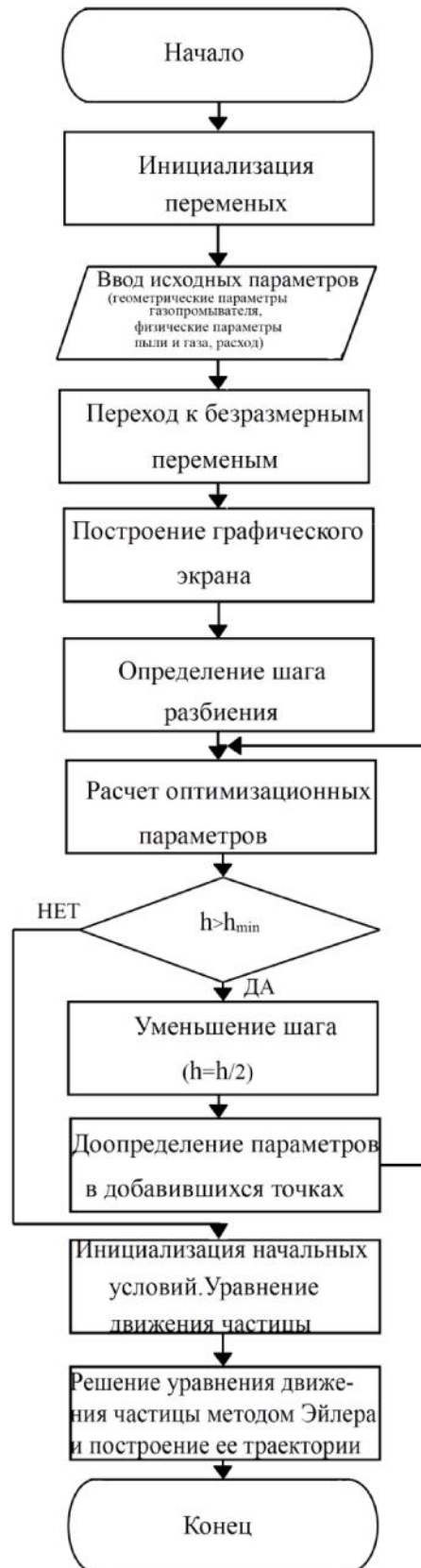
$$\left\{ \begin{array}{l} U^{n+1} = (U^n + 18C_p \Delta t^n / r^n) / (1 + (18C_p + V^n / r^n) \Delta t^n) \\ V^n = (V^n + (18C_p V(r^n, z^n) + (U^n)^2 / r^n) \Delta t^n) / (1 + 18C_p \Delta t^n) \\ W^n = (W^n + 18C_p W(r^n, z^n) \Delta t^n) / (1 + 18C_p \Delta t^n) \\ r^{n+1} = r^n + V^{n+1} \Delta t^n \\ z^{n+1} = z^n + W^{n+1} \Delta t^n \\ \varphi^{n+1} = \varphi^n + U^{n+1} \Delta t^n / r^{n+1} \\ \Delta t^{n+1} = C / \sqrt{(V^n)^2 + (W^n)^2} \end{array} \right. \quad (2.30)$$

2.28-2.29

2.28,

$$\varepsilon_r = \left| \frac{r}{(1/N)} \right| \frac{1}{Nr} + \left| \frac{r}{h} \right| \frac{h}{r} + \left| \frac{r}{\Delta t} \right| \frac{\Delta t}{r}. \tag{2.31}$$

,	0,5	1,0	2,0	3,0	5,0	10
$\Delta t / \tau = 1/(4 \dots)$	1/2	1/4	1/8	1/12	1/20	1/40
ε	0,26	0,13	0,064	0,040	0,025	0,013



2 10
6,4 1,3%,

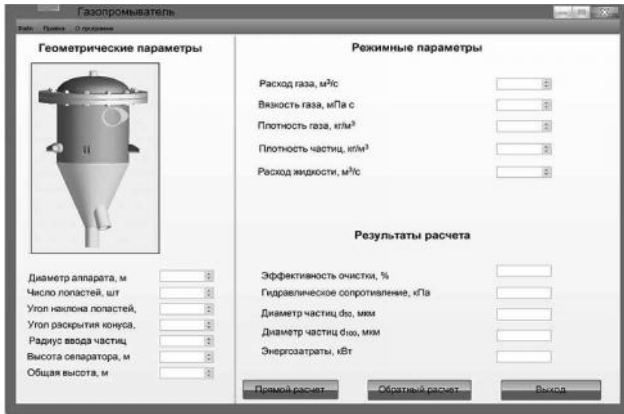
0,5 1,0
2,6%,

(= 2600 / ³)

1
 $\Delta t = 2 \cdot 10^{-6} c.$

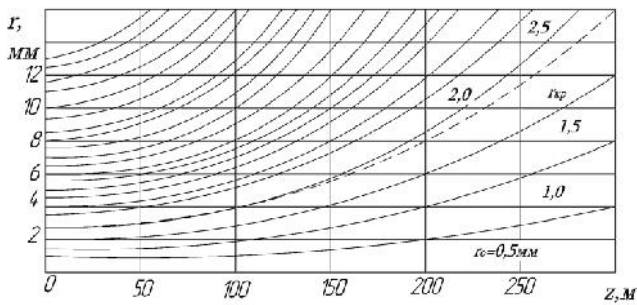
1)

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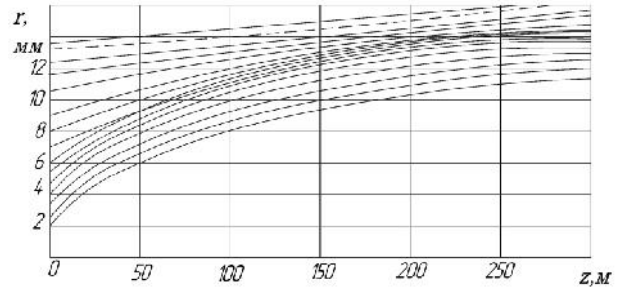
2.29 –

2.30-2.31



2.30 –

$d \ 5$:



2.31 –

$d \ 1$:

$r \ 5D$

r

$d \ 1$

2.5

(. . . U_x U_r),

p .

(2.32, 2.33),

p ,

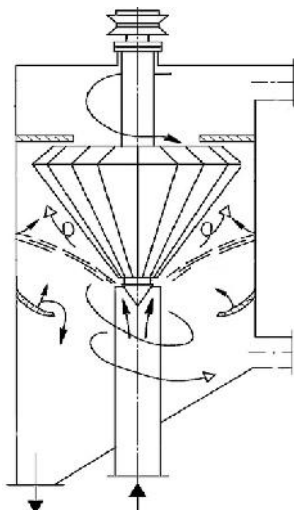
p

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p p « »

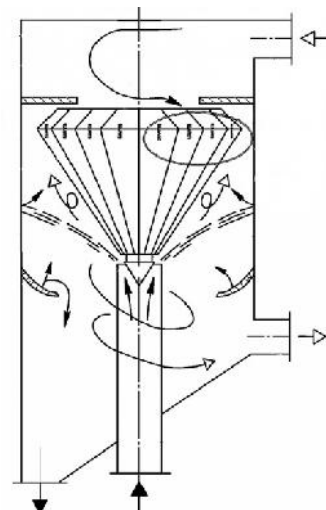
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2.32 -

2339435

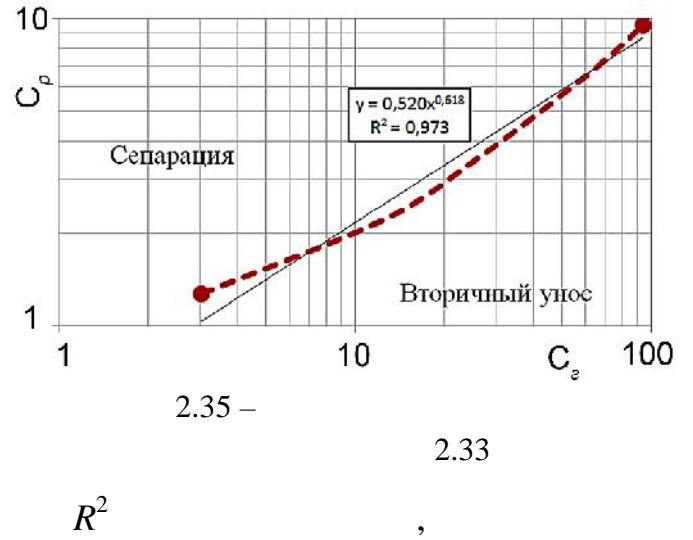
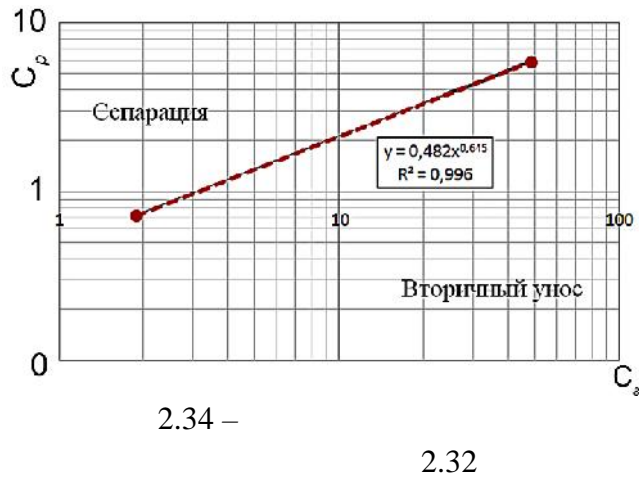


2.33 -

2516658

2.34, 2.35

p



$f()$.

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2.34, 2.35,
 $y=0,482x^{0,615}$ $y=0,520x^{0,618}$.

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0,6

$f()$

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100%.

$$\lambda = \sqrt{1 + \frac{U_\phi^2}{U_x^2}} \quad (2.36)$$

$$\eta_y = \frac{2}{1 - m^2} \int_m^1 t_1 (1 - e^{-\lambda T}) dt \quad (2.37)$$

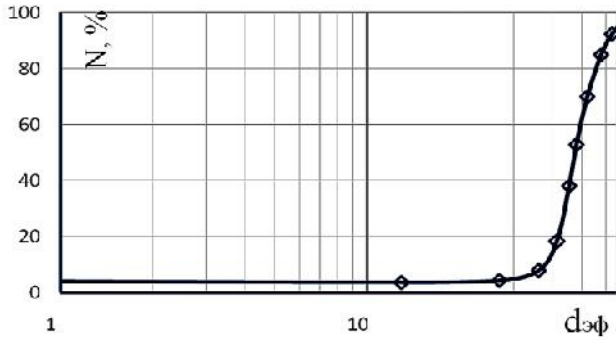
$$d \quad (2.25)$$

$$d$$

$$d = \sqrt{\frac{\mu R_z^3 G^{0.6}}{\rho G \phi R^{1.2} \vartheta^{0.6}}} \quad (2.38)$$

(2.37).

$$= (100 - N) / 100.$$



2.37 –

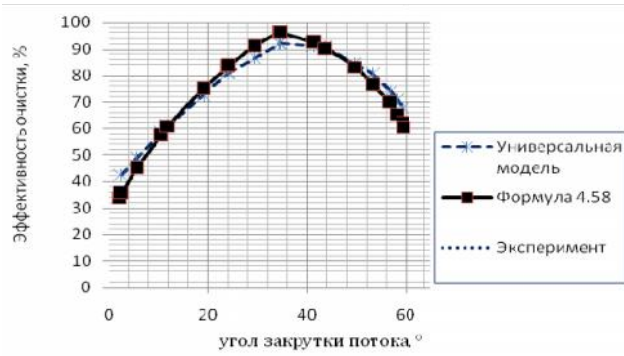
$d \ d$

$d \ d \ (N)$

:

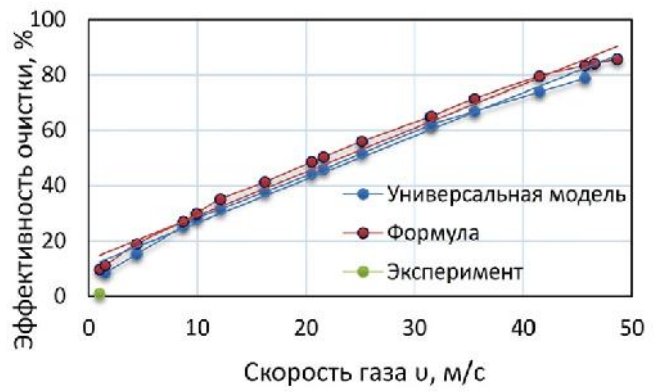
,
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(2.38, 2.39).



2.38 –

,
 ()



2.39 –

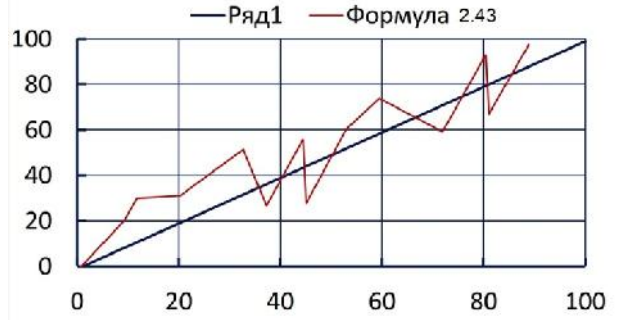
,
 ()

12%,

2.40, 2.41.



2.40 –



2.41 –

(2.43)

2.6

, ...

(y)

(z₁),

(z₂),

(z₃),

(z₄).

$$y = b_0 + b_1 z_1 + b_2 z_2 + b_3 z_3 + b_4 z_4 + b_{12} z_1 z_2 + b_{13} z_1 z_3 + b_{14} z_1 z_4 + b_{23} z_2 z_3 + b_{24} z_2 z_4 + b_{34} z_3 z_4 + b_{11} z_1^2 + b_{22} z_2^2 + b_{33} z_3^2 + b_{44} z_4^2. \quad (2.39)$$

[64]

(2.1).

(2.39)

2.42.

$$x_j = \frac{z_j - z_j^0}{\Delta z_j},$$

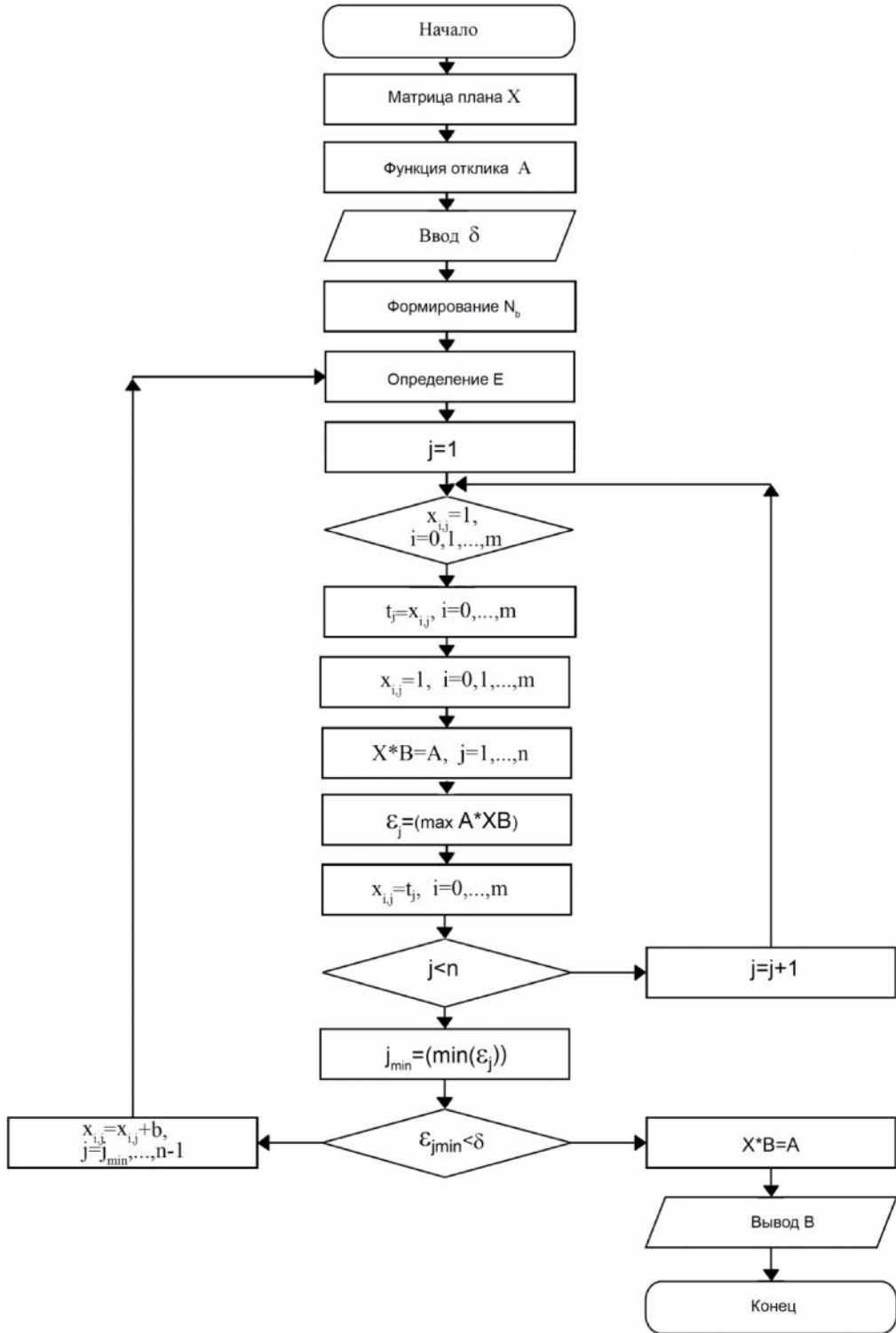
2.1 -

	z ₁ (/)	z ₂ (⁰)	z ₃ (^{3/} /)	z ₄ ()
, Z _j ⁰	30	40	5	3
, ΔZ _j	5	10	1	1,5 ÷ 2,0

z₁, z₂, z₃, z₄ –

1, 2, 3, 4.

$$Z_j^0 - , Z_j^0 = \frac{z_j^{\max} + z_j^{\min}}{2}; \Delta Z_j - , \Delta Z_j = \frac{z_j^{\max} - z_j^{\min}}{2}.$$



2.1

(2.2).

250.

$$f = 4 - 1 = 3$$

4

$(y_1^0 = 58, y_2^0 = 56, y_3^0 = 59, y_4^0 = 57)$:

$$\bar{y}^0 = \frac{\sum_{i=1}^4 y_i^0}{4} = 57,5; \quad S^2 = \frac{\sum_{i=1}^4 (y_i^0 - \bar{y}^0)^2}{3} = 1,67$$

:

$$b_j = \frac{\sum_{i=1}^N x_{ji} \cdot y_i}{\sum_{i=1}^N x_{ji}^2}; \quad S_{bj}^2 = \frac{S^2}{N}$$

t-

:

$$t_j = \frac{|b_j|}{S_{bj}}, \tag{2.40}$$

$b_j -$

;

$S_{bj} -$

$t -$

$$= 0,05$$

$$f = 3$$

$$t_p(f) = 2,56.$$

e:

$$\begin{aligned} y &= 48,53 + 9,34x_1 - 7,24x_2 - 3,04x_3 + 2,7(x_1 - 0,7) - 3,99(x_2 - 0,7) - \\ &\quad - 1,37(x_3 - 0,7) + 1,6(x_4 - 0,7) + 1,48x_5 = \\ &= 55,292 + 9,34x_1 - 7,24x_2 - 3,04x_3 + 2,7x_4 - 3,99x_5 - 1,37x_6 + 1,6x_7 + 1,5x_8. \end{aligned} \tag{2.41}$$

2.2 –

N	x_0	x_1	x_2	x_3	x_4	x_1^1	x_2^1	x_3^1	x_4^1	$1\ 2$	$1\ 3$	$1\ 4$	$2\ 3$	$2\ 4$	$3\ 4$	Y
1	+1	+1	+1	+1	+1	0,2	0,2	0,2	0,2	+1	+1	+1	+1	+1	+1	53
2	+1	-1	-1	+1	+1	0,2	0,2	0,2	0,2	+1	-1	-1	-1	-1	+1	47
3	+1	+1	-1	-1	+1	0,2	0,2	0,2	0,2	-1	-1	+1	+1	-1	-1	73
4	+1	-1	+1	-1	+1	0,2	0,2	0,2	0,2	-1	+1	-1	-1	+1	-1	43
5	+1	+1	-1	+1	-1	0,2	0,2	0,2	0,2	-1	+1	-1	+1	+1	-1	64
6	+1	-1	+1	+1	-1	0,2	0,2	0,2	0,2	-1	-1	+1	-1	-1	-1	38
7	+1	+1	+1	-1	-1	0,2	0,2	0,2	0,2	+1	-1	-1	+1	-1	+1	54
8	+1	-1	-1	-1	-1	0,2	0,2	0,2	0,2	+1	+1	+1	-1	+1	+1	56
9	+1	+1	-1	+1	+1	0,2	0,2	0,2	0,2	-1	+1	+1	+1	-1	+1	66
10	+1	-1	+1	+1	+1	0,2	0,2	0,2	0,2	-1	-1	-1	-1	+1	+1	39
11	+1	+1	+1	-1	+1	0,2	0,2	0,2	0,2	+1	-1	+1	+1	+1	-1	55
12	+1	-1	-1	-1	+1	0,2	0,2	0,2	0,2	+1	+1	-1	+1	-1	-1	58
13	+1	+1	+1	+1	-1	0,2	0,2	0,2	0,2	+1	+1	-1	+1	-1	-1	52
14	+1	-1	-1	+1	-1	0,2	0,2	0,2	0,2	+1	-1	+1	-1	+1	-1	46
15	+1	+1	-1	-1	-1	0,2	0,2	0,2	0,2	-1	-1	-1	+1	+1	+1	72
16	+1	-1	+1	-1	-1	0,2	0,2	0,2	0,2	-1	+1	+1	-1	-1	+1	42
17	+1	0	0	0	0	-0,8	-0,8	-0,8	-0,8	0	0	0	0	0	0	58
18	+1	+1,414	0	0	0	1,2	-0,8	-0,8	-0,8	0	0	0	0	0	0	69
19	+1	-1,414	0	0	0	1,2	-0,8	-0,8	-0,8	0	0	0	0	0	0	50
20	+1	0	+1,414	0	0	-0,8	1,2	-0,8	-0,8	0	0	0	0	0	0	40
21	+1	0	-1,414	0	0	-0,8	1,2	-0,8	-0,8	0	0	0	0	0	0	52
22	+1	0	0	+1,414	0	-0,8	-0,8	1,2	-0,8	0	0	0	0	0	0	50
23	+1	0	0	-1,414	0	-0,8	-0,8	1,2	-0,8	0	0	0	0	0	0	55
24	+1	0	0	0	+1,414	-0,8	-0,8	-0,8	1,2	0	0	0	0	0	0	60
25	+1	0	0	0	-1,414	-0,8	-0,8	-0,8	1,2	0	0	0	0	0	0	57

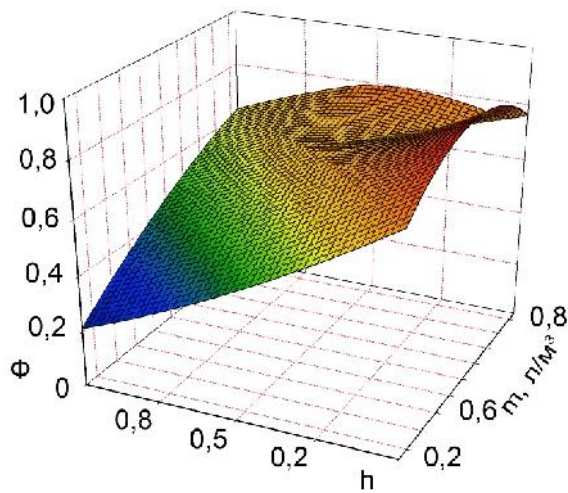
(2.41) :

$$y = 67,28 - 19,23z_1 + 2,85z_2 + 6,87z_3 - 1631z_4 + 0,492z_1^2 - 0,038z_2^2 - 2,15z_3^2 + 49200z_4^2 + 0,31z_2z_3. \tag{2.42}$$

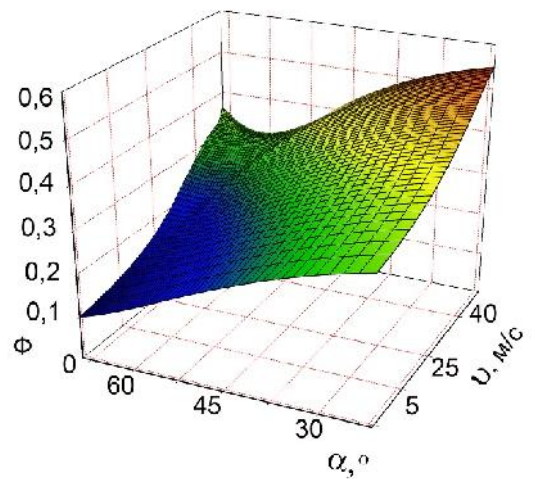
F - a :

$$S^2 = \frac{\sum_{i=1}^N (y_i - \bar{y}_i)^2}{N - 1} = \frac{121,3}{25 - 9} = 7,58$$

$$F = \frac{S^2}{S^2} = \frac{7,58}{1,67} = 4,54$$



2.43 -



2.44 -

= 0,05

, 8,95
 $f_1 = 15 \quad f_2 = 3,$
 $(F < F_p(f_1, f_2)).$ (2.42)

2

1.

CFX,

Ansys

U' , (r, z) , U' , U'_r

2.

$$Re = (1,5 \div 6,0) \cdot 10^4.$$

3.

‘ ’ “ ” , :
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4. , .
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5. .
: 1,2...2,6 % .

3

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[81]

[75, 134, 135]

(2.8).

3.1

[14].

(0,25 3.1).

0 25 / .

20 ,

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— $= 1 \div 20 / ;$

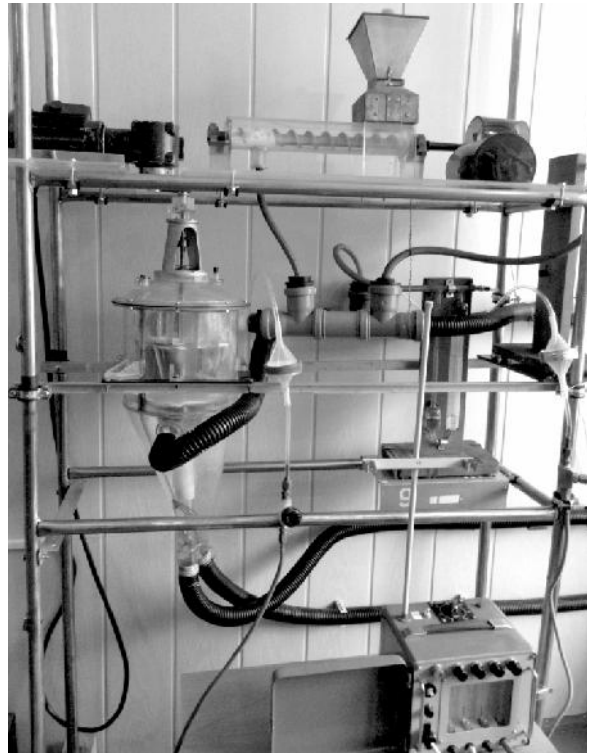
— $= 0 \div 100^{-1};$

— $\dot{\alpha} < 90^\circ$

— $\dot{\alpha} > 90, \quad \dot{\alpha} -$

— ;

— $= 0 \div 65^\circ$



3.1 –

— .

5 35 / .

$$L/G = (0 \div 1,6).$$

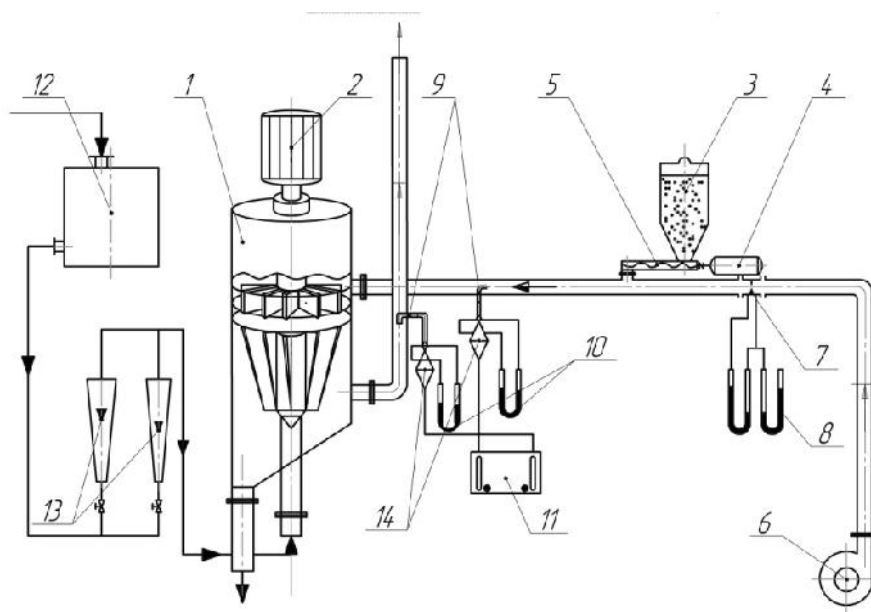
(); (/),

($^3 / ^3$); ($^3 /$),

(/).

[60].

$L/G = 0,1;$



- 3.2 - ;
- 1 - ; 2 - ; 3 - ; 4 - ;
- 5 - ; 6 - ; 7 - ;
- 8,10 - ; 9 - ; 11 - ;
- 12 - ; 13 - ; 14 - ;

$L/G = 0,3...1,6.$

,
 .
 , ,
 .
 , (3.2).
 .
 -1,
 - 9,
 - 14

.
 - 11.
 -55,
 -10
 .
 8
 .
 ΔG_1 : ΔG_2
 $= (G_1 - G_2) / G_1$
 $Q (\text{ }^3/)$
 , / $S, \text{ }^2$:
 $Q = \cdot S,$
 , U-
 , :

$$v = \sqrt{\frac{2H}{\rho}},$$

, / ³.

ρ –

1)

2)

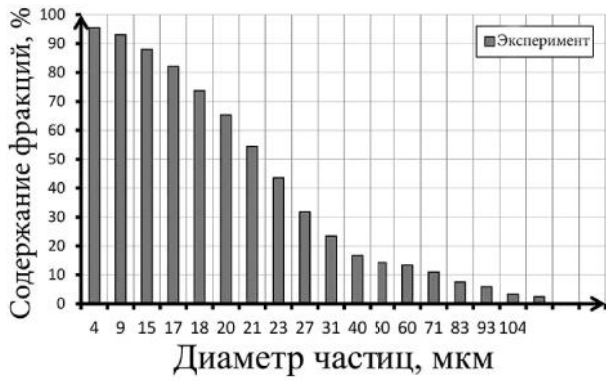
[59]

2,10

36,8°.

924

1245 / ³,



3.3 –

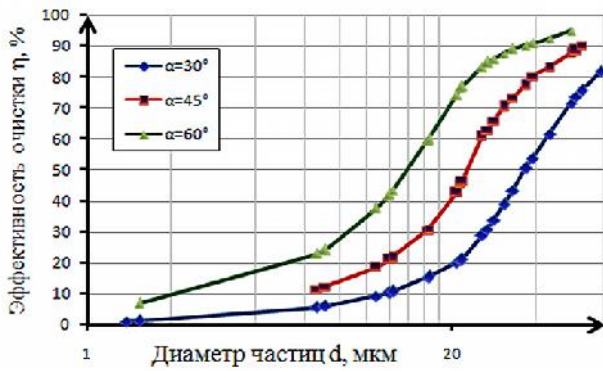
70%
10

3.3)

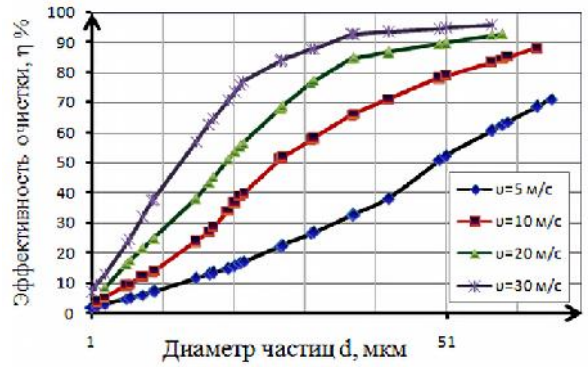
100

3.4

3.5



3.4 –



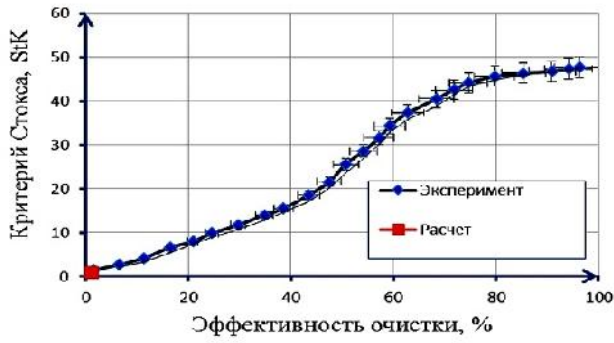
3.5 –

(3.5),

20 30

/ .

(3.6).

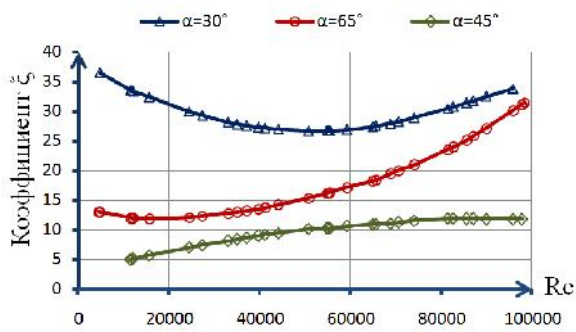


3.6 –

3.2

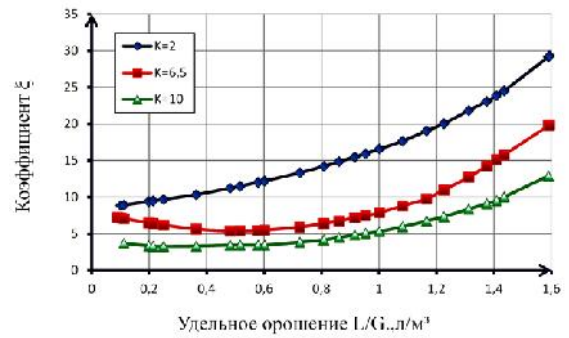
(3.7,)

$= (L/G)$



3.7 –

5:7 / .



:

;

$$L/G = 0,1 \div 1,5.$$

5 20 /

L/G

L/G

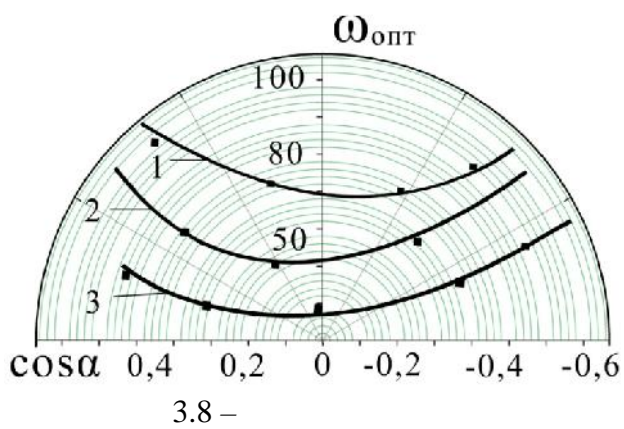
$$L/G = 0,4 \div 0,6,$$

$$L/G = 0,6 \div 0,8$$

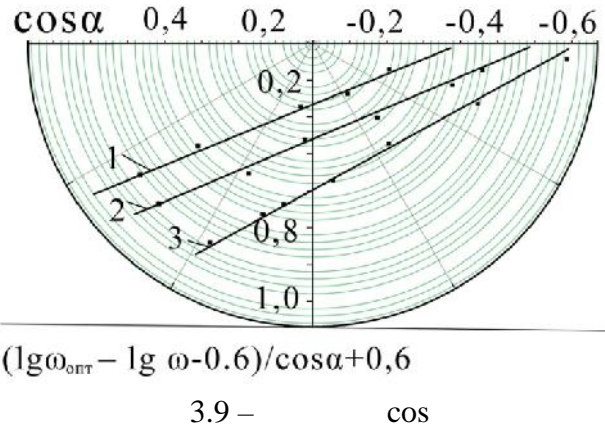
L/G

[47].

3.3



3.8 – $\dot{\alpha}$:
1 – =21,2; 2 – =13,5; 3 – =7,7 (/)



3.9 – cos :
1 – =21,2; 2 – =13,5; 3 – =7,7 (/)

$\dot{\alpha} > 0$.

(3.9).

$\dot{\alpha} > 90^\circ$,

$\dot{\alpha} < 90^\circ$.

$\dot{\alpha}$,

, $\dot{\alpha} = 10^\circ$,

= (cos $\dot{\alpha}$)

cos $\dot{\alpha} = -0,2$

$$= \exp(a \cdot \cos \dot{\alpha} + b \cdot \cos^2 \dot{\alpha})$$

$a, b -$

$$(\lg \dots - \lg \dots) / \cos \dots + 0,6 \dots \cos \dots \quad \lg \dots - 0,6$$

$$\cos \dots = -0,6. \quad (3.9),$$

$$\approx \exp \left[- (1,06 + 0,034 \nu) \cdot \cos \alpha - 2,18 \cdot \cos^2 \alpha \right] \quad (3.1)$$

$= 10 \div 30^\circ$

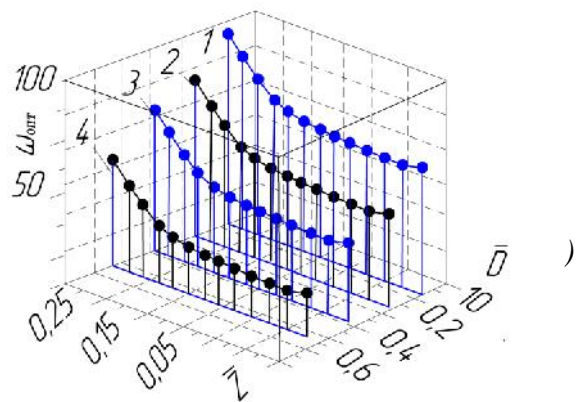
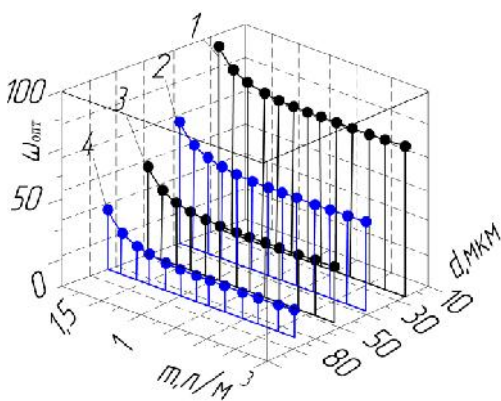
$\dots \dot{\alpha} = 100 + 110^\circ.$

$z,$

$\check{z} = /z$

$$= (D/z)/D$$

$(3.10,)$



3.10-

1- = 34,5 / ; 2- = 21,7 / ; 3- = 13,5 / ; 4- = 7,2 /

$$z^{1,05}$$

(3.10,).

$$\exp(-0,018 \cdot 10^6 d_p)$$

G

(25 /).

2

(2).

1,65

$$\approx (m \cdot 10^6)^{0,31}$$

3.10,

$$\approx \check{D}^{-0,31}$$

$$= 397.38 \cdot v^{1.65} (m \cdot 10^6)^{0.31} \check{D}^{-0.31} \cdot \check{z}^{1.05} \times \exp[-0.018 \cdot 10^6 d_p - (1,06 + 0,034v) \cdot \cos \alpha - 2,18 \cdot \cos^2 \alpha] \quad (3.2)$$

3.1 –

	n	R ²	R _k	D		
3.8	17	86,70	0,9311	0,61	0,0213 ¹	4,58 ¹
3.9	14	86,63	0,9308	0,56	0,0206 ¹	4,92 ¹
3.10,	23	92,65	0,9625	2,51	0,0066 ¹	0,84 ¹
3.10,	15	98,36	0,9918	1,40	69.29 ¹	2,78 ¹
3.10,	16	97,19	0,9858	1,44	74.82 ¹	2,40 ¹
3.10,	17	85,54	0,9249	1,04	0,306 ¹	0,83 ¹

± 1,5%,

3.4

3.4.1

.
 ,
 ,
 , . . . :

$$\Delta = \Delta + \Delta \tag{3.3}$$

:

$$\Delta = \sum \xi \frac{\rho v^2}{2}$$

$$\sum \xi = \xi + \xi$$

— ;
 — , , .
 [87],

. :
 90°,
 , , -
 .
 « » [86].
 « »

k,

，
，
·
-
； -
· [125]

$$\xi = \frac{1}{n} \left(\left(\frac{R}{r} \right)^{2n} - 1 \right) + \frac{1}{k^2} \cdot \left(\frac{v_2}{v_1} \right)^2, \quad (3.4)$$

$$\xi = 4 \cdot \left(\frac{L}{G} \right)^{0.6} \cdot \sqrt{1 + \frac{1}{k^2}}, \quad (3.5)$$

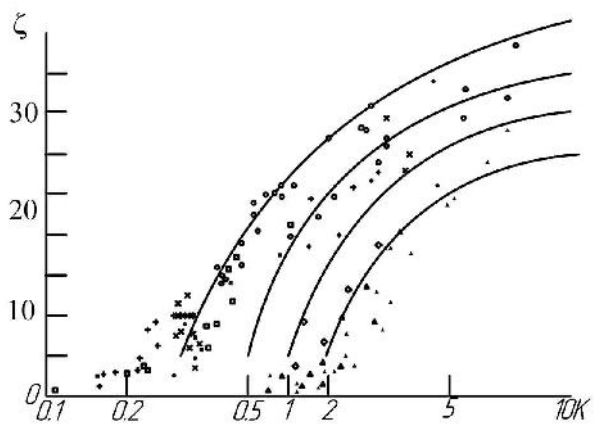
R - ， ；
 r - ， ；
 L, G - ， $^3/$ ；
 v_1, v_2 - ， / ；
 - ；
 k - ；
 n - 。

(3.6):

$$\xi = \frac{1}{n} \left((R/r)^{2n} - 1 \right) + \frac{\varepsilon^2}{K^2} \left(1 + \frac{\rho}{\rho} \right) \cdot \left(\frac{v}{v} \right)^2 + 4 \cdot \left(\frac{Q}{G} \right)^{0.6} \cdot \sqrt{1 + \frac{1}{K^2}} \quad (3.6)$$

(3.11). 3.12 ，
 $=45^\circ$ ，

6...8% ， $=30^\circ$.



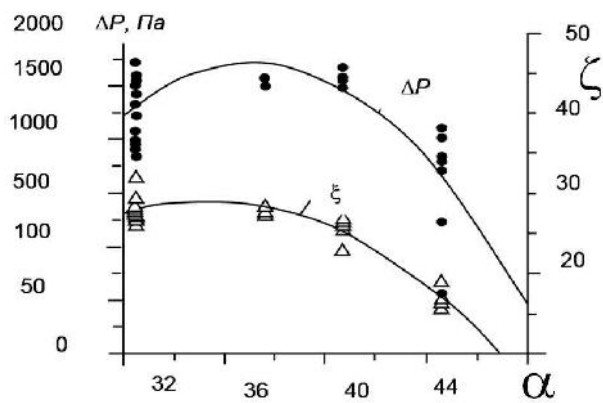
3.11 –

$K:$

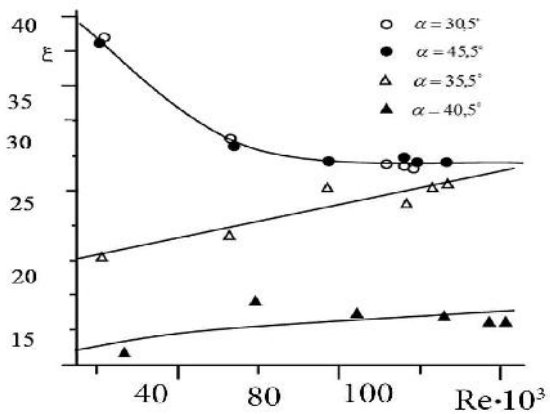
— ;.....

$(90^\circ \div 45^\circ),$

$Re = D / \mu.$



3.12 –



3.13 –

3.12 , =45°

, 6...8%
 =30°. 3.13,
 8·10⁴ .
 35,5°,

3.4.2

$$H_T = \rho u \left(u - \frac{v}{\operatorname{tg} \beta_2} \right) \quad (3.7)$$

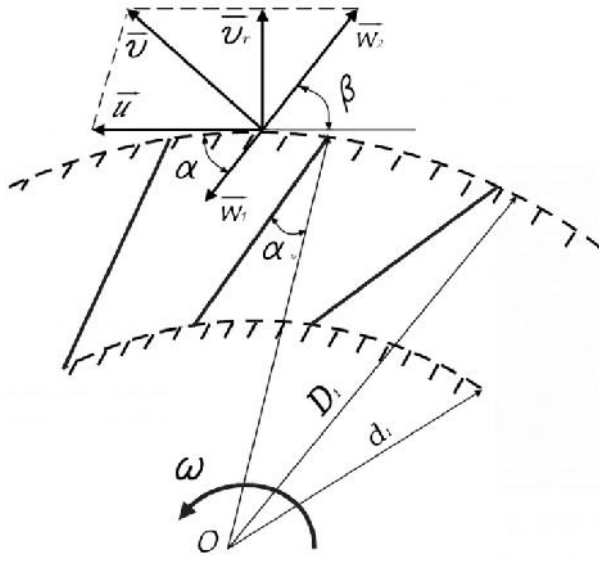
— , / ;
 — .

3.12, 3.13

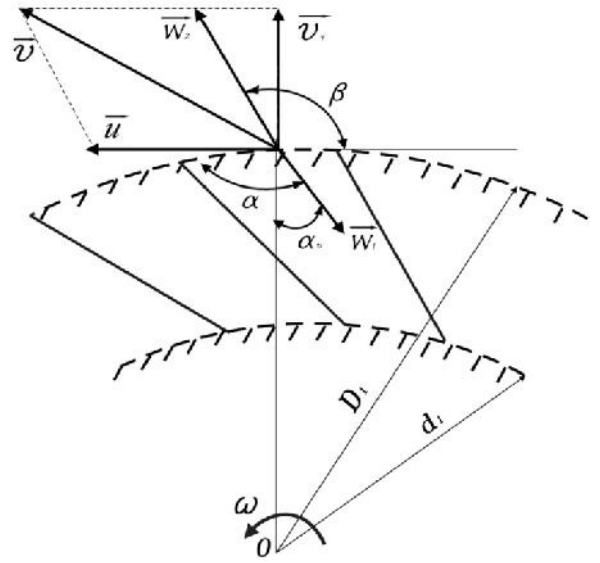
$$= W_2 \cdot \sin \alpha_2$$

W₂ — , / .

$$H_T = \rho u (u - W_2 \cos \beta_2) \quad (3.8)$$



3.14 -



3.15 -

(3.8)

[5],

($p > 3$).

$$y > 0 \quad \tau_p = \frac{2l_1 z}{D_1 + l_1 z \sin \alpha_y}$$

$$y = 0 \quad \tau_p = \frac{l_1 z}{(D_1 + 2l_1)}$$

$$p = 0,8 \div 2,5 \quad [55].$$

$\mu,$

$$2 = 20 + 170^\circ$$

μ

[50].

(3.14, 3.15) $u = \cdot (D/2), \quad 2 = ,$

$\mu,$

:

$$\mu = \frac{1}{1 + \frac{1,5 + 1,1\beta_2 / 90}{z(1 - \bar{d}_1)}} \quad (3.9)$$

(3.9) (3.8)

$$H_T = \rho u(u - W_2 \cos \beta_2) \frac{1}{1 + \frac{1,5 + 1,1\beta_2 / 90}{z(1 - \bar{d}_1^2)}}$$

, ,

$$H_T = \frac{\rho u(u - W_2 \cos \beta_2)}{1 + \frac{1,5 + 1,1\beta_2 / 90}{z(1 - \bar{d}_1^2)}} \quad (3.10)$$

.

, (),

(3.15).

$$u = \omega \frac{D_1}{2} \quad \beta_2 = \alpha$$

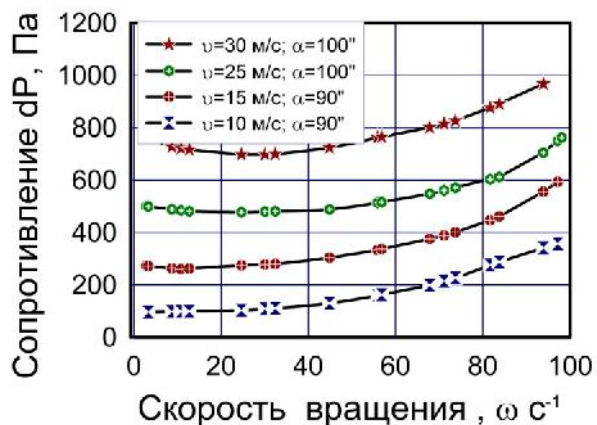
(3.3) (3.10)

:

$$\Delta \rho_{\omega > 0} = \frac{0,5 \rho \omega D_1 (0,5 \omega D_1 - W_1 \cos \alpha)}{1 + \frac{1,5 + 1,1 \alpha / 90}{z(1 - d_1^2)}} \quad (3.11)$$

(3.11) (3.3),

: $\Delta = \Delta + \Delta + \Delta \rho_{\omega > 0}$



3.16 –

10%,

3.5

(« »)

(
) [50].

63].

[55, 56,

$$\begin{aligned}
W_x &= \dot{v}_x i + \dot{v}_y j = \frac{VD_0}{v_r} = \frac{v_x D_0}{v_r} i + \frac{v_y D_0}{v_r} j \\
\dot{W}_\varphi &= \dot{W}_x i + \dot{W}_y j = \frac{WD_0}{v_r} = \frac{W_x D_0}{v_r} i + \frac{W_y D_0}{v_r} j \\
W_r &= \dot{U}_x i + \dot{U}_y j = \frac{UD_0}{v_r} = \frac{U_x D_0}{v_r} i + \frac{U_y D_0}{v_r} j
\end{aligned} \tag{3.12}$$

(3.12) x y

$$\frac{\rho_l D_0}{\rho_r v_r^2} \cdot \frac{dv_x}{dt} = -\frac{3}{4} \left(\frac{D_0}{v_r}\right)^2 \psi_c |U| U_x \tag{3.13}$$

$$\frac{\rho}{\rho_r v_r^2} \cdot \frac{dv_y}{dt} = -\frac{3}{4} \left(\frac{D_0}{v_r}\right)^2 \psi_c |U| U_y + \frac{\rho}{\rho_r v_r^2} \cdot g \tag{3.14}$$

(3.13) (3.14)

 $dx, \quad dy, \quad :$

$$\frac{\rho}{\rho_r v_r^2} \cdot v_x \cdot \frac{dv_x}{d} = -\frac{3}{4} \cdot \frac{D_0^2}{v_r^2} \psi_c |U| U_x \tag{3.15}$$

$$\frac{\rho}{\rho_r v_r^2} \cdot v_y \cdot \frac{dv_y}{d} = -\frac{3}{4} \frac{D_0^2}{v_r^2} \psi_c |U| U_y + \frac{\rho}{\rho_r v_r^2} \cdot g \tag{3.16}$$

$$T = \frac{\rho_r v_r t}{\rho D_0^2}; X = \frac{\rho_r x}{\rho D_0}; Y = \frac{\rho_r y}{\rho D_0};$$

$$P = \frac{\rho_l D_0^3}{\rho_r v_r^2} g; \psi = \frac{3}{4} \psi_c |U|$$

(3.16)

:

$$\frac{d\dot{v}_x}{dT} = -\psi \dot{U}_x \quad \frac{d\dot{v}_y}{dT} = -\psi \dot{U}_y + P \tag{3.17}$$

$$\dot{U}_x \frac{d\dot{v}_x}{dx} = -\psi \dot{U}_x \quad \dot{U}_y \frac{d\dot{v}_y}{dy} = -\psi \dot{U}_y + P \tag{3.18}$$

, (3.17) :

$$\Delta \dot{U}_y = \Delta \dot{U}_x \left(\frac{\dot{U}_y}{\dot{U}_x} - \frac{P}{\Psi \dot{U}_x} \right), \quad (3.19)$$

(3.18)

$$\Delta X = -\frac{\dot{v}_x \Delta \dot{v}_x}{\Psi \dot{v}_x}, \quad \Delta Y = -\frac{\dot{v}_y \Delta \dot{v}_y}{\Psi \dot{v}_y - P} \quad (3.20)$$

(3.17, 3.18) ,

$$\frac{\rho_r l}{\rho_l D_0} = idem, \quad (3.21)$$

$$\frac{UD_o}{v_r} = idem, \quad (3.22)$$

$$\frac{\rho_l D_0^3}{\rho_r v_r^2} \cdot g = idem, \quad (3.23)$$

$$\frac{\dot{U}_x}{\dot{U}_y} = idem, \quad (3.24)$$

$l -$

[120].

:

$$T = \frac{\rho_r v_r t_l}{\rho_l D_0^2} \quad (3.25)$$

$$\frac{\rho_r d_x}{\rho_l D_0} = idem, \tag{3.26}$$

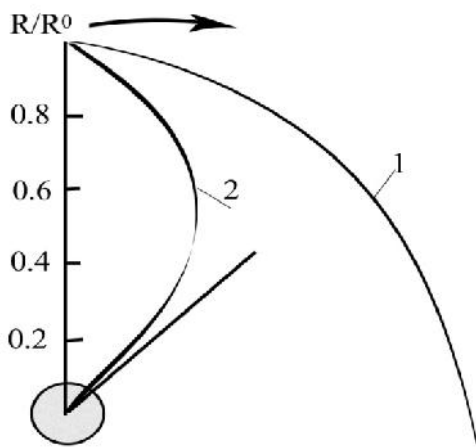
$$\frac{U d_l}{v_r} = idem, \tag{3.27}$$

$$\frac{\dot{U}_x}{\dot{U}_y} = \frac{\omega_{pt}}{v_l} = idem, \tag{3.28}$$

d_x – , ;
 d_l – , ;
 ω – , / ;
 v_l –

(3.26 – 3.28)

3.17



3.17 –

R_l 1
 , 2

$$\rho_l u^2 D_0^2; \sigma D_0; \mu_l u D_0; \rho_r u^2 D_0^2$$

:

$$\frac{\sigma}{\rho_l u^2 D_0} = idem \quad (3.29)$$

$$\frac{\mu_l}{\rho_r u D_0} = idem \quad (3.30)$$

:

$$\frac{\sigma}{\rho_l u^2 d_l} = idem \quad (3.31)$$

$$\frac{\mu_l}{\rho_r u d_l} = idem \quad (3.32)$$

(3.31) (3.32),

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,

$$\frac{\rho_r d_x}{\rho_l d_l} = idem \quad (3.33)$$

$$\frac{U d_l}{v_l} = idem \quad (3.34)$$

$$\frac{\omega}{v_l} = idem \quad (3.35)$$

$$\frac{\sigma}{\rho_l \omega^2 d_l} = idem \quad (3.36)$$

$$\frac{\mu_l}{\rho_l \omega d_l} = idem \quad (3.37)$$

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3.5.1

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 , (3.31), (3.32), (3.36) (3.37)

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 , ,

$$\sqrt{1 + (v_l / \omega)^2},$$

..

$$\frac{d_x \omega}{v_r} \cdot \frac{\mu_l}{\rho_l v_l d_l} \cdot \sqrt{1 + (v_l / \omega)^2} = idem \quad (3.38)$$

:

$$\sqrt{1 + (v_l / \omega)^2} = f_1(m_1),$$

(3.38)

$$\frac{Re_r}{Re_l} f_1(m_1) = idem \quad (3.39)$$

m_1 - ,

, / ³.

Re_r Re_l \tilde{m} , ..

$$\tilde{m} = \frac{Re_r}{Re_l} = \frac{\omega d_x v_l}{v_l d_l v_r} \quad (3.40)$$

(3.39)

$$\tilde{m} = f_2\left(\frac{1}{m_1}\right) \quad (3.41)$$

$$f_2\left(\frac{1}{m_1}\right) = \frac{idem}{f_1(m_1)}$$

$$- = const \quad (3.36)$$

:

$$\frac{G_0}{\omega^2} = idem, \quad (3.42)$$

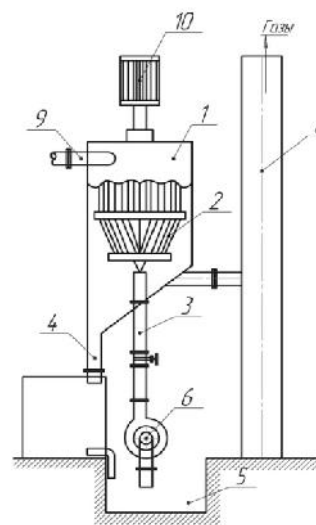
$$G_0 = - \frac{\sigma}{\rho_l d_l} \quad (3.42) \quad \omega_l^2,$$

$$\frac{G_0}{v_l^2} \cdot \left(\frac{v_l}{\omega}\right)^2 = idem \quad (3.43)$$

$$(3.43) \quad , \quad \dots \quad \sqrt{\quad} \quad m_l$$

$$(\quad) , \quad \omega_l \quad m_l \quad \omega \quad const, \quad (3.36)$$

$$(3.35) \quad (3.41)$$



3.18 -

m_l 2.

()

(3.18) :

$$d_x = d_2(1 + 2\Theta_0 \operatorname{tg} \frac{\alpha_1}{2}) \quad (3.44)$$

$$\omega = \frac{4Q_1}{\pi d_2^2 (1 + 2\Theta_0 \operatorname{tg} \frac{\alpha_1}{2})^2} \quad (3.45)$$

$$Q_1 - \dots ;$$

$$1 - \dots$$

$$d_x \quad (3.40)$$

0,

$$\Theta_0 = \frac{L_x}{d_2} = \frac{1}{2 \operatorname{tg} \frac{\alpha_1}{2}} \left(\frac{Q_1 v d_l}{Q v \tilde{m} d_2 \sin \varphi} - 1 \right) \quad (3.46)$$

-

;

$$Q_1 - \dots$$

$$, \quad Q_1 \quad , \quad Q \quad , \quad (3.46)$$

$$:$$

$$\Theta_0 = \frac{1}{2 \operatorname{tg} \frac{\alpha_1}{2}} \left(\frac{\omega_2 d_2 v \gamma_2}{v_l d_l v \gamma_1 \tilde{m}} - 1 \right) \quad (3.47)$$

1 2-

, , / 3.

(3.48)

$$\Theta_1 = \frac{L_0}{d_1} = \frac{L_1 - \psi d_2}{d_1} \quad (3.48)$$

(3.49)

$$\Theta_1 = \frac{1}{2 \operatorname{tg} \frac{\alpha_1}{2}} \left(1 - \frac{Q_l v_l d_l}{Q_l v_l \tilde{m} d_1 \sin \varphi} \right) \quad (3.49)$$

$L_l -$

, ;

$d_1 -$, ;
 $L_0 -$, ;
 $-$ $L_0 d_1$ [31-33]

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$$_1=(0,06\div 0,10),$$

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[73, 77].

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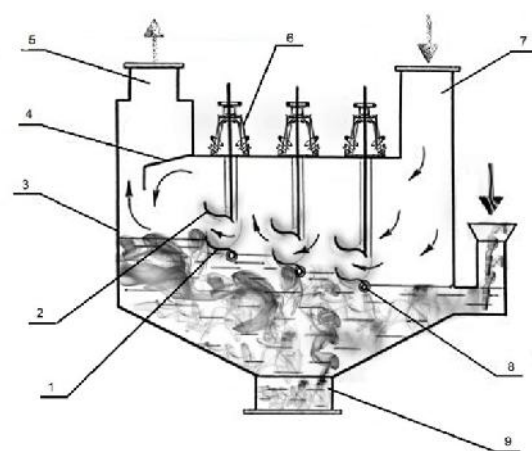
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4.1 -

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8 - ; 9 -

9,

« » (4.2).

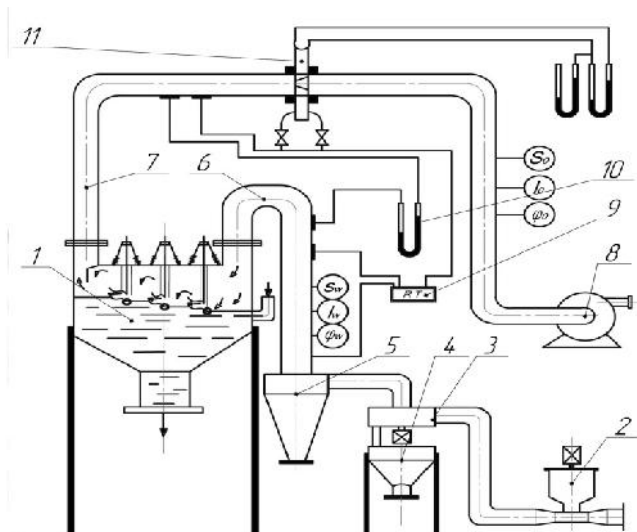
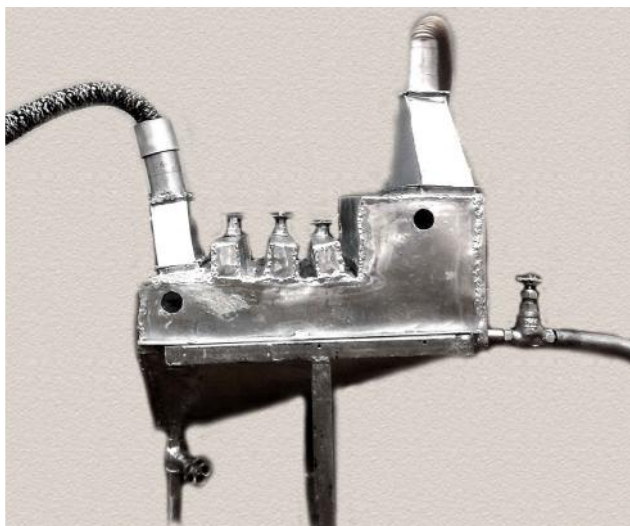
3

15 / .
800 .

0,5 / ³

600 / ³

96,3 % [254].



4.2 – " "

4.3 – :

1 – ; 2 – ;
3 – ; 4 – ;
5 – ; 6,7 – ; 8 –
; 9 – ;
10 – ; 11 –

$h = 0,175$.

« »

[104].

[105].

[101].

(4.4).

1

[67].

[68].

(4.4).

[69].



4.4 –

– 11,
–55,

-10

$$\Delta G_2 - \Delta G_1 = Q \left(\frac{\Delta G_1}{G_1} - \frac{\Delta G_2}{G_2} \right), \quad : = (G_1 - G_2) / G_1$$

$$, / \quad S, \quad : Q = \cdot S, \quad U-$$

1)

2)

-55

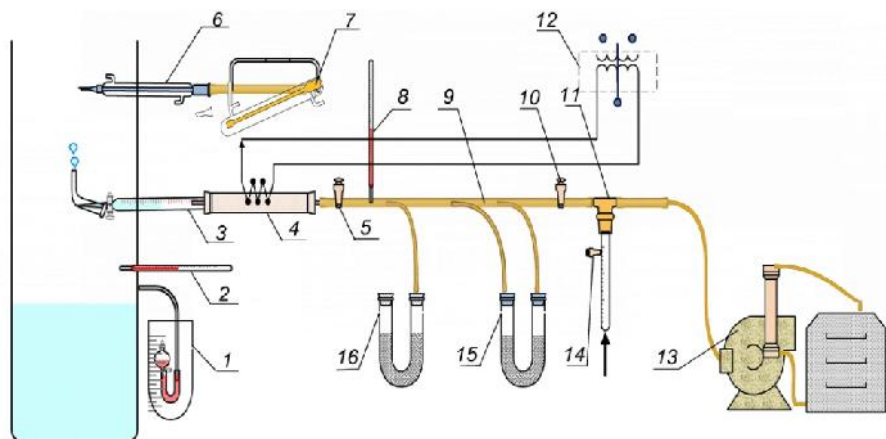
-10,

-55.

$$100 \div 200 \quad / \quad 3$$

[69]

4.5.



4.5 –
 1 – ; 2, 8 – ; 3 – ; 4 – ; 5, 10 – ;
 2, 8 – ; 7 – ; 9 – ; 11 – ;
 12 – ; 13 – ; 14 – () ;
 15, 16 –

3

-10, 4.

9,

15,

13.

8

16,

2

1.

11

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14,

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5,

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,

$$m = L / L, \quad 3/3,$$

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$m,$,

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:

$$\frac{g}{S} = \frac{g}{bh_k - bh} - \frac{g}{b(h_k - h)} \tag{4.1}$$

S - ;

b - ;

h - ;

h - .

,

:

$$m = f(g \cdot h) \tag{4.2}$$

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[157]:

$$d = \frac{467 \cdot 10^3 \sqrt{\sigma}}{g_o} + 17,869 \cdot \left(\frac{\mu}{\sqrt{\rho \cdot \sigma}} \right)^{0,68} \frac{L}{L} \tag{4.3}$$

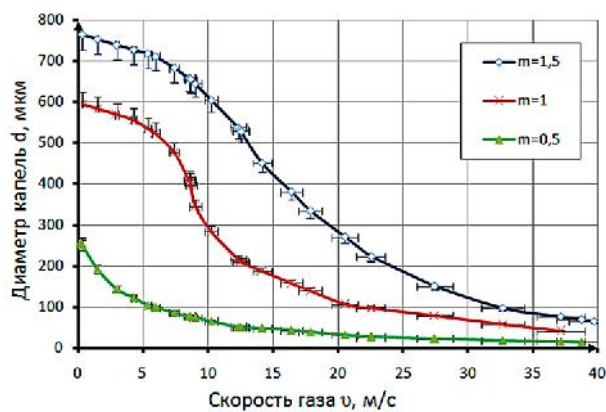
- 0 - , / ;
- , / ;
- , /³;
- μ - , / ;
- L - , /³ ;

$$L = \dots, \quad (4.3)$$

4.6

20° : = 998 /³; μ = 1,002·10⁻³ · /²; = 72,86 · 10⁻³ / .

(4.3)



4.6 –

0
m.

:

$$\eta = f\left(\frac{m}{\xi_c} \cdot \frac{\vartheta}{d_0}\right) \quad (4.4)$$

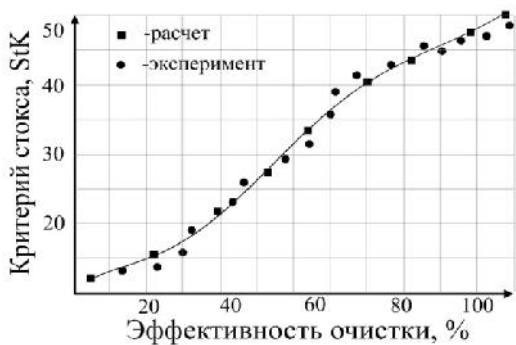
m –
–
–
d₀ –

;

;

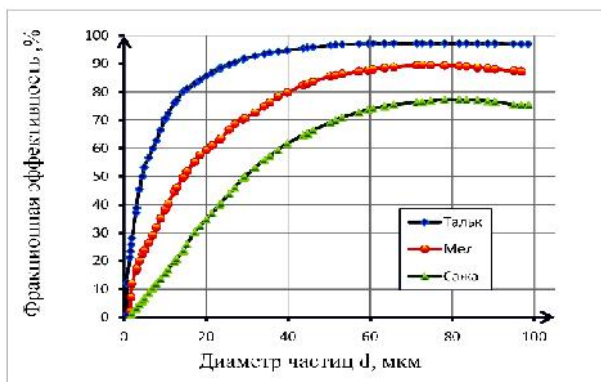
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4.7



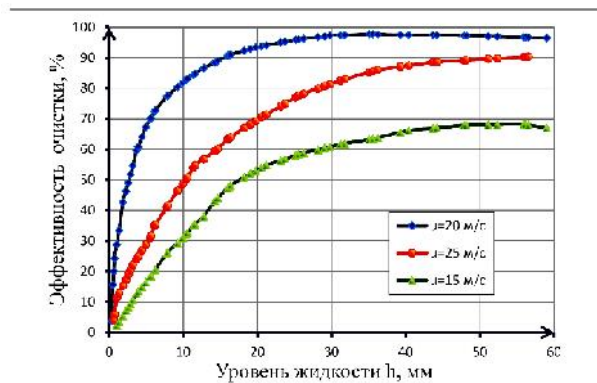
4.7 –

StK



4.8 –

4.8



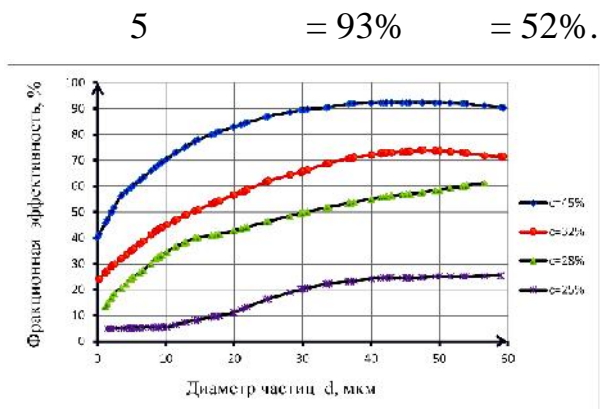
4.9 –

70%.

75%.

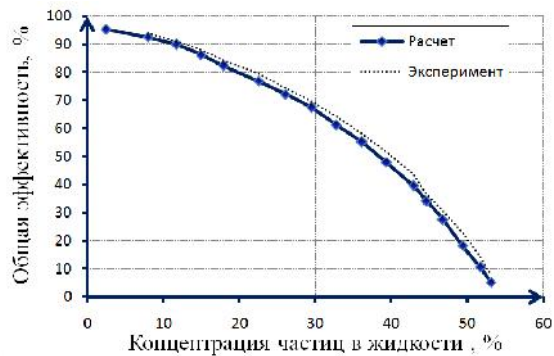
5
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20 23 / (4.9).



4.10 –

5
36% 45%
98% 90%



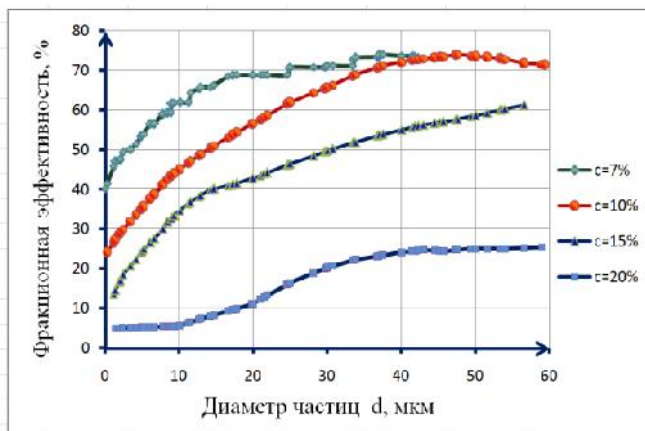
4.11 –

(83,2% 99,8%

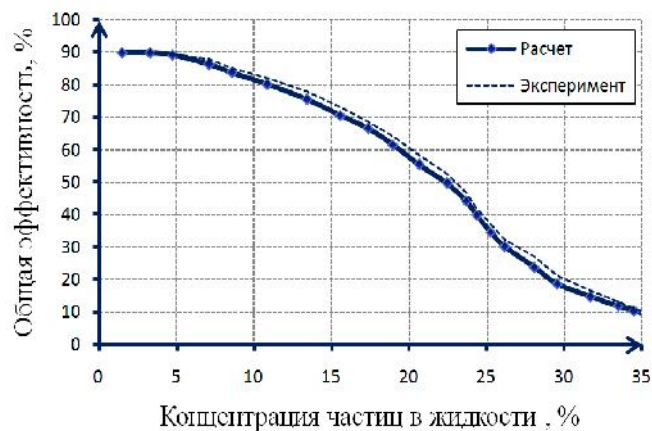
).

7% 20%
 = 65% = 20%, (4.12, 4.13),
 18% 30% = 80% = 50%.

(50%).



4.12 –



4.13 –

[102].

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1.

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3.

4.

5.

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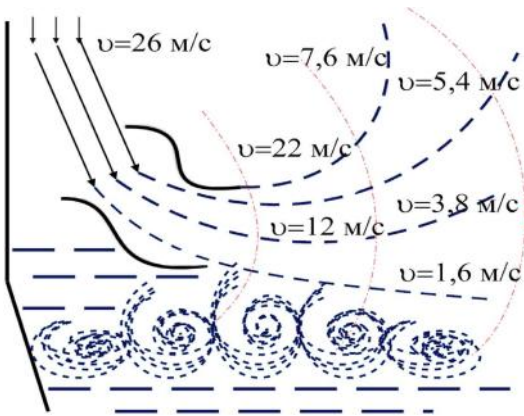
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4.14 -

300 600 [82].

h -

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d -

n -

A_r -

V -

()

10 / ,

10 / ,

"

"

[80]:

$$\frac{h}{d} = n\sqrt{A_r} \tag{4.7}$$

, :

$$A_r = \frac{\rho V^2}{gd\rho_l} \tag{4.8}$$

, / .

[84]:

$$\frac{D_v}{d} = 1 + 0,67\left(\frac{h}{d}\right)^{0,85} \tag{4.9}$$

" "

$$V_o = Vg \cdot \frac{d^2}{D_v^2 - d^2} \tag{4.10}$$

" "

:

$$\frac{dW}{d\xi} = \frac{8\alpha\xi}{\pi(\xi+1)(\xi-1)^3} \tag{4.11}$$

=dW/dZ -

W=f+ -

Z=x+ y -

;

.

$$\tag{4.11}$$

:

$$W = \frac{\alpha}{\pi} \left[\ln \frac{\xi+1}{\xi-1} - 2 \frac{\xi}{(\xi-1)^2} \right] \tag{4.12}$$

(4.11)

$$\frac{dZ}{d\xi} = \frac{dZ}{dW} \cdot \frac{dW}{d\xi} = \frac{1}{\xi} \cdot \frac{dW}{d\xi} \tag{4.13}$$

Z

$$\frac{dZ}{d\xi} = \frac{8a}{\pi(\xi+1)(\xi-1)^2} \tag{4.14}$$

$$Z = \frac{a}{\pi} \left[\ln \frac{\xi-1}{\xi+1} + 2 \frac{\xi-2}{(\xi-1)^2} + 4 \right] \tag{4.15}$$

(4.15)

0

=0.

$$\tag{4.12}$$

(4.15)

,

f

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:

$$Z' = \frac{\pi \cdot Z}{a} = x + iy = \frac{\pi \cdot x}{a} + i \frac{\pi \bar{\pi} \cdot y}{a}$$

$$W' = \frac{\pi W}{a} \quad ;$$

$$Z = - \left[W + \frac{4}{(\xi-1)^2} - 4 \right] \quad (4.16)$$

$$Z' = \quad ;$$

$$W' = \quad .$$

$$m_r \frac{d\vec{V}_r}{\tau} = \vec{F} \quad (4.17)$$

$$m_r = \quad ;$$

$$\vec{V}_r = \quad ;$$

$$\vec{F}_r = \quad ,$$

(4.17)

d 70

:

$$\frac{\pi d_r^3}{6} p_r \frac{d\vec{V}_r}{d\tau} = \frac{\pi d_r^3}{6} p_r \vec{g} - 3\pi \mu d_r (\vec{V} - \vec{V}_r) \quad (4.18)$$

(4.18)

:

$$V_{r0} = \frac{V_r}{V} ; V_0 = V_0 = \frac{\vec{V}}{V} ; \tau_0 = \tau \frac{V}{a}$$

$$\frac{d\vec{V}_{r0}}{d\tau_0} = \frac{\vec{g}}{g} F_r - \frac{1}{St} (\vec{V}_0 - \vec{V}_{r0}) \quad (4.19)$$

$$F_r = \frac{ga}{V_\infty^2} - \quad ;$$

$$St = \frac{d_r^2 p_r V}{18\mu a} - \quad .$$

:

$$V_{r0x} = \frac{d}{d\tau_0} ; V_{r0y} = \frac{dY}{d\tau_0} = \frac{d^2}{d\tau_0^2} ; \frac{dV_{r0y}}{d\tau_0} = \frac{d^2 Y}{d\tau_0^2}$$

x y:

$$\frac{d^2x}{d\tau_0^2} = -F_r - \frac{1}{St} \left(V_{0x} - \frac{dx}{d\tau_0} \right) \quad (4.20)$$

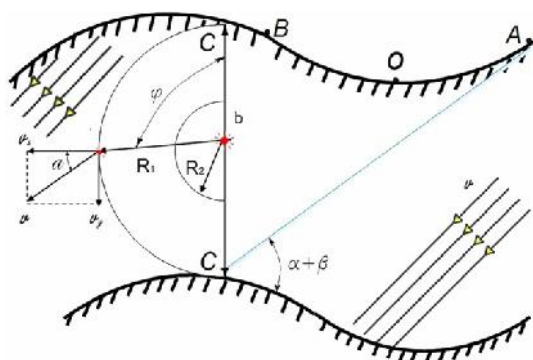
$$\frac{d^2y}{d\tau_0^2} = -\frac{1}{St} \left(V_{0y} - \frac{dy}{d\tau_0} \right)$$

(4.18-4.20)

4.5

71-73].

[61,



4.15.

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$$p_c/p_r + 0,5v_c^2 = p_1/p_2 + 0,5v_1^2 = p^*/p \tag{4.21}$$

* _

0

> 0 .

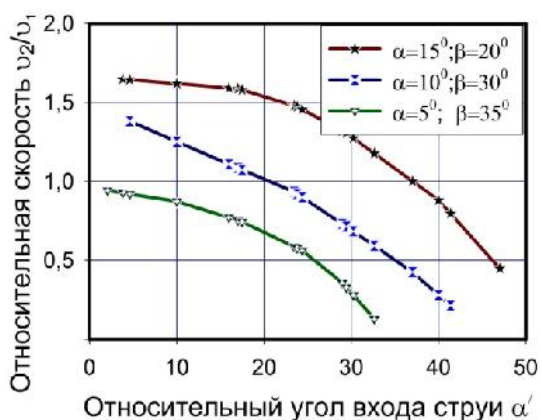
$$S \sin \alpha_1 = \frac{b}{l} \sin \alpha_2 \tag{4.21}$$

$$v_1 \rho Q_k \cos(\alpha_1 + \beta) + \rho_1 F_k \sin \beta = v_2 \rho Q_k \cos(\alpha_2 - \beta) + \rho_2 F_k \sin \beta, \tag{4.22}$$

$$v_2/v_1 = (l/\sin\beta) \left[\sin\alpha_1 \cos(\alpha_2 - \beta) + \sqrt{\sin^2\alpha_1 \cos^2(\alpha_2 - \beta) + \sin\beta \cdot \sin(2\alpha_1 + \beta)} \right] \tag{4.23}$$

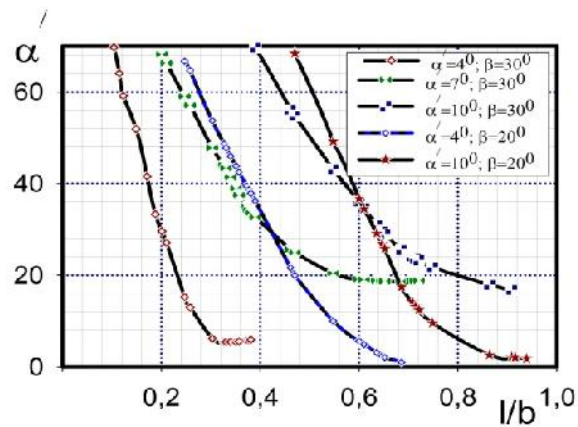
$$l/b = (v_2/v_1) \sin\alpha_1 = \sin\beta \sin\alpha_1 / \sin\alpha_2 + \sin(\alpha_1 + \beta) \tag{4.24}$$

4.17)



4.16 –

2/ 1



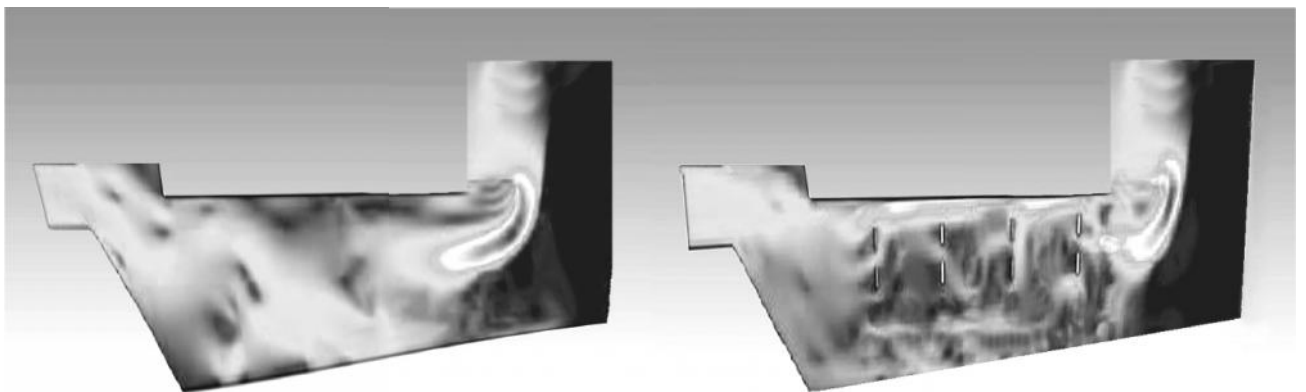
4.17 –

Ansys CFX.

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4.19).

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4.18 –

4.19 –

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4.6

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 Jarzkbbski Giowiak [113], -
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 Nukijama Tanasawa [174, 175], ,
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[185]

[183, 186]

Kabsch [112]

 $m_s,$

$$r = \frac{m_s}{A \cdot t}$$

, Kabsch [112]

Calvert'a

Pemberton'a [115]

Semrau, Barth'a

Stokes'a.

Slinna [116],

[82],

Jarzkbski Giowiak [125],

Tanasawa [76],

Nukijama

[120],

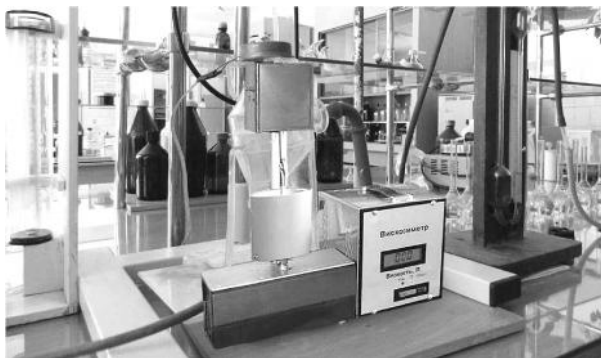
» [254] (4.2),

[103].

4.4).

[105],

($\delta_{50} = 15$, $10^{-3} \%$ $\delta_{50} = 25$ (25°C)).



4.20 –

$$-8 \quad (4.20).$$

2

[105]:

$$V = \int_0^t Q \cdot dt = \frac{f \cdot (P_1 - P_2)}{8 \cdot l \cdot \gamma} \cdot R^4 \cdot t$$

$$[\eta] = \frac{\pi \cdot (P_1 - P_2) \cdot R^4}{8 \cdot L \cdot V} \cdot t \quad (4.25)$$

[] – ; P_1, P_2 – ; R – ; L – ; V – ; t – ; k – ,

$$[\eta] = \frac{kGt}{L} \quad (4.26)$$

(93,2%

99,8%

)

(4.21),

5

36%

45%

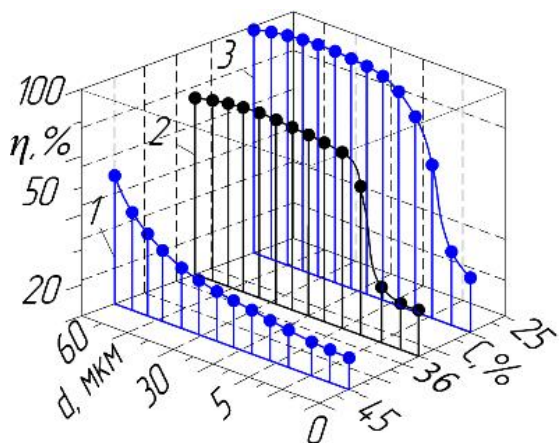
98%

90%

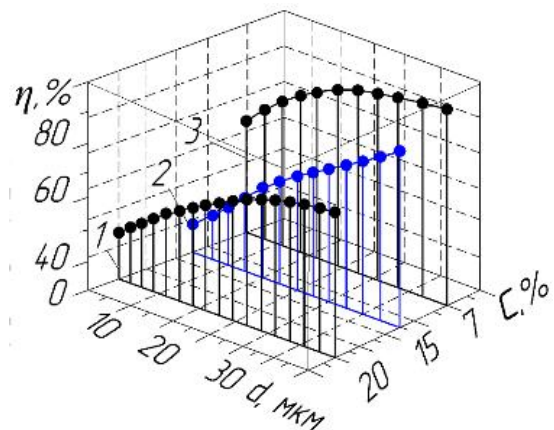
5

= 93%

= 52%.



4.21 –



4.22 –

: 7% 20%
 = 65% = 20%, (4.22),
 : 18% 30% = 80%
 = 50%.
 (50%).

4.21-4.22

(80-88%

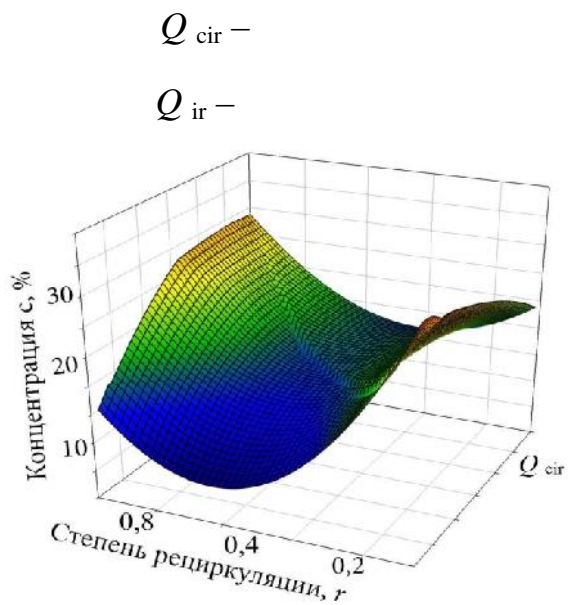
50-65 %

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[164-166].

0,02 0,05 / ³, . . .

$$r = \frac{Q_{cir}}{Q_{ir}} \tag{4.27}$$



4.23 –

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$$G \cdot (c - c_r) \approx G \cdot c = Q_{cir} \cdot c_r \tag{4.28}$$

$$(c - c_r) = c_r \cdot \frac{G}{Q_{cir}} \tag{4.28}$$

,

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$$r = 1 - \frac{G \cdot c}{Q_{cir} \cdot c_r} \tag{4.29}$$

c_r

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[234].

5.1 –

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[228].

15 40 / .

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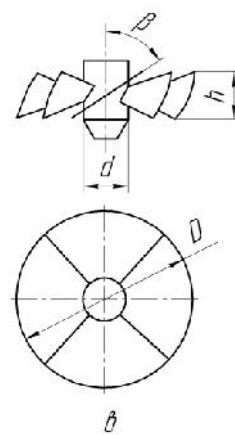
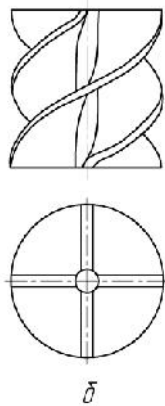
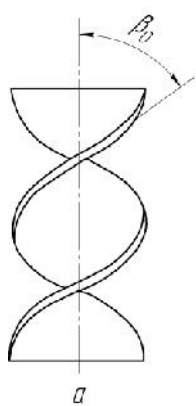
(20:50)

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5.1,)

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(5.2,) [134].



5.1 -

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(5.1,)

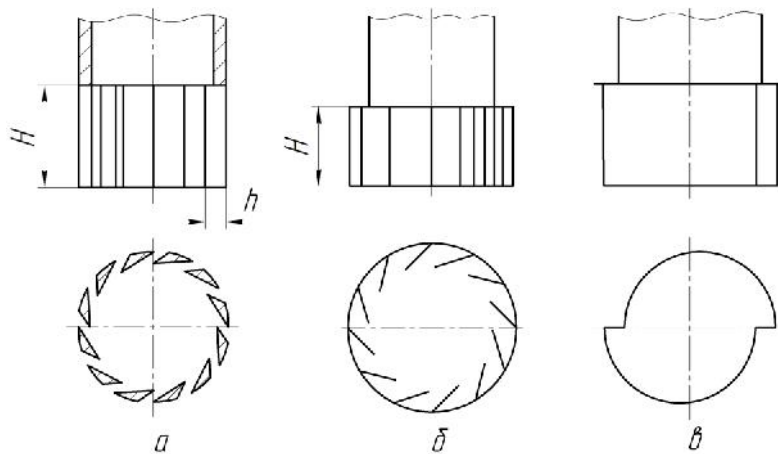
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(5.2,) [134],

50 150 .

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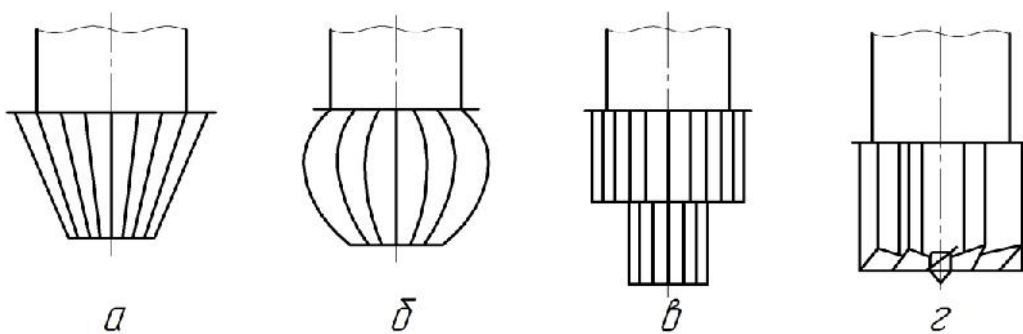
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5.2-

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- ; - ; -
 (5.2) [134]



5.3-

:

- ; - - ; - - ;

n

S

5.2 –

	f	n	S
	$\frac{2}{1 + \sqrt{1 + \text{tg}^2 \beta_0}}$	$\approx \frac{2}{3} \text{tg} \beta_0$	$\frac{2 \text{htg} \beta_0}{\pi D}$
	$\left[1 - \frac{d^2}{D^2}\right] \cos \beta - \left(1 - \frac{d}{D}\right) \frac{2\delta z}{\pi D}$	$\text{tg} \beta$	$\frac{zh \sin \beta}{\pi D \cos \beta - \delta z}$
	$\frac{4bHz}{\pi D^2}$	$\frac{\sin \gamma}{f}$	$\frac{h \sin \gamma}{b}$
	$\frac{4H}{D} \left(\cos \gamma - \frac{\delta z}{\pi D}\right)$	$\frac{\sin \gamma}{f}$	$\frac{zh \sin \gamma}{\pi d \cos \gamma - \delta z}$

$z, -$; $b -$
 ; $-$; $H -$; $h -$
 ; $D -$; $d -$.

5.2

(5.4) [14, 134].

n

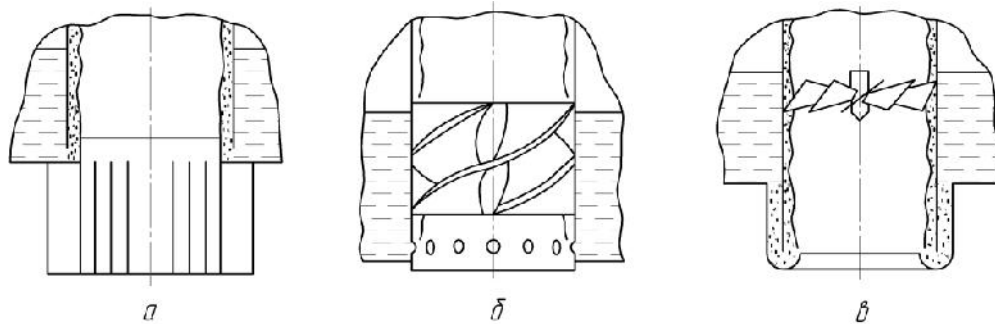
5.3.

5.3 –

				H/D	
20 – 40	-	0,5 – 1,0	-	5 – 8	
50 – 100		1 – 1,5		2 – 5	

100 – 200		1 – 1,5		1 – 2	-
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H/D



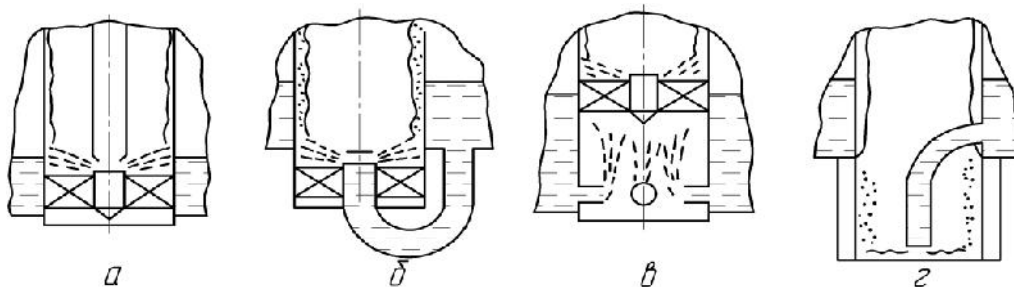
5.4 –

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5.5) [11, 14]. , U- -

(. (5.5, ,)



5.5 -

- ; -U- ; - ; - -

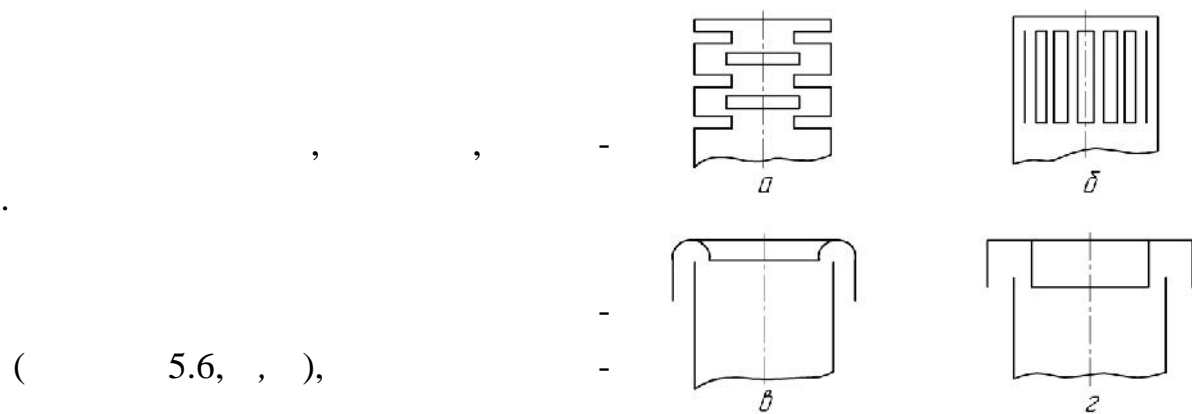
(5.5,)

[14,16,20].

(5.3,)

[14].

[11].



(5.6, ,),

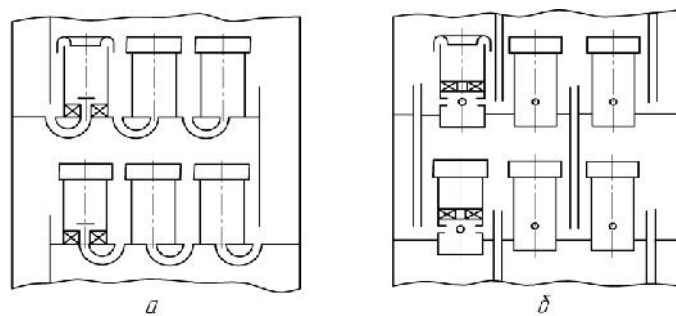
5.6-

(5.6 ,) [11,14].

[11].

[134].

[16, 19, 21],



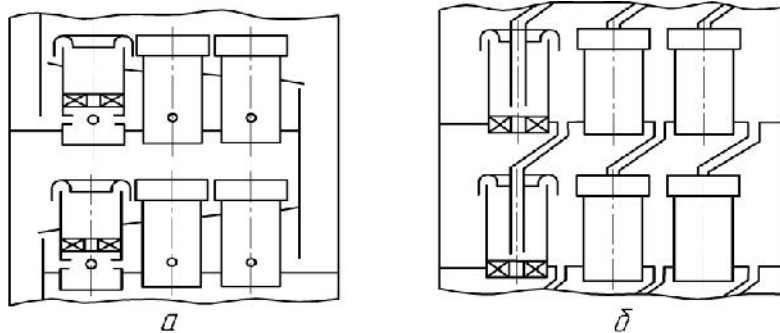
5.7 -

(5.7,)

(5.7,)

(5.8,) [102, 105],

(.5.8,) [20, 102, 106].



5.8 -

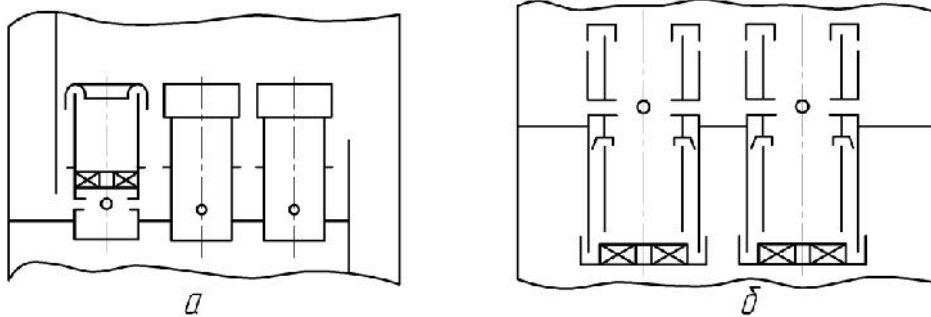
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- ; -

(5.9,) [106, 107]

(5.9,)

[108].



5.9 -

- ; -

L/G

L/ G

[101, 107].

, 300 600 .

5.2

[234]:

1.

2.

3.

5.2.1

[33, 49],

[33]:

$$\begin{aligned}
 W_\varphi &= W_\varphi^m \frac{r}{r_b}; & W_z &= W_z^m \frac{r}{r_b} & (r \leq r_b) \\
 W_\varphi &= W_\varphi^m \frac{r_b}{r}; & W_z &= W_z^m & (r \geq r_b)
 \end{aligned}
 \tag{5.1}$$

$$W_z = \dots \quad (\quad)$$

$$r_b = \dots$$

[33]:

$$\begin{aligned} \frac{W_\phi}{\bar{W}_z} &= \frac{6}{f} \frac{(1-\bar{r})(\bar{r}-\varepsilon)}{(1-\varepsilon)^2} \sin \beta \\ \frac{W_z}{\bar{W}_z} &= \frac{6}{f} \frac{(1-\bar{r})(\bar{r}-\varepsilon)}{(1-\varepsilon)^2} \cos \beta \end{aligned} \quad (5.2)$$

$$\begin{aligned} z &= 2r/D - \dots \\ &= d/D - \dots \end{aligned}$$

$$\frac{\partial P}{\partial r} = \frac{\rho \bar{W}_\phi^2}{r} \quad (5.3)$$

$$g = \dots$$

$$(5.1) \quad f = \cos \beta$$

$$P(r=1) \quad (r=0) \quad :$$

$$\Delta P_r = 6n^2 \frac{\rho \bar{W}_z^2}{2} \quad (5.4)$$

[117]:

$$\begin{aligned} a_o &= 16,46 \cdot 10^{-3} \left(\frac{q}{\cos \beta} \right)^{0,3} ; \left(\frac{f}{\bar{W}_z} \right)^{0,75} \mu^{0,23} \quad \frac{q}{\cos \beta} \leq 1,1 \\ a_o &= 16,6 \cdot 10^{-3} \left(\frac{q}{\cos \beta} \right)^{0,4} ; \left(\frac{f}{\bar{W}_z} \right)^{0,75} \mu^{0,23} \quad \frac{q}{\cos \beta} \geq 1,1 \end{aligned} \quad (5.5)$$

$$\mu = \dots / \dots^2 ;$$

$$q = \dots^3 \cdot \dots ;$$

[11, 14, 117].

d [11]:

$$\frac{d}{D} = 0,05 \left(\frac{\sigma_l f^2}{\rho_g \bar{W}_z^2 D} \right)^{0,35} \quad (5.6)$$

(5.5).

$$\Delta z = 0,25D/n \quad (5.7)$$

V_r ,

$$\left(\frac{v_r}{\bar{W}_z} \right)^2 \approx 3\xi \frac{\rho_g}{\rho_l d} \cdot n \sqrt{1+n^2} r \quad (5.8)$$

$l -$

;

5.2.2

A:

$$= \frac{l \cdot W_\tau}{R \cdot W_a} \quad (5.9)$$

W $W_a -$

[216].

A

$$n = \frac{M_c \cdot C}{K_c \cdot D} \tag{5.10}$$

C – , 8/ ;
D – .

$$M_c = 4\rho \cdot W_a \cdot W_\tau \cdot R^2 \cdot l, K_c = \pi\rho W_a^2 R^2 \tag{5.11}$$

, n,
5.4.

n,

$$\theta = \frac{M}{K \cdot R} \tag{5.12}$$

M – ; K – ; R –

5.4 –

1	2	3
3	l $\frac{W_i}{W_a}$ n	$\frac{1}{3} \cdot \frac{d_2^3 - d_1^3}{d_2^2 - d_1^2}$ $\frac{d_2^2}{d_2^2 - d_1^2} \cdot \text{tg}\beta_2$ $\frac{8d_2}{3\pi} \cdot \frac{d_2^3 - d_1^3}{(d_2^2 - d_1^2)^2} \text{tg}\beta_2$

3	l $\frac{W_i}{W_a}$ n	$\left[r_1^1 + \frac{(d_1^1 + 2d_1)(d_1 - d_1^1)}{6(d_1^1 + d_1)} \right] \text{os}\beta_2$ $\frac{d_1^2}{2h_1(d_1^1 + d_1) \sin\left(\beta_2 + \frac{\pi}{z}\right)}$ $\frac{8d_1(d_1^2 - d_1d_1^1 + d_1^{12}) \text{os}\beta_2}{3\pi(d_1 + d_1^1)^2 \sqrt{4h_1^2 - (d_1 - d_1^1)^2} \sin\left(\beta_2 + \frac{\pi}{z}\right)}$
	l $\frac{W_i}{W_a}$ n	$\left[r_2^1 + \frac{(d_2^1 + d_2)(d_2 - d_2^1)}{6(d_2^1 + d_2)} \right] \text{os}\beta_2$ $\frac{d_2^2}{2h_1(d_2^1 + d_2) \sin\left(\beta_2 + \frac{\pi}{z}\right)}$ $\frac{8d_1(d_2^2 - d_2d_2^1 + d_2^{12}) \text{os}\beta_2}{3\pi(d_2 + d_2^1)^2 \sqrt{4h_1^2 - (d_2 - d_2^1)^2} \sin\left(\beta_2 + \frac{\pi}{z}\right)}$
	l $\frac{W_i}{W_a}$ n	$0,5d_1 \cdot \text{os}\beta_2$ $\frac{\pi d_1^2}{4h_1 \cdot z \cdot \varepsilon}$ $\frac{d_1^2 \cdot \text{os}\beta_2}{h_1 \cdot z \cdot \varepsilon}$
	l $\frac{W_i}{W_a}$ n	$0,5d_2 \cdot \text{os}\beta_2$ $\frac{\pi d_2^2}{4h_1 \cdot z \cdot \varepsilon}$ $\frac{d_2^2 \cdot \text{os}\beta_2}{h_1 \cdot z \cdot \varepsilon}$

[49],

n

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n ,

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1.

$$\Psi = \frac{W_{\max} - W_{\min}}{W_{cp}}, \%$$

(5.13)

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45°

$2 = 20^\circ \quad 30^\circ$

$2 \quad 30 \quad 45^\circ$

$2=30^\circ \quad (0,5 \div 0,6) d.$

$x = 0,2 + 0,3$

2

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$m=L/G,$ / . m

$$W = f(R)$$

[134].

$n,$

5.3

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- 1)
- 2)

– 4
20...80%.

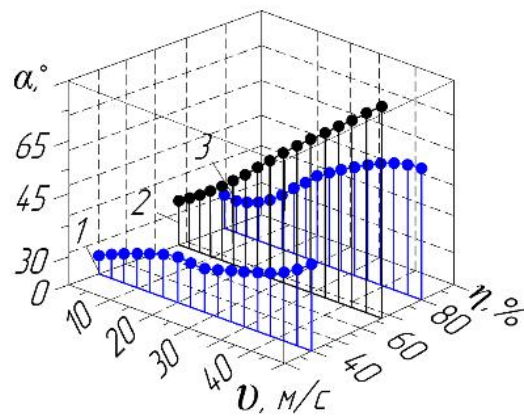
15 40 / ,
25°...65°.

(80%)

...45°

25 / .

45° ,



5.11 –
(η)

35°.

(3)

800

35° 550

45°.

5.12

27 /

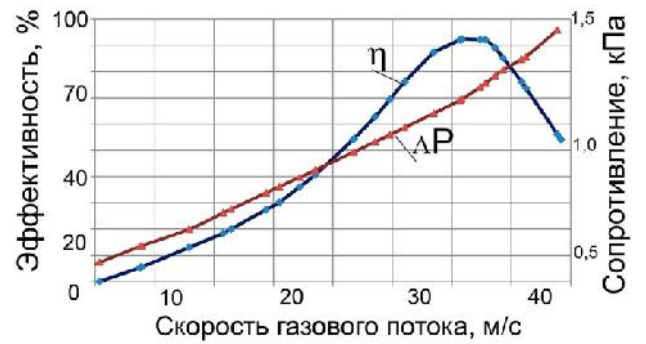
78 %.

30 /

40 /

63%.

578
 1425
 25 / ,
 78%,
 1200

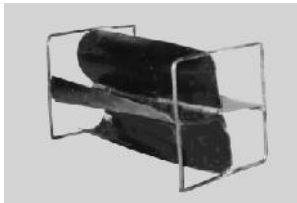


5.12 –

, ()

$$y = () = \frac{1}{\sqrt{2f}} \int_{-\infty}^{-\frac{y^2}{2}} \cdot dy , \tag{5.14}$$

$$= \frac{\lg \delta_{50} - \lg \delta_{\eta=50}}{\sqrt{\lg^2 \sigma + \lg^2 \sigma_{\eta}}} , \tag{5.15}$$



5.13 –

$$\delta_{\eta=50} = \delta'_{\eta=50} \cdot \sqrt{\frac{v' \cdot D \cdot \rho' \cdot \mu}{v \cdot D \cdot \rho \cdot \mu}}, \quad (5.16)$$

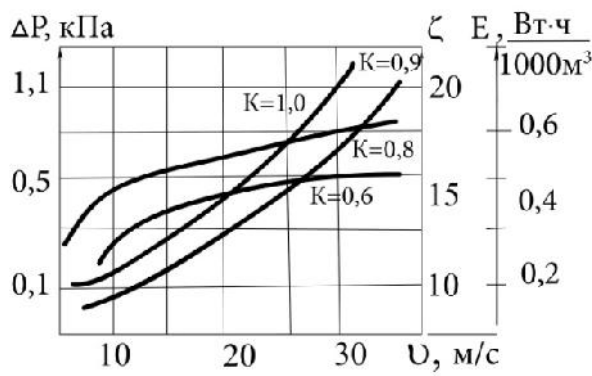
50% ;

5.14 5.15.

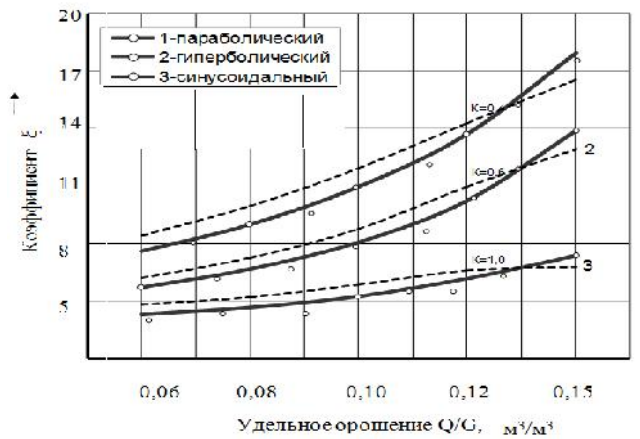
500

= 0,6

77% .



5.14 –



5.15 –

$$= \frac{32}{f^2} \cdot \frac{[\zeta]}{[x]} \cdot \frac{L}{D} \quad (5.17)$$

: = 1,4 · 0,72 .

(2)

tg .

d_p

12%,

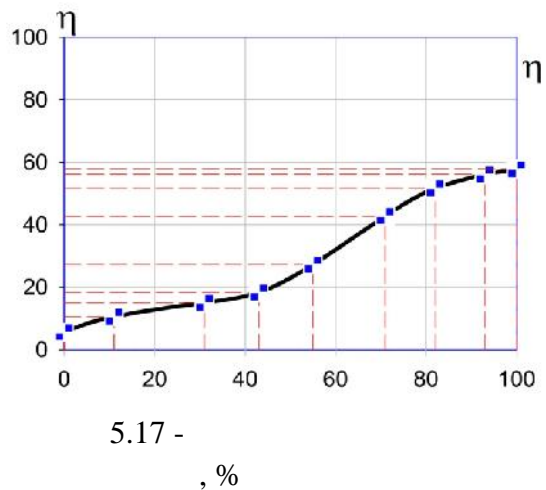
$$D = 16 \div 100, \Delta = 0,392 \div 0,720,$$

$$= 0 \div 1\% \quad p_p = 1150 \div 3200 \frac{1}{3},$$

$$d_{50} = 3,4 \div 3200,$$

$$p = 0,1 \div 0,4 \quad (\quad),$$

$$p = 500 \div 1400 \quad (\quad),$$



:

$$\Delta P = \Delta P_{-} + \Delta P_{+}$$

" " P

" "

:

$$\Delta = \Delta_{-v} + \Delta = \frac{\rho W_{cp}^2}{2} (\zeta_v + \zeta) \quad (5.18)$$

$P_v -$
 $P -$

;

P_{+}

$P_v,$

[102]

:

$$\Delta_v = \frac{\rho W_{cp}^2}{2} \cdot \frac{h_1}{d \cdot \sin^3 \beta_2}, \tag{5.19}$$

$h_1 -$, ;
 $W_{cp} -$, / ;
 $d = 4F / -$, ;
 $F -$;
 $-$, ;
 $2 -$,

[109],

$$\Delta = f(\bar{h}_1) \quad \bar{h}_1 = \frac{h_1}{l} \quad l = \frac{2S}{Z}$$

$h_1 -$;
 $l -$,
) =2, $l = 2$

$$=(2\div 2,5)l,$$

$$\Delta_v = \frac{\rho W_{cp}^2}{2} \cdot \frac{(r_2^2 + r_1^2) [\pi(r_2^2 - r_3^2)]^2}{16 [\pi(r_2^2 - r_1^2) - z\delta(r_2 - r_1)] \sin^2 \beta}, \quad (5.20)$$

$$r_3 - \quad , \quad ;$$

$$- \quad , \quad ;$$

$$W_{cp} - \quad , \quad / .$$

$$[80, 100]$$

$$[103]$$

$$\zeta \left(\frac{D}{d} \right)^n = f \left[\text{Re} \left(\frac{d}{D} \right)^2 \right] \quad (5.21)$$

$$D - \quad ;$$

$$\frac{D}{d} = 0,5 + \frac{8}{\pi^2} \left(\frac{S}{d} \right)^2 \quad (5.22)$$

$$S - \quad ;$$

$$d - \quad .$$

$$S/D = 2,65 \div 1,3$$

$$\zeta = \frac{0,705}{\text{Re}^{0,28}} \left(\frac{d}{D} \right)^{0,09} + 0,009 \left(\frac{d}{D} \right)^{0,65} \quad (5.23)$$

$$\text{Re} \ 5,9 \cdot 10^4.$$

$$S/D \ 1,75.$$

$$5\%.$$

$$S/D = 1,8 \div 2,5$$

$$\zeta = \frac{4,72}{\text{Re}^{0,35}} \left(\frac{d}{D} \right)^{0,74} \quad (5.24)$$

$$\text{Re}(S/D)^2 = 260 \div 6 \cdot 10^3.$$

$$\text{Re} \geq 5,5 \cdot 10^3$$

:

$$\Delta_v = 18,7 \rho W_{pl}^2 \text{Re}_g^{-0,25} F_{pl} \tag{5.25}$$

$$\text{Re} = \frac{W_{pl} \cdot d \cdot \rho}{\mu};$$

d –

, ;

W_{pl} –

, / ;

F_{pl} –

$$\text{Re} \geq 5,5 \cdot 10^3$$

:

$$\Delta_v = 1,4 \rho W_{pl}^2 (\quad) \tag{5.26}$$

$$\Delta_v = 0,9 \rho W_{pl}^2 (\quad)$$

[57].

[104]

,

v

$$\zeta_v = \exp\left(4,23 - 2,345 \frac{F_{pl}}{F}\right), \tag{5.27}$$

F_{pl} –

, ²;

F –

, ².

:

$$\zeta_v = 3,1 \alpha^{0,7} \left(\frac{B}{\varepsilon}\right)^{1,54} \left(\frac{h_1}{D}\right)^{-1,48} \tag{5.28}$$

— ;
B — ;
 — ;
 , .

v

$z=0$

[128].

$$=h_1/d_1$$

0,7÷0,8.

0,7÷0,8

$v=1$, ,

$$v = f(h_1)$$

[234].

h_1 0,6÷0,7

h_1

$$d_1 = d_1/D$$

$$d_2 = d_2/D$$

$$\zeta = \frac{0,025}{d_1^8} + \frac{30,5\bar{d}_2^4}{d_1} \tag{5.29}$$

$$v = f (d_1, d_2)$$

$$\bar{d}_{1,0} = 0,573 \cdot m^{-0,364} \tag{5.30}$$

$$m = \frac{z}{d_1}$$

1

$\beta_1 \geq 50^\circ$,

[134].

$$\zeta_v = 3,54 \left(\frac{0,025}{\bar{d}_1^8} + \frac{30,5 \cdot \bar{d}_2^4}{\bar{d}_1} \right) \cdot \cos^{10} \beta_2, \tag{5.31}$$

$$0,425 \leq \bar{d}_1 \leq 0,7; 0,4 \leq \bar{d}_2 \leq 0,8; \beta_1 \geq 50^\circ; 0 \leq \beta_2 \leq 15^\circ; \bar{h}_1 \geq 0,73.$$

[194].

$$z \quad F_{pl} = const$$

$$v = f(z)$$

« ».

$$F_{pl} = const, z = const$$

$$d_2 = d_2/D$$

$$v = f(d_2)$$

W_t

v.

$$\zeta_v = 8,5 \frac{z^{0,4} \cdot \sqrt{\bar{d}'_2}}{\bar{F}'_{pl}{}^2} \tag{5.32}$$

$$Re \geq 9 \cdot 10^4; z = 1 \div 8; \bar{d}'_2 = 0,05 \div 0,8; \bar{F}'_{pl} = 0,2 \div 1,0.$$

[239].

$$\frac{F}{F_{out}} \quad R_{out} \quad F_{out}$$

2,

:

$$\zeta_v = f\left(\frac{F}{F_{out}}; \frac{R_{out}}{R}; \beta_2\right) \tag{5.33}$$

:

$$\frac{F}{F_{out}} = \frac{out}{\pi \rho W_a^2 R^3} = \frac{F}{F_{out}} \cdot \frac{R_{out}}{R} \cdot \sin \beta_2 \tag{5.34}$$

... n [80] ... M_{out}

$$\zeta_v = \varepsilon \mu^{-2} \tag{5.35}$$

$\mu -$

$$\mu = \left[\left(\frac{F}{F_{out}} - 1 \right)^2 \sin^2 \beta_2 + \frac{2 - \Psi}{\Psi^3} \right]^{-0.5} \tag{5.36}$$

c -

$$c=1,1.$$

P_{out} ... $d \mu / d = 0:$

$$\frac{1 - \Psi}{\sqrt{\frac{\Psi^3}{2}}} = \frac{F}{F_{out}} \cdot \frac{R_{out}}{R} \sin \beta_2 \tag{5.37}$$

P ,

d_3

$$\Delta P = 1,45 \rho W_{cp}^2 \cdot \bar{d}_3^{-2,94} \tag{5.38}$$

$$= L/G \ 2$$

$$0,5 \div 1,0,$$

2

2

:

$$\zeta_{0v} = 2,44 \left(\frac{L}{G} \right)^{0,2};$$

$$\zeta_{0v} = 1,56 \left(\frac{L}{G} \right)^{0,2};$$

$$\zeta_{0v} = 5,2 \left(\frac{L}{G} \right)^{0,4}.$$

v

0,5÷0,6.

0,6

v

$$\text{Re}_g > 20000, \frac{S}{d} = 1$$

$$\zeta_{0v} = 8,6 \text{Re}_l^{0,17} \quad \text{Re}_l \leq 1700;$$

$$\zeta_{0v} = 0,8 \text{Re}_l^{0,45} \quad \text{Re}_l \geq 1700;$$

0,6

$$\zeta_{0v} = 5,2 \left(\frac{F_{pl}}{F} \right)^{-1,4} \cdot \left(10 \frac{L}{G+L} \right)^{-0,08} \quad (5.39)$$

0,6

$$\zeta_{0v} = 0,904 \frac{L}{G} + 8,2.$$

$$F_{pl}/F=0,4 \div 1,2 \quad \text{Re}_g \cdot 2 \cdot 10^4;$$

Re_g 30000

[160].

$$\text{Re}_g > 17800 \quad \frac{S}{D} = 1$$

:

$$\zeta_{0v} = 7,2 \text{Re}_l^{0,16} \quad \text{Re}_l < 1200;$$

$$\zeta_{0v} = 0,676 \text{Re}_l^{0,5} \quad \text{Re}_l > 1200;$$

[152]

$$\Delta P = 9,8 \cdot \rho_g \cdot W_{cp}^2 \left(16,1 \cdot 10^{-6} \bar{L} \cdot \text{Re}_g^{-1} \bar{H} + 1,21 \right), \quad (5.40)$$

— , / 3;

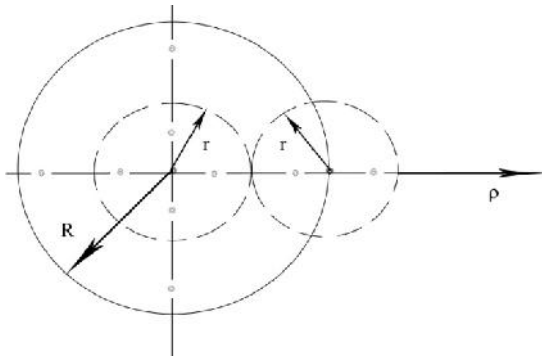
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5.4

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 . [154].
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5.17 -

$$\frac{\partial C}{\partial \tau} = D_d \nabla^2 C \tag{5.41}$$

$$C - \quad ;$$

$$D_d - \quad ;$$

$$r - \quad ;$$

$$(5.41)$$

$$\frac{\partial C}{\partial \tau} = D_d \left(\frac{\partial^2}{\partial r^2} + \frac{2}{r} \frac{\partial C}{\partial r} \right) \tag{5.42}$$

$$\frac{\partial(Cr)}{\partial \tau} = D_d \frac{\partial^2(Cr)}{\partial r^2} \tag{5.43}$$

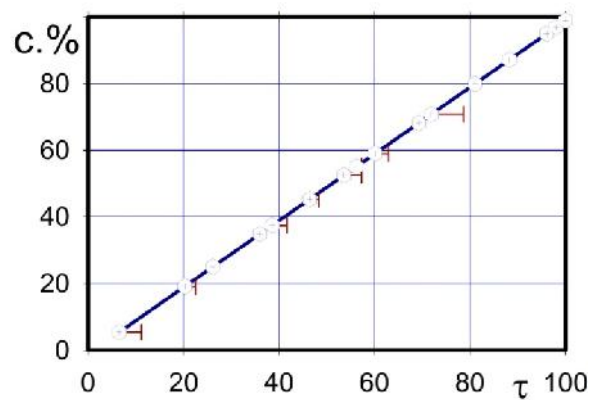
$$C' = 0 \quad r = 2R \quad (=0),$$

$$C' = C \quad = 0.$$

$$(5.43)$$

$$C' = C \left[1 - \frac{2R}{r} + \frac{2R}{r} \operatorname{erf} \left(\frac{r-2R}{2\sqrt{D_d \tau}} \right) \right] \tag{5.44}$$

N,
2R



5.18 -

$$J = -D_d (\partial C' / \partial r), \tag{5.45}$$

2R,

(dC / dr)

r=2R.

$$\vec{N} = 16\pi R^2 D_d \frac{\partial C'}{\partial r} \tag{5.46}$$

$r=2R$ (5.44)

$$\frac{\partial '}{\partial r} = \frac{C}{2R} \left[1 + \frac{2R}{\sqrt{\pi D_d \tau}} \right]. \tag{5.47}$$

, d ,

$$\bar{N}d\tau = 8\pi R D_d C \left[1 + \frac{2R}{\sqrt{\pi D_d \tau}} \right] d\tau. \tag{5.48}$$

d , ,

$C/2$:

$$16\pi R D C \left[1 + \frac{2R}{\sqrt{\pi D \tau}} \right] d\tau$$

d , :

$$\frac{dC}{d\tau} = -\frac{16}{2} \pi R D_d C^2 \left[1 + \frac{2R}{\sqrt{\pi D_d \tau}} \right]. \tag{5.49}$$

$C -$

K_0 :

$$K_0 = 16\pi R D_d = \frac{8kT}{3\mu_c} \zeta_c \tag{5.50}$$

(5.49),

:

$$\frac{dC}{d\tau} = -\frac{K_0}{2} C^2. \tag{5.51}$$

(5.51)

$C=C_0, =0, :$

$$\frac{1}{C} - \frac{1}{C_0} = \frac{K_0}{2} \tau. \tag{5.52}$$

(5.52)

5.18

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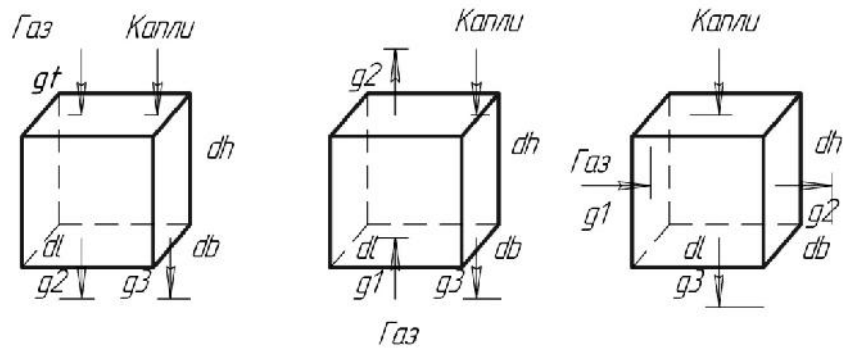
$$C = C_0 / (1 + \tau / \tau^t) \tag{5.53}$$

5.4.2

$$Q = 1/4 n \pi d^2 v_c \eta_\Sigma \tag{5.54}$$

$(0,5 \quad 0,7)$
 $= 2000 / ^3$
 $0,5$
 $(5.54),$

[23, 25].



5.19 –

– ; – ; –

$$dlldb dh \quad (5.19).$$

(*dl**db*)

$$V = \alpha v (dl db) \quad (5.55)$$

(*dbdh*).

$$g_1 = u (dl db) C \quad (5.56)$$

$$g_1 = u(dbdh)C \tag{5.57}$$

$$u - \dots, \dots \tag{5.58}$$

/ 3,

$$g_2 = u(dldb)(C - dC) \tag{5.58}$$

$$g_2 = u(dbdh)(C - dC) \tag{5.58}$$

$$=u- t \quad =u- l,$$

$$: \omega_l = u, v_l = 0$$

$$(5.55)$$

d_K

t_s

$$1/4C\omega\pi d^2\eta_\Sigma \tag{5.59}$$

$$6(dldb dh)\alpha/(\pi d^3) \tag{5.60}$$

$$g_3 = \frac{6\pi d_K^2 \alpha \omega C \eta_\Sigma}{4\pi d_K^3} (dldb dh) = \frac{3}{2} \cdot \frac{\alpha \omega C \eta_\Sigma}{d_K} (dldb dh) \tag{5.61}$$

$$g_1 - g_2 - g_3 = 0$$

$$uCldb - u(C - dC)dldb - \frac{3}{2} \cdot \frac{\alpha \omega C \eta_\Sigma}{d_K} dldb dh = 0 \tag{5.62}$$

$$uCbdh - u(C - dC)bdh - \frac{3}{2} \cdot \frac{\alpha \omega C \eta_\Sigma}{d_K} dldb dh = 0 \tag{5.63}$$

$$\omega = u \pm v$$

$$\frac{dC}{C} = -\frac{3}{2} \cdot \frac{\alpha \eta_{\Sigma}}{d_K} \cdot \frac{\omega}{u} dh \tag{5.64}$$

$$, \quad w=u \quad u=0,$$

$$\frac{dC}{C} = -\frac{3}{2} \cdot \frac{\alpha \eta_{\Sigma}}{d_K} \cdot dl \tag{5.65}$$

$m, \quad \text{ }^3/ \text{ }^3,$

:

$$m = \frac{V}{V} = \frac{\alpha v dl db}{u dl db} = \frac{\alpha v}{u} \tag{5.66}$$

$$m \frac{\omega}{v} = \frac{\alpha \omega}{u}$$

$$, \quad u=v$$

$$m = \frac{V}{V} = \frac{\alpha dl}{dh} \tag{5.67}$$

$$\alpha dl = mdh$$

(5.64), (5.65):

$$\frac{dC}{C} = -\frac{3}{2} m \frac{\omega}{v} \frac{\eta_{\Sigma}}{d_K} dh \qquad \frac{dC}{C} = -\frac{3}{2} m \frac{\eta_{\Sigma}}{d_K} dh \tag{5.68}$$

$$(\qquad) \tag{5.68}$$

$$\eta = 1 - \exp\left(-\frac{3}{2} m \frac{\omega}{v} \cdot \frac{H}{d_K} \eta_{\Sigma}\right) \tag{5.69}$$

$$\eta = 1 - \exp\left(-\frac{3}{2} m \cdot \frac{H}{d_K} \eta_{\Sigma}\right) \tag{5.70}$$

:

1) $\qquad \qquad \qquad ;$

2) $\qquad \qquad \qquad , \qquad \qquad \qquad ;$

3)

$$K_{1,2} = \pi(R_1 + R_2)^2 [\omega_0(R_2) - \omega_0(R_1)] \quad (5.82)$$

$$K_{1,2} = \pi(R_1 + R_2)^2 [\omega_0(R_2) - \omega_0(R_1)] \varepsilon(R_1, R_2), \quad (5.83)$$

$(R_1, R_2),$

$: R_1 \quad R_2,$

$$St_c \frac{d\bar{\omega}}{d\tau} = (\bar{v} - \bar{\omega}) [1 + \zeta_c (\text{Re}^* |\bar{v} - \bar{\omega}|)], \quad \bar{\omega} \rightarrow \bar{e} \quad \tau \rightarrow -\infty,$$

$$St_c = \frac{2 \rho_d R_1^2}{9 \mu_c R_2} \omega_0(R_2), \quad \text{Re}^* = \frac{R_1 \rho_c \omega_0(R_2)}{\mu_c}. \tag{5.84}$$

$$St_c - \omega_0(R_2) -$$

(5.84)

(5.83–5.84).

$$y = y_0, \quad y = y_0 \quad (y \rightarrow y_\infty \quad \tau \rightarrow -\infty)$$

$$y_0, \quad \varepsilon = y_0^2 / R_2^2. \tag{5.85}$$

[14, 15].

[30]

$$\varepsilon \approx \begin{cases} \frac{k_c^2}{(k_c + 0,5)^2} & k_c > 1/12 \quad Re \gg 1000 \\ \left(1 + \frac{3}{4} \frac{\ln 2k_c}{k_c - 1,214}\right)^{-2} & k_c > 1,214 \quad Re \ll 1000 \end{cases} \quad (5.86)$$

(5.86)

[117, 194],

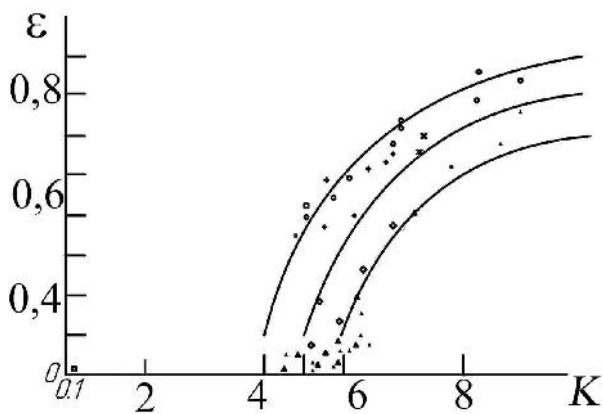
$$\varepsilon \approx \frac{1}{1 + Re/30} \left[\left(1 + \frac{3}{4} \frac{\ln 2k_c}{k_c - 1,214}\right)^{-2} + \frac{k_c^2}{(k_c + 0,5)^2} \frac{Re}{30} \right] \quad (5.87)$$

[51, 117]

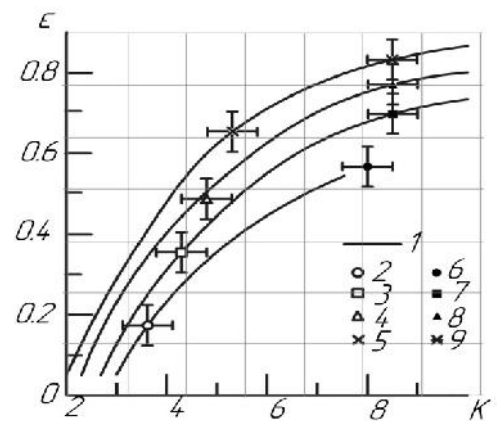
$k_c \quad 1 \quad Re \quad 1000$

(5.87)

5.20 5.21.



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5.21 -

1 Re 1000

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$$3 \quad 62 \quad / \quad ^3.$$

$$40^0 \div 45^0$$

$$25 \quad / \quad .$$

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$$1,3 \div 2,0 / ^3 .$$

$$60 / ^3$$

(98÷99%)

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$$10 / ^3 .$$

98÷99%

$$0,05 \div 0,1 / ^3 ,$$

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$$200 \div 300 / ^3$$

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$$3 \div 3,5 / .$$

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o [21, 129, 139, 223].

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$$-Qdc = v \cdot dF \tag{6.1}$$

Q - o

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- o

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(6.1)

$$\int_{c_x}^{v_x} \frac{dc}{c} = \frac{v \cdot F}{Q} \tag{6.2}$$

(6.2)

o

100 %,

(6.2)

$$v = \frac{(\rho_p - \rho) \cdot d_p^2 \cdot v^2}{18\mu R}$$

:

$$S_{tk} = \frac{(\rho_p - \rho) \cdot d_p^2 \cdot v}{18\mu R}$$

:

$$K_r = \frac{v_\phi}{v_r}$$

$$N = \frac{v}{Q} \cdot F - S_{tk} \cdot K_r \quad (6.3)$$

, (6.3)

$$E = \frac{\varepsilon}{S_{tk} \cdot K_r} \quad (6.4)$$

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(6.4),

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 St_K

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$$\tau_p \frac{(\rho_p - \rho) \cdot d^2}{18\mu}$$

$$\tau = \frac{R}{v}$$

/

*

$$E^* = \frac{\zeta}{K_r} \tag{6.5}$$

(2.32)

(6.5) :

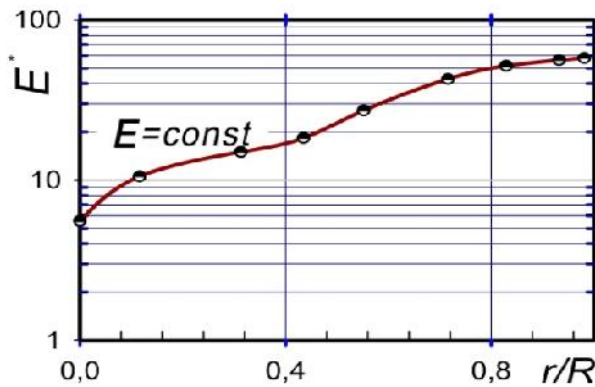
$$E^* = \frac{\zeta \cdot r}{v} = \frac{x}{v \cdot r} \cdot \int_0^x \frac{r}{\tau_0 x^2} dx \tag{6.6}$$

(6.6)

r ,

(6.6)

* r .



6.1,

*=10

r =0,

0 < r_0 < 0,2

const,

r > 0,4

6.1 -
*

20%

, ...

$$r < 0,2.$$

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$$r = 0,2$$

$$r = 0,$$

(3),

$$\frac{S}{S - S_0}$$

,

$$\xi = \frac{2(\rho - \rho_0)}{\rho v^2} \quad (6.7)$$

$$\xi = \left(\frac{S}{S - S_0} \right) \quad (6.8)$$

$$\frac{S}{S - S_0} \approx 1$$

[146, 154]

$$S = S - S_0 \tag{6.9}$$

$$r^2 = r^2 - r_0^2 \tag{6.10}$$

(2.29) , 0,5 1,0 d

$$(\rho_r - \rho) \frac{\pi d_r^3}{6} \cdot \frac{v_\phi^2}{r} = \frac{24a}{Re} \cdot \frac{\pi d_r^2}{4} \cdot \frac{\rho v_r^2}{2} \tag{6.11}$$

$$a = \frac{1}{0,848 \cdot \lg \frac{\xi}{0,057}}$$

[81]:

$$Re = \frac{v \cdot d \cdot \rho}{\mu}$$

Re –
d –

$$(6.11) :$$

$$\frac{(\rho_r - \rho) d_r^2 \cdot v_\phi^2}{18 \mu r a} = \frac{v}{v} \tag{6.12}$$

: r ,

$$(6.12)$$

$$\frac{(\rho_r - \rho) d_r^2 \cdot v_\phi^2}{18 \mu r a} = \frac{v_\phi r v}{r v_\phi^2} \tag{6.13}$$

(6.13)

(6.13)

 $r_{in.}$ $r_0 > 0,2;$ $r_0 < 0,2.$ $15 \div 20^\circ,$

, (.2.3) ,

$$v_{\varphi r} = v_{\varphi} \tag{6.14}$$

:

$$\varphi a \frac{Q}{h} = \varphi \cdot a \frac{a}{h} \tag{6.15}$$

$$\frac{Q}{Q + Q_0} = K \tag{6.16}$$

(6.15)

$$\frac{\varphi a h}{\varphi_a h} = \frac{1 - K}{K} \tag{6.17}$$

(6.17). ,

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- (6.7) (6.8)

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- $r < r < r$

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1.

$$D = 1,26 \sqrt{\frac{Q}{W}} \quad (6.18)$$

2.

$$D' = (0,75 \div 0,85) D$$

3.

$$z = (10 \div 25) D'$$

4.

$$l_{\Lambda} = \frac{0,5 D_i \sin \frac{360}{z_i}}{\sin(\alpha_y + \frac{360}{z_i})} \quad (6.19)$$

35° 45°.

5.

$$\omega_o = 397,38 \cdot w^{1,65} (m \cdot 10^6)^{0,31} \bar{D}^{-0,31} \cdot \bar{z}^{1,05} \times \exp[-0,018 \cdot 10^6 d_p - (1,06 + 0,034 w) \cdot \cos \alpha - 2,18 \cdot \cos^2 \alpha] \quad (6.20)$$

>90°.

7.

$$\Delta p_{\omega > 0} = \frac{0,5 \rho \omega D_1 (0,5 \omega D_1 - W_1 \cos \alpha)}{1 + \frac{1,5 + 1,1 \alpha / 90^\circ}{z(1 - d_1^2)}} \quad (6.21)$$

8.

1 000 ³ .

0,475 .

$$P = Q \cdot \Delta \rho \tag{6.22}$$

6.5

500 600° ,

250 ° .

(): 17% O₂; 16%N₂; 67 % .

70 / ³ SO₂; 30 / ³ H₂S; 200 / ³ F 20 / ³ Cl.

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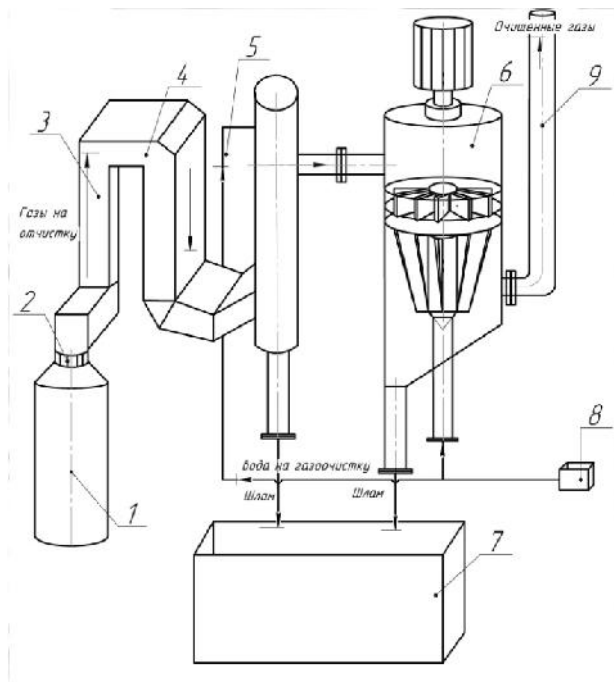
(6.2).

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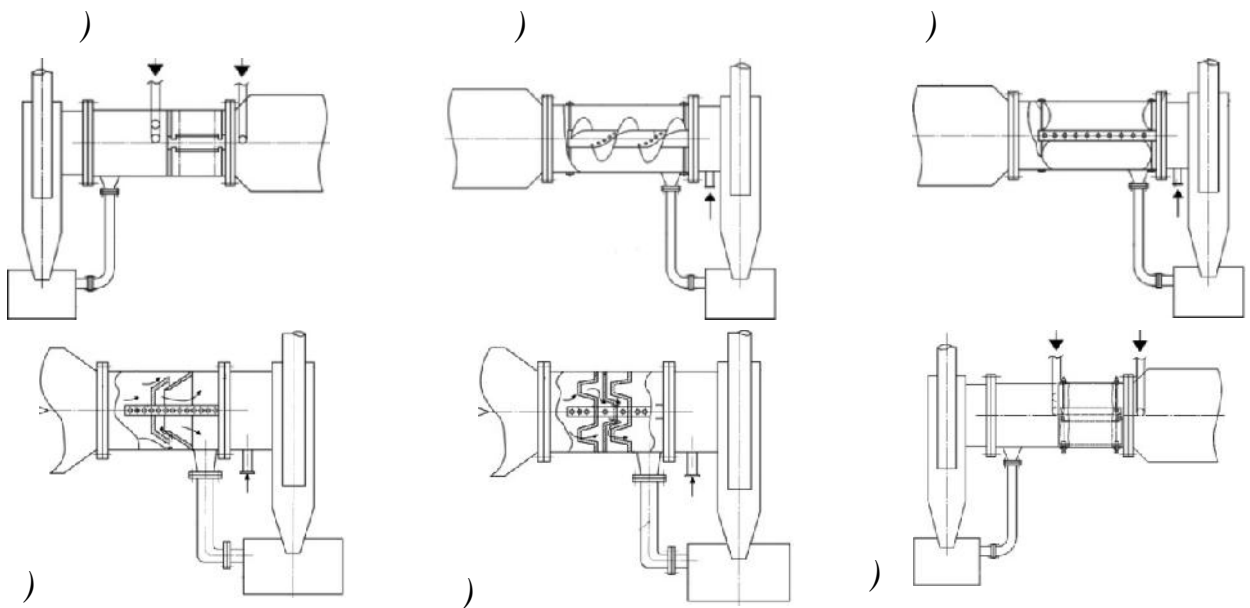
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 500 10000 ^{3/} .

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- 2403951; - 2234358

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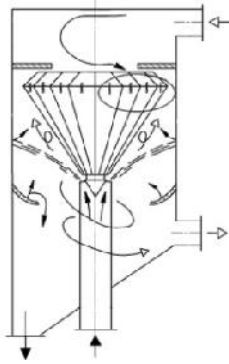
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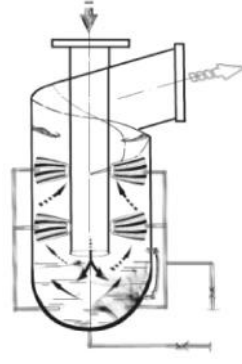
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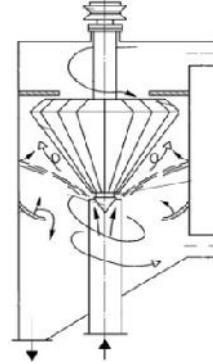
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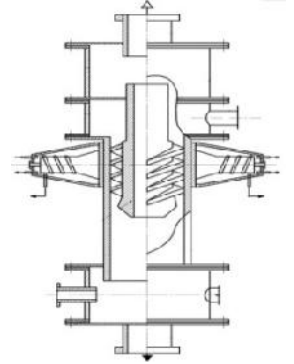
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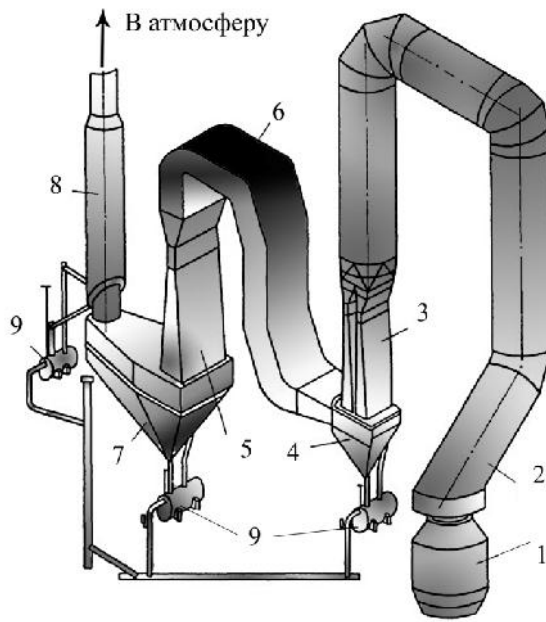
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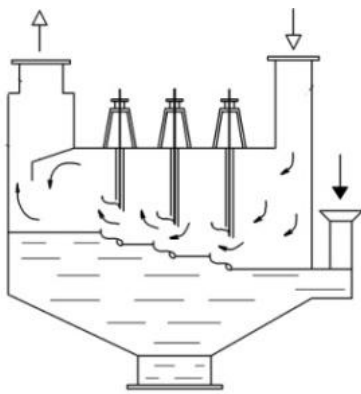
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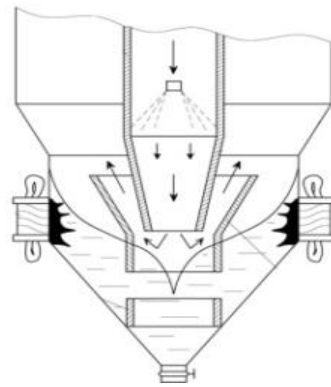
6.2 –

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[29, 30].

$$= \frac{1}{N} \cdot \sum_{i=1}^N A_i \cdot m_i,$$

N

$$= \sum_{i=1}^N A_i \cdot m_i,$$

$m_i =$

$$m_i = (1 - \eta_i) \cdot m_{oi}.$$

$\rho =$

$$m_i = \rho \cdot Q_i.$$

m

$$m = \frac{\sum_{i=1}^N A_i \cdot (1 - \eta_i) \cdot C_i}{\sum_{i=1}^N \eta_i \cdot C_{oi}} \tag{6.23}$$

$\eta_i = \eta$

$$= \frac{1}{N} \cdot \sum_{i=1}^N A_i \cdot C_i \quad m = \frac{\cdot \cdot (1 - \eta)}{\eta}$$

$$m \hat{E} \min. \quad m$$

$$= \frac{\sum_{i=1}^N \eta_i \cdot c_i}{\sum_{i=1}^N A_i \cdot (1 - \eta_i) \cdot c_i} \quad (6.24)$$

$N=1$

$$\varepsilon' = \frac{\eta_1}{\eta} \cdot \frac{1 - \eta}{1 - \eta_1} \quad (6.25)$$

$\rightarrow \max.$

$$: \quad = \quad 0 \quad - \quad 1,$$

$$, \eta_i = 0.$$

$= \quad /$

$$= \frac{\sum_{i=1}^N A_i \cdot C_i \cdot \eta_i}{\sum_{i=1}^N A_i \cdot C_i} \quad (6.26)$$

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 $\eta_i = \eta$, , $= \eta$. , -
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$$\Delta = I - 2 \Delta .$$

$\rightarrow \max$

$$=(U \setminus U) \rightarrow \max.$$

$$I = Uc \cdot Q (/),$$

$\Delta Y = \Delta C / \rho (/)$

$$Z = C \cdot Q \cdot \Delta P .$$

- , (/)

$$\begin{aligned}
 & m \quad : \\
 & \quad \cdot \rho \cdot \sum_{i=1}^N A_i \cdot C_{oi} \cdot \eta_i \\
 & = \frac{\quad}{C \cdot \Delta} \quad (6.27) \\
 & - \quad ; \\
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 & B - \quad - \\
 & (\bar{i} \quad).
 \end{aligned}$$

$$\varepsilon = \frac{\Delta P \cdot \eta_1}{\Delta P_1 \cdot \eta} \quad (6.28)$$

6.3 –

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6		²	6,4	4,7
7		.	24	28

8		.	0,627	0,475
	1000 ³			
9		/	-	0,4
10			1,0	1,85

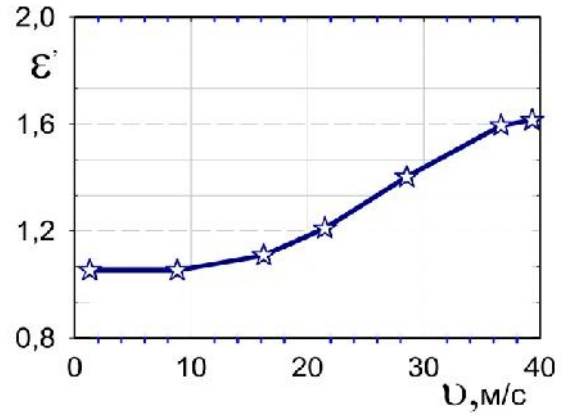
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$$U', U'_r, U'_z, \dots (r, z)$$

Ansys CFX.

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, . . . $\hat{\alpha} = 100 + 110^\circ$;

(30 /) (100 ⁻¹).

4.

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30÷38%

5.

94%.

6.

26

/ .

$D -$;
 $F -$ 0 ;
 $F -$ 0 0 ;
 $G -$;
 $L -$;
 $M -$ 0 0 ;
 $M -$ 0 0 ;
 $M -$ 0 0 ;
 $P -$ 0 ;
 $P -$;
 $P -$;
 $P -$;
 $Re -$ 0 ;
 $R -$;
 $R_1, R_2 -$;
 $Re -$;
 $Stk -$;
 $Sh -$;
 $U_\varphi, U_x, U_r -$ 0 0 , 0 ;
 $V_\varphi, V_x, V_r -$ 0 , 0 ;
 $W_\varphi, W_x, W_r -$ 0 , 0 ;
 $V -$ 0 ;

V_{\dots} ;
 \dots ;
 \dots ;
 n_{\dots} ;
 \dots ;
 \dots ;
 \dots ;
 z_{\dots} ;
 r_{\dots} ;
 K_{\dots} ;
 \dots ;
 C_{\dots} ;
 a_{\dots} ;
 b_{\dots} ;
 d_0_{\dots} ;
 d_{\dots} ;
 d_{\dots} ;
 $r_{\varphi m}$;
 z_{\dots} ;
 \dots ;
 \dots ;
 \dots ;
 φ_{\dots} ;
 \dots ;
 m_{\dots} ;
 \dots ;
 \dots ;

\dots ;
 \dots ;
 $a - \dots$ 0 ;
 \dots ;
 \dots ;
 $h - \dots$;
 $\mu - \dots$;
 \dots ;
 $\dots, C - \dots$;
 \dots ;
 $k, - \dots$;
 $R^2 - \dots$;
 $R_k - \dots$;
 $DW - \dots$;
 \dots ;
 \dots ;
 $n - \dots$;
 $d_{20} - \dots$;
 $\lg - 0$ 0 (0) ;
 \dots ;
 \dots ;
 $\lg \eta - \dots$;
 $\min - \dots$.

0 - ;

i - ;

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d - ;

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1. , . : , 1999. – 248 .
2. , /
- , 1988. – 81 .
3. ,
. : , 1983. – 351 .
4. ,
// , 1988. 8. .45-48.
5. /
. : - , 1986. – 240 .
6. ,
/ , 1981. – 28 .
7. , , // /
. , 1987. 5. – .23.
8. ,
. : , 1989, 40 .
9. ,
. – . : , 2005. – 163 .
10. ,
. : , 1989. – 456 .
11. ,
// – , 1984. – 8. – .50-54.
12. ,
. : , 1987. – 328 .
13. ,
. : , 1993. – 496 .
14. , : ,
1982. – 248 .
15. ,
. : , 1985. – 216 .

16. , . , . . .
 .: , 1980. – 320
17. , . , . . . , . . .
 . .: , 1981. – 392 .
18. -
 . . . 18.
 . 1-41-00. , 2001. 126 .
19. / . ., 2009. 6(25). 26 .
20. . . 861914 , 01 47/14. /
 . . . , 1981. . 33.
21. . . 469874 , 01 47/06. /
 . . . , 1973. . 17.
22. . . 1421379 , 01 47/06. - /
 1988. . 33.
23. . . 1430073 , 01 47/06. /
 . . . , 1988. . 38.
24. . . 1185674 , 01 47/06. /
 . . . , . . . , 1995. . 36.
25. . . 1438829 , 01 47/06. /
 . . . , 1988. . 43.
26. 2091137 , 01 47/14. / . . . ,
 . . . , 1997. . 27.
27. 2054306 MK B01D47/15. /
- B.H. , A.M. B . 1996. . 5.
28. , . .
 . - .: , 1988. – 368 .
29. Smoluchovski, . Zeit. Phys. Chem., 92, 129. 1917.
30. , . , . . . -
: . 1982.– 199 .
31. , . , . . . :
 .: . 1936.– 607 .

32. , . „ 1993. – 109 .
33. ,
.: , 1978. – 144 .
34. , 1983. – 296 .
35. , „ 1981. – 480 .
36. , –
1983. – 265 .
37. , . . „
. , 1979. 312 .
38. ,
// . 1987. . 21, 3. . 411-415.
39. , . . „
- - - - - // . 1984. . 18.
1. . 66-68.
40. ,
: 1986. – 543 .
41. , . . . Ky e . . „
/ , 11, . 62, 11, 1989. c.2486-2490.
42. , A.M.
.: , 1990. – 288 .
43. , . . . , . . . ,
.: , 1991. – 319 .
44. , . . „
. – , 1985. – 306 .
45. , . . „
. – , 2003. . 65.
46. , : , 1981 – 366 .
47. , . . „ – , 1990. – 72 .
48. , . . „
. 1996. 5, . 3-19

- 49. , 1998. – 307 .
- 50. / – ∴
- 2016. – 640 .
- 51. , ∴ , 1968 – 114 .
- 52. : 1985, 35 .
- 53. , – ∴ , 1989. – 512 .
- 54. , , , – ∴ , 1985. – 352 .
- 55. , , 2000. – 800 .
- 56. , ∴ , 1985. – 302 .
- 57. , y r . ∴ r , 1990. – 400 .
- 58. , r r . ∴ r , 1987. – 328 .
- 59. , - r . . 1-3. – . 2006. – 634 .
- 60. , - r : . . 1-3. . 2006. – 1820 .
- 61. , // . , 1981. .206-209.
- 62. , ∴ . 1986. – 630 .

106. 2339435 . / . . //
 .27.11.2008. . 33.
107. , . . , , / . . //
 . . , 1960. – 347 .
108. , : , 1984. – 108 .
109. , . . . – : , 1998. – 320 .
110. , . / . . : , 1959. – 566 .
111. Coufont, C. Forces on spherical particles in terms of upstream flow characteristics / . Line. – 9 French chemical Engineering Congress, Saint – Nazaire, 9-11 Sept. 9. 2003. 1206-1211 . .
112. Hinze, J. O. Turbulence / J.Hinze. – McGraw-Hill, New York, 1975.
113. Schubert, H. The role of turbulence in unit of particle technology / 2nd World Congress Particle technology (September 19-22. 1990) – Tokyo, 3. 1990. 55-67 . .
114. , . . // . I980. . 6. . 237-250.
115. , . . , : , 1989. 24 .
116. , . . , // . 1992. . 3, 3. . 165-180.
117. , // 1990. . 7. 3. . 456-459.
118. , : , 2002. – 536 .
119. , . . , – : , 12. : , 1979, . 70-109.
120. , – : . . 25. : , 1963, . 108- 120.
121. Marble, C. Forces on spherical particles in terms of upstream flow characteristics / . Coufont, Nazaire, 9-11 Sept. 9. 2004. 1007-1011 . .

122. . . .
 ∴ , 1976. – 296 .
123. , ∴ . 1972. – 440 .
124. , 1 2. ∴ , 1970. – 1068 .
125. , . . , ∴ ,
 . ∴ , 2008, . 25-39.
126. , . . , . . ,
 ∴ , 1985. – 192 .
127. , ∴ , 2003. – 840 .
128. , . . , . . ,
 . – ∴ , 1993. – 320 .
129. , . . ,
 // . - . 1996. 8. . 45-47.
130. , : . 1965. 53 .
131. , . . , . . ,
 . – ∴ , 2005. – 163 .
132. ,
 : " " , 1992. – 301 .
133. , . . ,
 // . – , 1984. – 8. – . 50-54.
134. Hugo, A., Hallvar d F. Theoretical analysys of fluid partical collisionese in turbulents flow// Chemical Engineering Science. – 1999. 21. – . 4749-4755.
135. Shubert, H. The Turbulence in particles technology// World Congresse. “Particle technology.” Tokyo, Pt-3. 1990. . 55-67.
136. , . . , , ,
 1983, . 5. . 150-156
137. , . . ,
 //
 , 2004. 9. – . 54-57.

138. . . . // . . .1996. 7. .8-13.
139. , . . „ . . .
 . . .: ,1997.173 .
140. , . . „
 . . . , ,1953. .25-34.
141. , „ „- .: ,1987.- 588 .
142. ,: . . .
- 1988.- 256 .
143. , . . „ . . „ . . .
 .- .: ,1987.- 282 .
144. , . . „ . . „ ,
 .: ,1958.- 152
145. , . . „ - , - .: ,1989.- 152
146. , . . „- .: ,1987.- 92 .
147. , . . „ . . „ . . „ . . .
 //
 ,1997.- 8.- .12-13.
148. ,
 .: ,1961.- 170 .
149. , , ,1981. - 616 .
150. , . . . /
- 2 .- .: ,1983.- 312 .
151. , - .: - . - ,1982.- 240 .
152. , - .: ,
 1994.- 180 .
153. ,- .: - ,1999.- 320 .
154. Fraser, R. P., Sixth Symposium (International) on Combustion, 1957, New York, London.
155. Giffenen, E., Lamb, A. J., The effect of air density on spray atomization, The Motor Industry Research Ass., Report 5, 1953.
156. Pohlhausen, K, Zeitschr, F. angew. Math, und Mech.,1921, No 1.

157. Tate, R. W., Marschall, W. R., Atomization by centrifugal pressure nozzles, Chem. Eng. Progress, 1953, 49, 4 a. 5.
158. Taylor, G. I., Proc. of the 7-th Internal. Congress for appl. Mechanics, 1948, 2, part 1.
159. Taylor, G. I., The Quart. Journ. of Mech. a. Appl. Mathematics, 1950, 3, part 2.
160. Turner, G. M., M ult n, R. W., Drop size distribution from spray nozzles, Chem. Eng. Progress, 1953, 49, 4.
161. Tresch, Chemie Eng. Technik, 1954, 26, 6.
162. Nu i ama, S., Tanasawa J., Experiments on the atomisation of liquids in an air stream, Rep. 1 Trans, from Trans. Soc. Mech. Eng. (Japan), 1938, 4, 14.
163. Nukiyama, S., Tanasawa, J., Experiments on the atomisation of liquids in an air stream. Rep. 4 Trans, from Trans. Soc. Mech. Eng. (Japan), 1938, 5, 18.
164. , O.H., B.A. A // .
- : T CO AH CCCP, 1997. C. 124-130.
165. , . . - , 2008. – 246 .
166. , . . , 3. . // . : , 1988. . 123-127.
167. , . , . . : - . 1989. 679 .
168. Rad liffe, ., Iare, H., Rep. NR 144 British NGTE, 1953.
169. Miesse, . , Cor elation of expe imental data on the disinteg ation of liquid jets, Industry a Engineering Chemistry, 1955, 47, Ns 9.
170. , . . , . . : 1981, 38 .
171. , . . , . . , . . . 1988, .44 .71-77

201. / , 2009. 6(25). – 26 .
202. , 1960. – 96 .
203. Rietem , . Liquid-solid separation in a cyclone: The effect of turbulence on separation // Proc. of the symp. of the internation between fluid and particles. L., 1962. P. 276-281.
204. Rietema, K. Performance and desing of hydrocyclones // Chem. Engineering Science 1981. Vol. 16. N 3/4. P. 290-325.
205. Rtonsheidl, F.D., Mason S.D. Particles motion of sheared suspension//I. Colloid and Interface Sci. 1961. Vol. 16. P. 210-261.
206. Schubert, H. Zur Prozessbestimmenden Rolle der Turbulenz bei Aufbereitungsprozessen. I. T. // Aufbereitungs. Technology. 1984. Bd. 15, N 9. S. 501-512.
207. Schinnzaki HTakasaka A., Nakamura M. et al. A practical multiple cyclone arrangement for improved classification//Chem. Eng. 1961. Vol. 25, N. 5. P. 329-338.
208. , 2012. – 23 .
209. Tarjan, D. . Computation of the peripherale velocity appearing of the radius on the hydrocyclons f om the veloc ty on the ente ing slu y // Techn. Eng. 1981. Vol. 33. 1/2. P. 119-133.
210. Tarjan, D. . Some theo etic question classifyin and sepa atin hyd oyclone // Ibid. 1981. Vol. 32, N 3/4. P. 357-388.
211. Trawinsky, H. Der Hydrozyclon als Hilfsgerat zur Grundstolfveredelung // Cheming and Technology 1973. Jg. 25, N 6. S. 331-340.
212. Trawinsky, H.F. Practicl aspecte of the desigung and industrial application of the hydro-cyclon // Cheming and Technology. 1979. July/Aug. P. 361-367.
213. ,
- o x . 2007. 1. . 166-171.
214. , // 1999 T. 22, 5. . 630-634.

215. , . . y
- // 1991. .54, 9. .2066-2070.
216. , : - -
.1953.– 493 .
217. , . . y
// 1981.
.24, 1. .I 19-124.
218. , . . y
// .1986 .59
7. .1623-1624.
219. , . . , . . y
//
. . : ,1983. .80-83.
220. ,
// . . :
.1978. .125-132.
221. , : . .
1981.– 447 .
222. , . . C c c
c c // M .
. : ,1978. .70-101.
223. , : 1996. – 287 .
224. , : ,1975. – 373 .
225. ,2016. – 227 .
226. , : ,1979. – 536 .
227. - / .
. . : ,1980. – 172 .
228. ,
. : ,1983. – 351 .

229. ,
 ∴ , 1975. – 558 .
230. , , 1962
 . – 512 .
231. , – , 1980, 11,
 . 2471-2474.
232. , , 1999, 3, . 27-35.
233. , ∴ ,
 1984. – 168 .
234. , A.H - . : -
 , 1985. – 200 .
235. ,
 ∴ , 1989. – 286 .
236. , ∴ , 1981. – 192 .
237. ,
 ∴ , 1982. – 260 .
238. , : , 1981. – 366 .
239. , - ,
 1973. – 19 .
240. , ∴ .
 1985. – 327 .
241. , 2- , . . ∴ , 1980. –
 358 .
242. ,
 . 3- . ∴ , 3. – 440 .
243. .
 ∴ , 2006, . 2, – 141 .

- 10.12.2012 . 20.05.14, . 14
260. 2519423 " - o " / . . a a,
 . . // . 26.12.2012. . 100614, . 16
261. 0 17.2.3.02-98. O a o . A o a.
 . . : , 1999. – 45 .
262.
 p ,
 p p . . : , 2006. – 14 .
263.
 .
 . . : r . 2001. – 52 .
264.
 -
 . . : , 1984. – 104 .
265.
 -
 . . : . 1987. – 46 .
266.
 , : .
 . . . , 2008. – 192 .
267. . 2- ./ : , 2000. – 200 .
268. / - : - ,
 2000. – 510 .
269. , . . : , .
 / . . , : - .
 . . , 2002. – 387 .
270. , . . : , . . :
 « » , 2004. – 220 .